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Chapter 1
Introduction

This manual assumes the reader has an engineering background in the general area of structural steel design and is already familiar with CSA S16-09 code.

Initiation of the design process, along with control of various design parameters, is accomplished using the Design menu. The design/check of composite beams is seamlessly integrated within the program.

Automated design at the object level is available for any one of a number of user-selected design codes, as long as the structures have first been modeled and analyzed by the program. Model and analysis data, such as material properties and member forces, are recovered directly from the model database, and no additional user input is required if the design defaults are acceptable.

The design is based on a set of user-specified loading combinations. However, the program provides default load combinations for each supported design code. If the default load combinations are acceptable, no definition of additional load combinations is required.

Composite beam design/check consists of calculating the flexural, axial, and shear forces or stresses at several locations along the length of a member, and then comparing those calculated values with acceptable limits. That comparison produces a demand/capacity ratio, which typically should not exceed a value of one if code requirements are to be satisfied. The program follows the
same review procedures when it is checking a user-specified shape or when checking a shape selected by the program from a predefined list.

The program checks the requirements for strength and deflection limit states at service and construction time conditions. It also checks vibration for service time condition. It considers shoring-unshoring phases if shoring is used. It calculates camber if it is required.

The program can determine the number of steel headed stud anchors required to achieve the desired level of composite action. On the other hand, the program can check the adequacy if the profile—number and distribution—of the steel headed stud anchors is provided.

Program output can be presented graphically on the model, in tables for both input and output data, or in calculation sheets prepared for each member. For each presentation method, the output is in a format that allows the engineer to quickly study the stress conditions that exist in the structure, and in the event the member is not adequate, aid the engineer in taking appropriate remedial measures, including altering the design member without re-running the entire analysis.

The program supports a wide range of composite beam design codes, including many national building codes. This manual is dedicated to the use of the menu option “CSA S16-09.” This option covers the “CSA S16-09 — Specifications for Structural Steel Building” (CSA S16-092009). The implementation covers load combinations from “NBCC 2010,” which is described in the section “Design Load Combinations” in Chapter 3. The loading based on “NBCC 2010” has been described in a separate document entitled “CSI Lateral Load Manual” (CSI 2012).

The design codes supported under “CSA S16-09” are written in Newton-millimeter units. All the associated equations and requirements have been implemented in the program in Newton-millimeter units. The program has been enabled with unit conversion capability. This allows the users to enjoy the flexibility of choosing any set of consistent units during creating and editing models, exporting and importing the model components, and reviewing the design results.
1.1 Organization

This manual is designed to help you quickly become productive using the CSA S16-09 composite beam design option. Chapter 2 addresses prerequisites related to modeling and analysis for a successful design in accordance with the code. Chapter 3 provides detailed descriptions of the specific requirements as implemented in the program for the code.

1.2 Recommended Reading/Practice

It is strongly recommended that you read this manual and review any applicable “Watch & Learn” Series™ tutorials, which are found on our web site, http://www.csiamerica.com/, before attempting to design a composite beam. Additional information can be found in the on-line Help facility available from within the program.
Chapter 2
Design Prerequisites

This chapter provides an overview of the basic assumptions, design preconditions, and some of the design parameters that affect composite beam design.

2.1 Design Codes

The design code can be set by the user when the model is started and changed at any time. Any one design code can be used in any one design run. A group of beams cannot be designed using one code and another set of beams designed for a different code in the same design run. However, different design codes can be used to perform different design runs without rerunning the analysis.

2.2 Units

For composite beam design in this program, any set of consistent units can be used for input. Typically, design codes are based on one specific set of units. The documentation in this manual is presented in Newton-millimeter-seconds units unless otherwise noted. However, any system of units can be used to define and design a building in the program.
2.3 Preferences

The composite beam design preferences are basic assignments that apply to all composite beams. Default values are provided for all preference items. Thus, it is not necessary to specify or change any of the preferences. However, at least review the default values to ensure they are acceptable. Some of the preference items also are available as beam specific overwrite items. The preferences are described in Appendix A. The overwrites are described in Appendix B. Overwritten values take precedence over the preferences.

2.4 Overwrites

The composite beam design overwrites are basic assignments that apply only to those beams to which they are assigned. Default values are provided for all overwrite items. Thus, it is not necessary to specify or change any of the overwrites. However, at least review the default values to ensure they are acceptable. When changes are made to overwrite items, the program applies the changes only to the beams to which they are specifically assigned. Overwritten values take precedence over the preferences. See Appendix B for more information about overwrites.

2.5 Composite Beam Properties

This section provides an overview of composite beam properties. Items described include beam properties, metal deck and concrete slab properties, shear connector properties, user-defined shear connector patterns, cover plate properties, effective slab width and beam unbraced length.

The many properties associated with composite beams are defined using various menus in the program. Other items related to the beam properties are specified in the Composite Beam Design Preferences or Overwrites forms.

2.5.1 Beam Properties

Figure 2-1 shows a typical composite beam for reference. The beam shown is a rolled beam section from the built-in section database.
Basic steel beam properties can be user defined along with the basic geometry of the steel section, except for the cover plate, if it exists. Cover plates are specified in the composite beam Overwrites. When defining a beam, a material property that includes the yield stress for that beam is also assigned. That yield stress is assumed to apply to the beam and the cover plate unless it is revised in the beam overwrites.

The Composite Beam Design postprocessor designs beams that are I-shaped sections and channel sections only. The beam section for a composite beam can be any I-shaped section, or a channel. The I-shaped section can be defined by selecting a W, WWF, S, SLB or HP shape from the built-in program steel section database, or by defining a user-specified I-shaped section. It is not necessary that the top and bottom flanges have the same dimensions in user-defined I-shaped sections used as composite beams. A channel section used as a composite beam can also be either user-defined or a section taken from one of the built-in program steel section databases.
Beam sections defined using Section Designer are considered as general sections, not I-shaped or channel-shaped sections (even if they really are I-shaped or channel-shaped), and cannot be designed using the Composite Beam Design postprocessor.

If the user defines a beam section by selecting it from the built-in section database, the program assumes that it is a rolled section and applies the design equations accordingly. If the user defines a section without selecting it from the built-in database, the program assumes it is a welded section and revises the design equations as necessary. The program does not check or design any of the welding for these welded beams.

### 2.5.2 Metal Deck and Slab Properties

Basic metal deck and concrete slab properties can be user defined. The geometry and the associated material properties of the metal deck, concrete slab, and shear connectors can be specified.

A beam designed using the Composite Beam Design postprocessor can have composite behavior only if it supports a deck section (not a slab or wall section).

The concrete slab over metal deck must be specified as a deck section property (not a slab section property) if the beam is to have composite behavior. If the slab is specified using a slab section property instead of a deck section property, the Composite Beam Design postprocessor designs the beams supporting that slab as non-composite beams.

A deck section can be specified as a Filled Deck (metal deck filled with concrete), an Unfilled Deck, or a Solid Slab (solid concrete slab with no metal deck). In the specified metal deck geometry includes the following:

- **Slab Depth**: The depth of concrete fill above the metal deck. This item is labeled $t_c$ in Figure 2-1.

- **Deck Depth**: The height of the metal deck ribs. This item is labeled $h_r$ in Figure 2-1.

- **Rib Width**: The average width of the metal deck ribs. This item is labeled $w_r$ in Figure 2-1.
• **Rib Spacing:** The center-to-center spacing of the metal deck ribs. This item is labeled $S_r$ in Figure 2-1.

If the deck has been specified as Filled Deck or Solid Slab (not Unfilled Deck), a slab material must be specified for the concrete. This should be a previously specified concrete material property. This concrete material property is used to specify all material properties of the concrete, except in some code-specific cases.

If the deck has been specified as Unfilled Deck, a steel material property must be specified for the deck material, and an equivalent shear thickness must be specified for the deck. These two items are used by the program to determine the membrane shear stiffness of the deck.

The weight-per-unit-area of the deck, $w_d$, can be specified. The self-weight of the deck object representing the concrete slab over metal deck is calculated using the weight-per-unit-area shown in the following equation.

$$\text{Weight-per-Unit-Area} = w_c \left( \frac{w_c h_c}{S_r} + t_c \right) + w_d$$

In the equation, $w_c$ is the weight-per-unit-volume of concrete. The first term is the weight-per-unit-area of the concrete and the second term is the weight-per-unit-area of the metal deck.

Note that the program does not check the design of the metal deck itself.

### 2.5.3 Shear Stud Anchor Properties

As described in the previous section, shear studs can be user defined along with the deck properties. The properties specified for shear studs are the diameter, $d_{sc}$, the height, $H_s$, and the specified tensile strength of the shear stud, $F_u$. In this program, shear connector patterns can be user specified.

The specification of composite deck stud anchors can include the following items:

- **Diameter:** The diameter of the shear stud.
- **Height:** The height of the shear stud. This item is labeled $H_s$ in Figure 2-1.
- **Tensile Strength, \( F_u \):** The specified tensile strength of the shear stud.

The program automatically calculates the strength of a single shear connector based on the shear stud and concrete slab properties. Revise this value using the composite beam overwrites, if desired.

### 2.5.4 Cover Plates

In this program, full-length cover plates can be specified on the bottom flange of a composite beam. Cover plates are not defined as part of the beam properties. They can be specified in the overwrites only. Thus, to specify a beam with a cover plate, the beam is designed as it typically would be without the cover plate, and then the user should add the cover plate in the overwrites.

One consequence of this process is that the cover plate is not included for overall analysis of the building. However, the cover plate is considered both for resisting moments and deflections for design of the composite beam within the program's Composite Beam Design postprocessor.

The properties specified for a cover plate are the width, \( b_{cp} \), the thickness, \( t_{cp} \), and a yield stress, \( F_{y_{cp}} \). The width and thickness dimensions are illustrated in Figure 2-1. The program does not check or design any of the welding between the cover plate and the beam bottom flange. It also does not determine cutoff locations for the full length cover plate.

### 2.6 Beams Designed as Composite Beams

The program puts the following restrictions on the frame objects that can be designed as composite beams.

(a) **Section Requirements**

Only I-shaped and channel-shaped beams can be designed as composite beams by the program. The I-shaped and channel-shaped beams can be selected from the built-in program section database, or they can be user defined.

Note that beam sections that are defined in Section Designer are always treated as general sections. Thus, if an I-type or channel-type section is defined using Section Designer, the program will consider it to be a general section, not an I-
shaped or channel-shaped section and will not allow it to be designed as a composite beam.

(b) Material Property Requirement

If a beam is to be designed as a composite beam, the Type of Design associated with the Material Property Data assigned to the beam must be Steel.

(c) Beam Orientation

The line type associated with the frame object that represents a composite beam must be "Beam." In other words, the frame object must lie in a horizontal plane, or within 20 degrees of horizontal.

For composite beams, the beam local 2-axis must be vertical. The Local axis 2 Angle is displayed on the Geometry tab of the Frame Information form.

(d) Support and Extent

The frame object representing a composite beam should span from support to support. Composite beams should not be modeled using multiple, adjacent frame objects between supports for a single composite beam.

In the case of a cantilever beam overhang, the frame object should span from the overhang support to the end of the beam. The cantilever beam back span should be modeled using a separate frame object. If cantilever beams are not modeled in this way, the analysis results for moments and shears will still be correct but the design performed by the Composite Beam Design processor probably will not be correct.

2.6.1 Frame Objects Designed by Default as Composite Beams

The program will design certain frame objects using the design procedures documented in this manual by default. Those frame objects must meet the following restrictions:

- The frame object must meet the section requirements described in the subsection entitled Section Requirements in this chapter.

- The frame object must meet the material property requirement described in the subsection entitled Material Property Requirement in this chapter.
The frame object must meet the two other requirements described in the subsection entitled Beam Orientation and Support and Extent in this chapter.

At least one side of the frame object must support a deck that is specified as a Deck section (not a Slab or Wall section). The deck section can be filled, unfilled or a solid slab. When the deck is unfilled, the beam will still go through the Composite Beam Design postprocessor and will simply be designed as a non-composite beam.

The frame object must not frame continuously into a column or a brace. Both ends of the frame object must be pinned for major axis bending (bending about the local 3-axis).

### 2.6.2 Overwriting the Frame Design Procedure for a Composite Beam

The three procedures possible for steel beam design are:

- Composite beam design
- Steel frame design
- No design

By default, steel sections are designed using either the composite beam design procedure or the steel frame design procedure. All steel sections that meet the requirements described in the previous subsection entitled Frame Objects Designed by Default as Composite Beams are by default designed using the composite beam design procedures. All other steel frame objects are by default designed using the steel frame design procedures.

Change the default design procedure used for a beam(s) by selecting the beam(s) and clicking the Design menu > Overwrite Frame Design Procedure command. This change is successful only if the design procedure assigned to a frame object is valid for that frame object. For example, if two steel beams, one an I-section and the other a tube section, are selected and an attempt is made to change the design procedure to Composite Beam Design, the change will be executed for the I-section, but not for the tube section because it is not a valid section for the composite beam design procedure. A section is valid for the
composite beam design procedure if it meets the requirements specified in the section entitled *Beams Designed as Composite Beams*, earlier in this chapter.

Note that the procedures documented for composite beam design allow for designing a beam as non-composite. One of the overwrites available for composite beam design is to specify that selected beams are designed as composite as required, non-composite with a minimum number of shear studs specified, non-composite with no shear studs, or always composite. These overwrites do not affect the design procedure. Changing the overwrite to one of the non-composite designs does not change the design procedure from Composite Beam Design to Steel Frame Design. The non-composite design in this case is still performed from within the Composite Beam Design postprocessor.

Using the composite beam design procedure, out-of-plane bending is not considered and slender sections are not designed. This is different from the Steel Frame Design postprocessor. Thus, the design results obtained for certain beams may be different, depending on the design procedure used.

Finally, note that the user can specify that the composite beam design procedures are to be used for a beam even if that beam does not support any deck, or for that matter, even if no slab is specified. In these cases, the beam will be designed as a non-composite beam by the Composite Beam Design postprocessor.

2.7 How the Program Optimizes Design Groups

This section describes the process the program uses to select the optimum section for a design group. In this description, note the distinction between the term *section*, which refers to a beam section in an auto select section list, and the term *beam*, which refers to a specific frame object in the design group.

When considering design groups, the program first discards any beam in the design group that is not assigned an auto select section list.

Next, the program looks at the auto select section list assigned to each beam in the design group and creates a new list that contains the sections that are common to all of the auto select section lists in the design group. The program
sorts this new common section list in ascending order, from smallest section to largest section based on section weight (area).

When designing with design groups, the program attempts to quickly eliminate inadequate beams.

The program then finds the beam with the largest positive design moment in the design group, or the “pseudo-critical beam.” The program then checks the design of the pseudo-critical beam for all sections in the common section list. Any sections in the common section list that are not adequate for the pseudo-critical beam are discarded from the common section list, making the list shorter. This new list is the shorter common section list. The shorter common section list is still in ascending order based on section weight (area).

Now the program checks all beams in the design group for the first section (smallest by weight [area]) in the shorter common section list. If the optimization is being performed on the basis of beam weight and the section is adequate for all beams in the design group, the optimum section has been identified. If the section is not adequate for a beam, the next higher section in the shorter common section list is tried until a section is found that is adequate for all beams in the design group.

If the optimization is based on price instead of weight, the program finds the first section in the shorter common section list (i.e., the one with the lowest weight) that is adequate for all beams. Next it calculates the cost of this first adequate section and then determines the theoretical heaviest section that could still have a cost equal to the adequate section by dividing the total price of the beam with the adequate section (steel plus camber plus shear connectors) by the unit price of the steel. This assumes that when the cost of the steel section alone is equal to or greater than the total cost of the adequate section, the section could not have a total cost less than the adequate section. The program then checks any other sections in the shorter common section list that have a weight less than or equal to the calculated maximum weight. If any of the other sections are also adequate, a cost is calculated for them. Finally, the section with the lowest associated cost is selected as the optimum section for the design group.

Regardless of whether the optimization is based on weight or cost, if all sections in the shorter common section list are tried and none of them are adequate for all of the beams in the design group, the program proceeds to
design each beam in the design group individually based on its own auto
section list and ignores the rest of the design group. If for a particular beam
none of the sections in the auto select section list are adequate, the program
displays results for the section in the auto select list with the smallest
controlling ratio shown in red. Note that the controlling ratio may be based on
stress or deflection.

By default, the program selects the optimum composite beam size based on
weight, not price. When a beam is optimized by weight, the program internally
optimizes the beam based on area of steel (excluding the cover plate, if it
exists). Thus, the weight density specified for the steel is irrelevant in such a
case.

By default, when auto select section lists are assigned to beams, the program
compares alternate acceptable composite beam designs based on the weight of
the steel beam (not including the cover plate, if it exists) to determine the
optimum section. The beam with the least weight is considered the optimum
section. The choice of optimum section does not consider the number of shear
connectors required or if beam camber is required.

In the composite beam design preferences, the user can request that the
program use price to determine the optimum section and assign prices to steel,
camber, and shear studs. If a price analysis is requested, the program compares
alternate acceptable beam designs based on their price and selects the one with
the least cost as the optimum section. By assigning different prices for steel,
shear connectors and camber, the user can influence the choice of optimum
section.

The costs for steel and cambering are specified on a unit weight of the beam
basis; for example, a cost per pound of the beam. The shear connector cost is
specified on a cost per connector. When a beam is optimized by price, the
program determines the price associated with the steel by multiplying the
volume of the beam (including the cover plate, if it exists) by the weight
density of the beam by the price per unit weight specified in the material
properties for the steel. The price associated with camber is determined by
multiplying the volume of the beam (including the cover plate, if it exists) by
the weight density of the beam by the specified price per unit weight for
camber defined in the composite beam preferences. The price for shear
connectors is determined by multiplying the total number of shear connectors
by the price per connector specified in the composite beam preferences. The total price for the beam is the sum of the prices for the steel, camber and shear connectors. Thus, when a beam is optimized by price, the weight density for the steel is important and must be correctly specified for the price to be correctly calculated.

The volume of the beam is calculated by multiplying the area of the steel beam (plus the area of the cover plate, if used) by the length of the beam from center-of-support to center-of-support.

2.8 Analysis Sections and Design Sections

It is important to understand the difference between analysis sections and design sections. Analysis sections are those section properties used to analyze the model when an analysis is run. The design section is whatever section has most currently been designed and thus designated the current design section.

It is possible for the last used analysis section and the current design section to be different. For example, an analysis may have been run using a W460X52 beam, and then it is determined in the design that a W410X46 beam worked better. In that case, the last used analysis section is the W460X52 and the current design section is the W410X46. Before the design process is complete, verify that the last used analysis section and the current design section are the same.

The program keeps track of the analysis section and the design section separately. Note the following about analysis and design sections:

- Assigning a beam a frame section property assigns the section as both the analysis section and the design section.

- Running an analysis always sets the analysis section to be the same as the current design section.

- Assigning an auto select list to a frame section initially sets the design section to be the beam with the median weight in the auto select list.

- Unlocking a model deletes the design results, but it does not delete or change the design section.
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- Changing a design load combination deletes the design results, but it does not delete or change the design section.

- Changing any of the composite beam design preferences deletes the design results, but it does not delete or change the design section.

- Deleting the static nonlinear analysis results also deletes the design results for any load combination that includes static nonlinear forces. Typically, static nonlinear analysis and design results are deleted when one of the following actions is taken:
  - Redefine existing or define new hinges.
  - Redefine existing or define new static nonlinear load cases.
  - Add or delete hinges.

Again, note that these actions delete only results for load combinations that include static nonlinear forces.

2.9 Output Stations

Frame output stations are designated locations along a frame object. They are used as locations to report output forces and to perform design, and they are used as plotting points for graphic display of force diagrams. When force diagrams are plotted, exact forces are plotted at each output station, and then those points are connected by straight lines. Output stations occur at user-specified locations and at point load locations along a beam. Designate the output stations for a frame object using the Assign menu.

For composite beam design, the program checks the moments, shears and deflections at each output station along the beam. No checks are made at any points along the beam that are not output stations.

2.10 Effective Width of the Concrete Slab

This section explains how the program considers the effective width of the concrete slab separately on each side of the composite beam. This separation is carried through in all of the calculations. It allows different deck properties on the two sides of the beam.
The effective slab width on either side of the beam can be specified in the overwrites. The effective widths are specified on the left and right sides of the beam. As illustrated in Figure 2-2, when viewed from the I-end of the beam toward the J-end of the beam, the program assumes the right side of the beam to be on the right-hand side.

![Diagram of beam with labeled sides](figure)

**Figure 2-2 Example of How the Program Defines the Left and Right Sides of the Beam**

### 2.10.1 Location Where Effective Slab Width is Checked

By default, the program checks the effective width of the beam over the entire middle 70% of the beam and uses the smallest value found as the effective width of the beam, $b_{\text{eff}}$, everywhere in the calculations for that beam. The 70% number is derived based on two assumptions:

- The capacity of the composite beam is approximately twice that of the steel beam alone.
- The steel beam alone is capable of resisting the entire moment in the composite beam for the last 15% of the beam length at each end of the beam. Note that for a uniformly loaded beam, the moment drops off to half of the maximum moment or less in the last 15% of the beam.
Redefine this default “middle range” of 70% in the composite beam design preferences, if desired (Appendix A).

2.10.2 Maximum Effective Width

In accordance with CSA 17.4.1, if there is a slab on both sides of a beam, its effective width is the smallest of:

a) 0.25 times the beam span; or

b) the average distance from the center of the steel section, truss or joist to the centers of adjacent parallel supports – how the program handles diagonal beams is explained further down.

In accordance with CSA 17.4.2, if there is a slab on one side only of a beam, its effective width is the smallest of:

a) 0.1 times the beam span; or

b) 0.5 times the clear distance between the steel section, truss or joist to the centers of adjacent parallel support.

In determining if there is a slab on both sides or on only one side of the beam, the program takes into account the actual width of the steel section and looks for a slab beyond a zone equal to the width of the section on each side.

2.10.3 Multiple Deck Types or Directions Along the Beam Length

For design calculations, the program assumes one deck type and deck direction on each side of the beam along the entire length of the beam, regardless of the actual number of types and directions of deck that may exist. The program allows different deck types and deck directions on the two sides of the beam in the calculations. Figure 2-3 shows examples of different deck types and different deck directions on the two sides of the beam.
The program checks the deck types and deck directions on each side of the composite beam within the specified middle range (see the previous subsection). When multiple deck types or deck directions occur on the same side of a composite beam, the program decides which single deck section and direction to use on that side of the beam.

The program goes through these steps in this order to choose the deck section.

1. The program calculates the product of $t_c \times f'_{c}$ for each deck where $t_c$ is the depth of the concrete above the metal deck and $f'_{c}$ is the concrete slab compressive strength. It uses the deck section that has the smallest value of $t_c \times f'_{c}$ in the calculations for the beam.

2. If two or more deck sections have the same value of $t_c \times f'_{c}$ but the deck spans in different directions, the program uses the deck section that spans perpendicular to the beam.

3. If two or more deck sections span in the same direction and have the same value of $t_c \times f'_{c}$, the program uses the deck section with the smaller $t_c$ value.

4. If two or more deck sections span in the same direction and have the same values of $t_c$ and $f'_{c}$, the program uses the first defined deck section.
In this program's composite beam design, the deck is assumed either parallel or perpendicular to the span of the beam. If the deck span is exactly parallel to the beam span or within 15 degrees of parallel to the beam span, the deck span is assumed to be parallel to the beam span. Otherwise, the deck span is assumed to be perpendicular to the beam span.

The assumed deck type and deck direction on each side of the beam can be specified using the composite beam overwrites.

Refer to the floor plan shown in Figure 2-4. The typical floor in this plan consists of 65 mm normal weight concrete over 75 mm metal deck that is designated Deck Type A. However, the upper left-hand quadrant of the floor consists of 90 mm normal weight concrete over 75 mm metal deck that is designated Deck Type B. Assume that the concrete compressive strength is 30 MPa for both deck types.
Now consider the beam labeled “Girder F” in the figure. Deck Type A exists along the entire length of the right-hand side of this beam. Thus, the program uses Deck Type A on the right side of the beam in the calculations. Both Deck Type A and Deck Type B exist along the left-hand side of the beam. The program uses the following method to determine which of these deck types to use on the left side of the beam in the calculations:

1. Determine the product of $t_c f_{c'}$ for each deck type.
   a. For Deck Type A: $t_c f_{c'} = 65 \times 30 = 1,950$ N/mm.
   b. For Deck Type B: $t_c f_{c'} = 90 \times 30 = 2,700$ N/mm.

2. Use Deck Type A on the left side of the girder in the composite beam calculations because it has the smaller value of $t_c f_{c'}$.

Note that the loads applied to the beam are still based on the actual deck types. Thus, the load applied to the upper half of Girder F in Figure 2-4 would include the contribution from Deck Type B even though Deck Type B might not be used in calculating the composite beam properties.

A second example is shown in Figure 2-5. In this example, the deck type is the same throughout the floor, but the direction of the deck changes in the upper left-hand quadrant of the floor.
Now consider the beam labeled “Girder G” in the figure. The deck ribs are oriented parallel to the span of Girder G along the entire length of the right-hand side of this beam. Thus, the program uses Deck Type A oriented parallel to the span of Girder G on the right side of the beam in the calculations.

Deck ribs oriented both perpendicular and parallel to the span of Girder G exist along the left-hand side of the beam. Because only the deck direction is different along the left side of the beam, not the deck type (and thus $t_c$ and $f'_{c}$ do not change), the program uses the deck that spans perpendicular to Girder G on the left side of the beam.
2.10.4 Effect of Diagonal Beams on Effective Slab Width

Consider the example shown in Plan A of Figure 2-6. In Plan A, the length of Beam A is \(L_A\). Assume that the effective width of this beam is controlled by the distance to the centerline of the adjacent beam. Also assume that the program checks the effective width of the slab over the default middle range (70%) of Beam A. If the variable labeled \(x_a\) in the figure is less than or equal to 0.15, the effective width of the concrete slab on the upper side of Beam A (i.e., the side between Beam A and Beam X) is controlled by the distance between Beam A and Beam X. On the other hand, if \(x_a\) is greater than 0.15, the effective width of the concrete slab on the upper side of Beam A is controlled by the distance between Beam A and Girder Y, at a location of 0.15\(L_A\) from the left end of Beam A. This distance is measured along a line that is perpendicular to Beam A.

\[\text{Plan A} \quad \text{Plan B} \]

\[\text{Plan C} \]

*Figure 2-6 Examples of the Effect of Diagonal Beams on Composite Beam Effective Width*
Now consider the example shown in Plan B of Figure 2-6. Assume that the effective width of Beam B is controlled by the distance to the centerline of the adjacent beam. When considering the perpendicular distance from Beam B to the adjacent beam on the upper side of Beam B, the program considers the diagonal beam labeled Beam Z when the angle $\theta$ is less than 45 degrees. If the angle $\theta$ is greater than or equal to 45 degrees, Beam Z is ignored when calculating the effective slab width on the upper side of Beam B.

Plan C in Figure 2-6 shows a special case where two diagonal beams frame into Beam C at the same point. In this special case, the program assumes that the effective width of the slab on the side of the beam where the two diagonals exist is zero. The user can, of course, change this in the overwrites. The program assumes the zero effective width because, although it is checking the effective width for Beam C, it is unable to determine whether a slab is actually between the two diagonal beams.

### 2.10.5 Effect of Openings on Effective Slab Width

Now consider Plan D shown in Figure 2-7. In this case, there is an opening on both sides of the slab at the left end of Beam D.
Assume again that the effective width of this beam is controlled by the distance to the centerline of the adjacent beam, and also assume that the program checks the effective width of the slab over the default center 70% of the Beam D length. If the width of the opening, \( x_D \cdot L_D \) is less than 0.15\( L_D \), the program bases the effective width of the concrete slab on the distance to the adjacent beams. On the other hand, if \( x_D \cdot L_D \) exceeds 0.15\( L_D \), the program assumes the effective concrete slab width for Beam D to be zero; that is, it assumes a non-composite beam.

### 2.10.6 Effective Slab Width and Transformed Section Properties

When the program calculates the transformed section properties, the concrete is transformed to steel by multiplying \( b_{\text{eff}} \) by the ratio \( E_c / E_s \). This ratio may be different on the two sides of the beam. See the section entitled *Transformed Section Moment of Inertia* for more information.

### 2.11 Beam Unbraced Lengths

The program considers the unbraced length for construction loading separately from that for final loads. For both types of loading, the unbraced length of the beam associated with buckling about the local 2-axis (minor) of the beam is used to determine the flexural capacity of the non-composite beam. The local 2-axis is illustrated in Figure 2-8.

By default, the program automatically determines the locations where the beam is braced for buckling about the local 2-axis. This information is then used to determine the unbraced length associated with any point on the beam. Instead of using the program calculated bracing points, the user can specify in the overwrites brace points for any beam.

For buckling about the local 2-axis, the program differentiates between bracing of the top flange of the beam and bracing of the bottom flange of the beam. The program automatically recognizes which flange of the beam is the compression flange at any point along the beam for any design load combination. With this ability and the program-determined or user-specified bracing point locations, the program can automatically determine the unbraced length of any segment.
along the beam and can apply appropriate code-specified modification factors (e.g., $C_b$ factor for flexure) to the flexural strength of the beam.

![Diagram of a Beam with Axes](image)

**Figure 2-8 Local 2Axis of a Beam**

### 2.11.1 Determination of the Braced Points of a Beam

The program considers the lateral bracing for the top and bottom flanges separately. In the Composite Beam Design postprocessor, the program assumes that beams can be braced by the deck section (or slab section) that they support and by other beams framing into the beam being considered. The program automatically determines the braced points of a beam for buckling about the local 2-axis as follows:

The top flange is assumed to be continuously laterally supported (unbraced length of zero) anywhere there is metal deck section with concrete fill framing into one or both sides of the beam or there is a slab section framing into both sides of the beam.

Metal deck sections with *no* concrete fill are assumed to continuously brace the top flange if the deck ribs are specified as oriented perpendicular to the beam.
span. If the deck ribs are specified as oriented parallel to the beam span, the deck is assumed to not brace the top flange.

The top and bottom flange are assumed to be braced at any point where another beam frames into the beam being considered at an angle greater than 30 degrees, as shown in the sketch to the right. It is up to the user to provide appropriate detailing at this point to ensure that the bottom flange is adequately braced. If appropriate detailing is not provided, the user should redefine the brace points using one of the methods described in the next section.

When the bracing is program calculated or brace points are user specified, the program always assumes that each end of the beam is braced at both the top and the bottom flange. If the unbraced length of a beam is longer than the actual beam, specify a user-defined unbraced length, not user-defined brace points.

2.11.2 User Defined Unbraced Length of a Beam

2.11.2.1 Overview

To use unbraced lengths other than those determined by the program, change the assumed unbraced length for any beam in the composite beam overwrites. This is true for both the construction loading unbraced lengths and the final loading unbraced lengths.

For buckling about the local 2-axis, specific bracing points can be specified along the beam that apply to the top flange, bottom flange, or both, or one maximum unbraced length can be specified that applies over the entire length of the beam to both the top and bottom flanges.

As soon as the user specifies any user defined bracing points or unbraced lengths for a beam, all of the program determined lateral bracing information on that beam is ignored. Thus, if any bracing point is specified for a beam, all of the bracing points for that beam should be specified.
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2.11.2.2 User Specified Uniform and Point Bracing

If the user specifies bracing along the beam for buckling about the local 2-axis, the user can specify continuous bracing along a beam flange, bracing at specific points along a beam flange, or both.

2.11.2.2.1 Point Braces

To define point braces, specify a distance along the beam that locates the brace point, and then indicate whether the top, bottom, or both flanges are braced at this location. Specify the distance as an actual distance or as a relative distance, both measured from the I-end of the beam. All distances are measured from the center of the support, not the physical end of the beam. The distances may be specified as either absolute (actual) distances or as relative distances. A relative distance to a point is the absolute distance to that point divided by the length of the beam measured from the center-of-support to center-of-support.

The user can change the default bracing assumed for a beam in the composite beam overwrites. The bracing specified can be different for construction loading and final loading.

2.11.2.2.2 Uniform Braces

To define uniform or continuous bracing, specify a distance along the beam that locates the starting point of the continuous bracing, specify a second (longer) distance along the beam that locates the ending point of the continuous bracing, and then indicate whether the top, bottom, or both flanges are continuously braced over this length. The distances can be specified as absolute (actual) distances or as relative distances, both measured from the I-end of the beam. A relative distance to a point is the absolute distance to that point divided by the length of the beam measured from the center-of-support to center-of-support.

2.12 Design Check Locations

One of the first tasks the program performs when designing or checking a composite beam is to determine the design check locations for the design load combinations used for checking the strength of the beam to carry the final design loads. There may be many design check locations along a beam. The design check locations are determined as follows:
The point of maximum positive moment for each design load combination used for checking the strength of the beam to carry the final design loads is a design check location. Note that there may be more than one of these design load combinations and thus there may be more than one point of maximum moment to consider.

The point of maximum negative moment (if negative moment exists) for each design load combination used for checking the strength of the beam to carry the final design loads is a design check location.

A point load or point moment location for any design load combination used for checking the strength of the beam to carry the final design loads is a design check location.

The ends of a cover plate, if one is specified, are design check locations.

The end or edge of the deck. This occurs, for example, at locations where the beam spans through an opening in the deck.

At each design check location the program checks the moment capacity of the composite beam and determines the number of shear connectors required between that location and the nearest point of zero moment (or in some special cases, the end of the slab).

The program determines one set of design check locations that applies to all design load combinations.

Consider, for example, a composite beam with two design load combinations used for checking the strength of the beam to carry the final design loads. Assume one of those load combinations is a uniform load over the full length of the beam and the other is a point load at the third point of the beam. Also assume there is positive moment only in the beam and no cover plate. In this example, the program considers the following design check locations:

- The point of maximum positive moment for the design load combination with uniform load only.
- The point of maximum positive moment for the design load combination with point loads at the third point.
- The location of the point load, that is, the third point of the beam.
The program checks the moment capacity and the number of shear connectors required between each of these four locations and the nearest point of zero moment for both of the design load combinations. Thus, for the design load combination with uniform load only, the program still checks how many shear studs are required between the location of the point load in the other design load combination and the nearest point of zero moment. This ensures that there is always a sufficient number of shear connectors in the appropriate location on the beam.

2.13 Design Load Combinations

2.13.1 Default vs. User-Specified Load Combinations

Several design load combinations are used for determining the various combinations of the load cases for which the beams need to be designed/checked. For normal loading conditions involving static dead load, construction load, live load and snow load, the program has built-in default loading combinations based on the NBCC code. These default composite beam design load combinations can be used for design, or the user may instead define design load combinations, or both default combinations and user defined combinations can be used. As many load combinations as needed can be specified. Also, the default design load combinations can be modified or deleted as needed. The default load combinations are used if the user requests them to be included or if no other user defined combination is available for composite beam design. The default combinations are automatically updated to conform to the appropriate code by the program any time the design code is changed.

Three separate types of default load combinations are considered. They are:

- Strength Check for Construction Loads: Design load combinations for checking the strength of the beam to carry construction loads. Note that these design load combinations are considered only if the beam is specified to be unshored. Beams can be specified as shored or unshored in the composite beam design preferences.

- Strength Check for Final Loads: Design load combinations for checking the strength of the beam to carry the final design loads.
Deflection Check for Final Loads: Design load combinations for checking the deflection of the beam under final design loads.

The program creates separate default design load combinations for each of these three conditions based on the specified dead, superimposed dead, live and reducible live load cases. In addition, the program creates special live load patterns for cantilever beams – see below.

The load combination factors are applied to the forces and moments obtained from the associated load cases and are then summed to obtain the factored design forces and moments for the load combination.

For reducible loads, a live load reduction factor is computed for each beam per the live load reduction method chosen in the Live Load Reduction Factor form. It is then applied on a beam-by-beam basis to the member forces of the live load case to reduce the contribution of the live load to the factored loading. The user can explicitly specify a live load reduction factor for any beam in the Composite Beam Design Overrides form.

None of the program default load combinations include the effect of roof loads, snow loads or lateral loads. If roof loads, snow loads or lateral loads need to be considered, the user should specify user-defined design load combinations. For other loading conditions involving moving load, time history, pattern live loads, the user must define design loading combinations either in lieu of or in addition to the default design loading combinations. The user is cautioned that if moving load or time history results are not requested to be recovered in the analysis for some or all of the frame objects, the effects of those loads will be assumed to be zero in any combination that includes them.

For multi-valued load combinations involving response spectrum, time history, moving loads and multi-valued combinations (of type enveloping, square-root of the sum of the squares or absolute) where any correspondence between interacting quantities is lost, the program automatically produces multiple sub combinations using maxima/minima permutations of interacting quantities. Separate combinations with negative factors for response spectrum cases are not required because the program automatically takes the minima to be the negative of the maxima for response spectrum cases and the previously described permutations generate the required sub combinations.
When a design combination involves only a single multi-valued case of time history, further options are available. The program has an option to request that time history combinations produce sub combinations for each time step of the time history.

2.13.2 Default Strength Checks for Construction Loads

The program performs the check using the construction load design load combination only if the beam is unshored. If the beam is shored, the check for construction loads is not performed and any specified design load combinations for construction loads are not relevant.

The automatically created design load combinations for checking the strength of an unshored beam subjected to construction loads are given by the two following equations:

1.4 (\(\sum WDL\))

1.25 (\(\sum WDL\)) + 1.5 (\(\sum CL\))

where:

\(\sum WDL\) = The sum of all wet dead load (WDL) load cases defined for the model. Note that if a load case is simply defined as dead load, it is assumed to be a WDL load case.

\(\sum CL\) = The sum of all construction load (CL) load cases defined for the model. Note that you need to explicitly define these.

2.13.3 Default Strength Checks for Final Loads

The automatically created design load combinations for checking the strength of a composite beam under final loads are given by the following equations.

1.4 (\(\sum WDL + \sum SDL\))

1.25 (\(\sum WDL + \sum SDL\)) + 1.5 (\(\sum LL + \sum RLL\))

where:
\[ \Sigma \text{SDL} = \text{The sum of all superimposed dead load (SDL) load cases defined for the model.} \]
\[ \Sigma \text{LL} = \text{The sum of all live load (LL) load cases defined for the model.} \]
\[ \Sigma \text{RLL} = \text{The sum of all reducible live load (RLL) load cases defined for the model.} \]

and the remainder of the terms are as defined above.

2.13.4 Default Deflection Check for Final Loads

The automatically created design load combination for checking the deflection of a composite beam under final loads is given by the following equation,

\[ \Sigma \text{WDL} + \Sigma \text{SDL} + \Sigma \text{LL} + \Sigma \text{RLL} \]

where all of the terms are as described previously. Note that all of the load factors for this serviceability check are 1.0.

If the beam is unshored, the WDL portion of the deflection is based on the moment of inertia of the steel beam alone and the remainder of the deflection is based on the effective moment of inertia of the composite section. If the beam is shored, the entire deflection is based on the effective moment of inertia of the composite section.

2.13.5 Special Live Load Patterning for Cantilever Back Spans

For strength design of cantilever back spans, the program performs special live load patterning. The live load patterning used for cantilever back spans is slightly different from what you might expect, so you should read this section carefully to understand what the program does.

Each composite beam design load combination for a cantilever has a dead load (DL), superimposed dead load (SDL) and a live load plus reduced live load (LL + RLL) component. There may also be other types of load components as well. The nature of the other types of load components is not important. The DL, SDL, (LL + RLL) and other components are shown in Figure 2-9a.
The program internally creates a *simply supported* model of the cantilever back span. It applies a load to this simply supported span that is equal to a factor times the LL + RLL applied to the span. The factor used is specified in the composite beam design preferences as the Pattern Live Load Factor. This internally created model and loading is illustrated in Figure 2-9b. In the figure, PLLF is short for Pattern Live Load Factor.

Finally for strength design (final loads only) of cantilever back spans, the program considers the following two conditions for each design load combination:

- DL + SDL + LL + RLL (± any other type of load if it exists) as specified over the full length (back span plus overhang) of the cantilever beam.

- DL + SDL (± any other type of load if it exists) over the full length (back span plus overhang) of the cantilever beam plus the (LL + RLL) multiplied by the Pattern Live Load Factor applied to the simply supported back span.

These two conditions are shown in Figure 2-9c.
Note that the conditions described herein are considered for strength design for final loads only. The program does not do any special pattern loading checks for deflection design or for construction loading design.

If load patterning different from that provided by the program is needed, the user should create a design load combination. When creating user defined live load patterning, it typically works best to give the specially defined pattern live load cases an “Other” design type instead of a “Live Load” design type. That way, the special pattern live load cases are not included in the automatically created default design load combinations, avoiding possible double counting of some live loads in those load combinations.

### 2.13.6 Special Live Load Patterning for Continuous Spans

For strength design of spans that are continuous at one or both ends, the program performs special live load patterning similar to that described in the previous section for back spans of cantilevers. The live load patterning used for continuous spans is slightly different from what you might expect, so you should read this section carefully to understand what the program does.

Each composite beam design load combination for a continuous span has a DL, SDL and (LL + RLL) component. There also may be other types of load components as well. The nature of the other types of load components is not important. The DL, SDL, (LL + RLL) and other components are shown in Figure 2-10a.

The program internally creates a *simply supported* model of the continuous span. It applies a load to this simply supported span that is equal to a factor times the LL + RLL applied to the span. The factor used is specified on the Beam tab in the composite beam design preferences as the Pattern Live Load Factor. This internally created model and loading is illustrated in Figure 2-10b. In the figure, PLLF is short for Pattern Live Load Factor.

Finally for strength design (final loads only) of continuous spans, the program considers the following two conditions for each design load combination:
- DL + SDL + LL + RLL (+ any other type of load if it exists) as specified with actual continuity.

- DL + SDL (+ any other type of load if it exists) as specified with actual continuity plus the (LL + RLL) multiplied by the Pattern Live Load Factor applied to the simply supported beam.

These two conditions are shown in Figure 2-10c.

**Note:** The conditions described herein are considered for strength design for final loads only. The program does not do any special pattern loading checks for deflection design or for construction loading design.

**Figure 2-10 Conditions Considered for Strength Design of a Continuous Span**

Note that the conditions described herein are considered for strength design for final loads only. The program does not do any special pattern loading checks for deflection design or for construction loading design.
If load patterning different from that provided by the program is needed, the user should create a design load combination. When creating user-defined live load patterning, it typically works best to give the specially defined pattern live load cases an “Other” design type instead of a “Live Load” design type. That way, the special pattern live load cases are not included in the automatically created default design load combinations, avoiding possible double counting of some live loads in those load combinations.

2.14 Beam Deflection and Camber

This section describes how the program calculates beam deflections and how it considers beam camber.

2.14.1 Deflection

In composite beam design, when a beam is shored, the deflection is calculated using the effective moment of inertia, $I_{\text{eff}}$, if there is composite action, or the moment of inertia of the steel beam alone, $I_{\text{bare}}$, if the beam is designed as non-composite or found to be a cantilever overhang. How $I_{\text{eff}}$ is computed is described in section Effective Moment of Inertia later in this Chapter.

If a composite beam is unshored, the dead load deflection is always based on the moment of inertia of the steel section alone (plus cover plate, if it exists), $I_{\text{bare}}$. The deflection for all other loads is calculated using (a) the transformed moment of inertia, $I_{\text{tr}}$, if there is full (100%) composite connection, (b) the effective moment of inertia, $I_{\text{eff}}$, if there is partial composite connection, or (c) the moment of inertia of the steel beam alone, $I_{\text{bare}}$, if the beam is designed as non-composite or found to be a cantilever overhang.

When deflection is used as a criterion for selecting the optimum beam size, the program checks that the total load deflection minus the camber does not exceed the specified total load deflection limit. It also checks that the live load deflection does not exceed the specified live load deflection limit.

The program calculates composite beam deflections using a moment-area technique. An $M/EI$ diagram is constructed by calculating $M/EI$ values at each output station along the length of the beam and then connecting the $M/EI$ values at those stations with straight-line segments. The program assumes that
the moment of inertia does not vary along the length of the beam (frame object).

Deflections for the beam are calculated at each output station. The overall deflected shape of the beam is drawn by connecting the computed values of deflection at each output station with straight-line segments. Thus, the program assumes a linear variation of $M/EI$ between output stations.

In this program's composite beam design, the reported deflection is the vertical displacement relative to a line drawn between the deflected positions of the ends of the beam. For example, refer to the beam shown in Figure 2-11. Figure 2-11a shows the original undeformed beam and also shows an arbitrary point along the beam labeled A. Figure 2-11b shows the beam in its deformed position and illustrates the deflection that the Composite Beam Design postprocessor reports for the beam at point A.

![Figure 2-11 Deflection Results Reported by the Composite Beam Design Postprocessor](image)

**2.14.2 Deflection Reported for Cantilever Overhangs**

For cantilever overhangs, the program's Composite Beam Design postprocessor reports the displacement of the beam relative to the deformed position of the supported end. *This displacement is calculated by the design postprocessor assuming that the supported end of the cantilever overhang is fixed against rotation.*

When reviewing the displacement at the end of the cantilever, the displacement is reported relative to the *undeformed* position of the end of the cantilever. In that case, the rotation at the supported end of the cantilever overhang is correctly taken into account. However, the displacements displayed are all based on the analysis section properties (non-composite moment of inertias).
2.14.3 Deflection caused by Concrete Shrinkage

The program computes the deflection caused by concrete creep and adds it to the deflection total.

\[
\Delta_s = \frac{L^2}{8} c \cdot \frac{e_s \cdot A_e \cdot y}{E} \cdot \frac{E_c}{E_c / (1 + \chi \phi)} \cdot I_{es}
\]  

(CSA13.6 b)

where:

- \(\Delta_s\) = the deflection caused by concrete creep
- \(L\) = span of the beam
- \(c\) = empirical coefficient taken as 0.5
- \(e_s\) = free shrinkage strain of concrete taken as \(583 \times 10^{-6}\) (CSA Appendix H)
- \(A_e\) = effective area of concrete slab
- \(y\) = distance from centroid of effective area of concrete slab to centroidal axis of the composite beam
- \(E\) = modulus of elasticity of steel
- \(E_c\) = modulus of elasticity of concrete
- \(\chi\) = aging coefficient of concrete, taken as 0.73 (CSA Appendix H)
- \(\phi\) = creep coefficient of concrete, taken as 2.7 (CSA Appendix H)
- \(I_{es}\) = effective moment of inertia of the composite beam

The values of \(e_s\), \(\chi\), and \(\phi\) can optionally be changed in the composite beam preferences and overwrites.

2.14.4 Camber

When the beam is not shored during construction and beam camber is calculated, the amount of camber is based on a percentage of the dead load (not
including superimposed dead load) deflection. By default, this percentage is 80%, but this value can be modified in the composite beam design preferences. If the beam is shored during construction, the amount of camber calculated by ETABS is zero, reflecting the fact that the beam does not deflect when concrete is poured on the deck on top of it.

By default, the minimum camber the program specifies (other than zero) is the largest of 15 mm or L/900 where L is the span of the beam, and the maximum camber it specified percentage of dead load deflection.

### Table 2-1 How the Program Specifies Camber

<table>
<thead>
<tr>
<th>CP * ∆DL (mm)</th>
<th>Camber Specified by the Program (mm)</th>
<th>CP * ∆DL (mm)</th>
<th>Camber Specified by the Program (mm)</th>
</tr>
</thead>
<tbody>
<tr>
<td>≥</td>
<td>&lt;</td>
<td>≥</td>
<td>&lt;</td>
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<tr>
<td>N.A.</td>
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<td>53</td>
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<td>43</td>
<td>48</td>
<td>88</td>
<td>N.A.</td>
</tr>
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<td>48</td>
<td>53</td>
<td>93</td>
<td>98</td>
</tr>
<tr>
<td></td>
<td></td>
<td>98</td>
<td>100</td>
</tr>
</tbody>
</table>

is the smallest of 150 mm and L/180. Camber is specified in 5 mm increments and it is rounded down. These numbers can be changed in the preferences, as well as the direction of the rounding (up or down).

There is also a minimum beam depth for camber of 340 mm, a minimum web thickness of 6 mm, and a minimum span of 7m. Again these numbers can be changed.

Review the beam cambers calculated by the program together with beam camber information related to the design code and any other information provided by the steel fabricator to make any necessary adjustments.

### 2.15 Floor Vibration

For CSA S16-09, by default the program performs the floor vibration check in accordance with AISC Steel Design Guide 11 (DG11). The program calculates
the first natural vibration frequency, estimated peak acceleration (in units of \( g \)), \( a_p/g \), and acceleration limit, \( a_o/g \), for each beam and reports this information to determine the adequacy of a composite beam section.

The acceleration limit of any floor system can be achieved by limiting the vibration characteristics of beams or girders. The program optimize the floor vibration only by limiting the estimated peak acceleration of each individual beam.

2.15.1 Excitation Types

The program supports the following excitation types:

(a) Walking Excitation
The recommended walking excitation criterion, methods for estimating the required floor properties and design procedure, was first proposed by Allen and Murray (1993). In DG11, the criterion is based on the dynamic response of steel beam floor systems to walking forces. The criterion can be used to evaluate structural systems supporting offices, shopping malls, footbridges and similar occupancies.

(b) Rhythmic Excitation
The rhythmic excitation criteria is based on the dynamic response of the structural system to rhythmic exercise forces distributed over all or part of the floor. This criterion is used to evaluate structural systems supporting aerobics, dancing, audience participation and similar events, assuming that loading function is known.

(c) Walking near Sensitive Equipment
For sensitive equipment, a criterion is based on the vibrational velocities given in Table 6.1 of DG11. The following expression can be used to convert given velocity, \( V \), to the corresponding acceleration, \( a \).

\[
a / g = 2\pi f V / g \tag{DG11 Eqn. 6.1}
\]

2.15.2 Design for Walking Excitation

2.15.2.1 Effective Panel Weight
The effective panel weights for the beam and girder panel modes are estimated from the following equation:
\[ W = wBL \]  
(DG11 Eqn. 4.2)

where,

- \( w \) = Supported weight per unit area
- \( B \) = Effective width
- \( L \) = Beam or girder span

\[ B_j = C_j \left( \frac{D_s}{D_j} \right)^{1/4} L_j \leq 2/3 \times \text{Floor Width} \]  
(DG11 Eqn. 4.3a)

For the beam panel mode, the effective width is

\[ B_j = C_j \left( \frac{D_s}{D_j} \right)^{1/4} L_j \leq 2/3 \times \text{Floor Width} \]  
(DG11 Eqn. 4.3a)

where,

- \( C_j \) = 2.0 for beams in most areas
- = 1.0 for beams parallel to an interior edge
- \( D_s = \frac{d_e^3}{12n} \) = Transformed slab moment of inertia per unit width
- \( d_e \) = Effective depth of concrete slab, taken as the depth of concrete above the form deck plus one-half the depth of the form deck
- \( n \) = \( E_s / E_c \) = Modular ratio
- \( E_s \) = Modulus of elasticity of steel
- \( E_c \) = Modulus of elasticity of concrete
- \( D_j = I_t / S \) = Transformed beam moment of inertia per unit width
- \( I_t \) = Effective moment of inertia of T-beam
- \( S \) = Beam spacing
- \( L_j \) = Beam span

For vibration calculations, the program calculates the moment of inertia assuming full (100%) composite connection, regardless of the actual percent composite connection.

For the girder panel mode, the effective width is

\[ B_g = C_g \left( \frac{D_s}{D_g} \right)^{1/4} L_g \leq 2/3 \times \text{Floor Width} \]  
(DG11 Eqn. 4.3b)

where,
\[ C_s = \begin{cases} 1.6 & \text{for girders supporting beam connected to the girder flange} \\ 1.8 & \text{for girders supporting beam connected to the girder web} \end{cases} \]

\[ D_g = \text{Girder transformed moment of inertia per unit width} \]

\[ D_g = \begin{cases} I_g/L_j & \text{for all except edge girders} \\ I_g/2L_j & \text{for edge girders} \end{cases} \]

\[ L_g = \text{Girder span} \]

Where beams or girders are continuous over their supports and an adjacent span is greater than 0.7 times the span under consideration, the effective panel weight, \( W_j \) or \( W_g \), can be increased by 50 percent.

For the combined mode, the equivalent panel weight is computed as follows:

\[ W = \frac{\Delta_j}{\Delta_j + \Delta_g} W_j + \frac{\Delta_g}{\Delta_j + \Delta_g} W_g \]  

(DG11 Eqn. 4.4)

The weight, \( W \), used in the frequency calculations is determined by the program as the sum of all dead loads, plus the sum of all superimposed dead loads, plus sum of additional dead load and sum of live loads on the beam specified in design overwrites, regardless of whether those loads are included in a design load combination. The program determines the type of load (dead, sdead, etc.) based on the type of load specified in the load pattern definition.

Thus, for the program to correctly calculate the weight supported by the beam, and thus correctly calculate the frequency, the user must be sure to tag all of the load types correctly when defining the static load patterns. Be careful not to define the same load twice (i.e., in two different load patterns) as a Dead, Superimposed dead. If it is necessary to define the same load twice, the user may want to tag the load as an Other-type load in the second case. Doing this keeps the program from double counting the load when calculating the weight, \( W \).

### 2.15.2.2 Vibration Frequency

The program calculates the first natural vibration frequency of a beam using the Dunkerley relationship.
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2.15.2.3 Damping

The damping associated with floor systems depends primarily on non-structural components, finishing, furnishings and occupants. DG11 Table 4.1 provides the recommended values for modal damping ratio, $\beta$. Recommended modal damping ratios ranges between 0.01 to 0.05.

2.15.2.4 Computation of Peak Acceleration

The program calculates the peak acceleration, $a_p$, from the following expression for walking excitation criteria:

$$a_p = \frac{P_o e^{(-0.35 f_n)}}{\beta W}$$  \hspace{1cm} (DG11 Eqn. 4.1)

where,

- $P_o$ = A constant force representing the excitation
- $f_n$ = fundamental natural frequency of a beam panel, a girder panel, or a combined panel, as applicable
- $\beta$ = Modal damping ratio
- $W$ = Effective weight supported by the beam panel, girder panel or combined panel, as applicable.

2.15.2.5 Acceleration Limit

Acceleration limits depend on occupancy categories and recommended values are provided in DG11 Table 4.1. The program uses Table 4.1 values as
program default. However, the user has control to change the acceleration limits in the design preferences or overwrites.

2.15.3 Design for Rhythmic Excitation

2.15.3.1 Effective Weight, \( w_t \)

The effective panel weight is the effective weight per unit area of participants distributed over the floor panel.

2.15.3.2 Rhythmic Loading Parameters: \( w_p, \alpha, I \) and \( f \)

The effective total weight per unit area distributed over the floor panel (weight of participants plus weight of floor system) is taken from DG11 Table 5.2. When areas are partially occupied by the occupants, the value of \( w_p \) is reduced on the basis of equivalent effect (moment or deflection) for a fully loaded span. The values of \( \alpha, I \) and \( f \) are also taken from DG11 Table 5.2.

2.15.3.3 Vibration Frequency

The program calculates the first natural vibration frequency of a beam using the Dunkerley relationship.

\[
f_n = 0.18 \sqrt{\frac{g}{(\Delta_j + \Delta_g)}}
\]

(DG11 Eqn. 3.4)

where,

\( f_n \) = First natural frequency of the beam in cycles per second

\( \Delta_j \) and \( \Delta_g \) = Beam and girder deflections due to the weight supported respectively

\( g \) = Acceleration of gravity

2.15.3.4 Damping

The damping associated with floor systems depends primarily on non-structural components, finishing, furnishings and occupants. DG11 Table 4.1 provides the recommended values for modal damping ratio, \( \beta \). Recommended modal damping ratios range between 0.01 to 0.05.
2.15.3.5 Computation of Peak Acceleration

The peak acceleration, $a_p$, of the floor due to a harmonic rhythmic force is obtained from the following expression:

$$a_p = \frac{1.3\alpha_i w_p/w_t}{g \left[ \left( \frac{f_n}{f} \right)^2 - 1 \right]^2 + \left( \frac{2\beta f_n}{f} \right)^2}$$  \hspace{1cm} (DG11 Eqn. 2.4)

where,

- $\alpha_i$ = Dynamic coefficient from DG11 Table 2.1
- $w_p$ = Effective weight per unit area of participants distributed over floor panel
- $w_t$ = Effective distributed weight per unit area of floor panel, including occupants
- $f_n$ = Natural frequency of floor structure
- $f$ = Forcing frequency
- $\beta$ = Modal damping ratio

The effective maximum acceleration, accounting for all harmonics, is estimated from the following combination rule (Allen 199a).

$$a_m = \left[ \sum a_i^{1.5} \right]^{1/5}$$  \hspace{1cm} (DG11 Eqn. 2.6)

where,

- $a_i$ = Peak acceleration for the $i^{th}$ harmonic.

2.15.3.6 Acceleration Limit

Acceleration limits depend on occupancy categories and recommended values are provided in DG11 Table 5.3. The program uses Table 5.3 values as program default. However, the user has control to change the acceleration limits in the design preferences or overwrites.
2.15.4 Design for Sensitive Equipment

2.15.4.1 Floor Vibration

The following procedure is used for calculating the stiffness of a floor under a concentrated force of 1kN per mm (5.7 kips per inch). The deflection of a beam panel under concentrated forces, $\Delta_{jp}$, is estimated as

$$\Delta_{jp} = \frac{\Delta_{0j}}{N_{eff}}$$

(DG11 Eqn. 4.6)

where,

$\Delta_{0j} =$ The static deflection of a single, simply supported, T-beam due to a 1-kN (0.225-kip) concentrated force calculated using the same effective moment of inertia as was used for the frequency calculation.

$N_{eff} =$ Number of effective beams or joists. The concentrated load is to be placed so as to produce the maximum possible deflection of the T-beam. The effective number of T-beams can be estimated from

$$N_{eff} = 0.49 + 34.2 \frac{d_e}{S} + \left(9.0 \times 10^{-6}\right) \frac{L_j^4}{I_t} - 0.00059 \left(\frac{L_j}{S}\right)^2 \geq 1.0$$

(DG11 Eqn. 4.7)

and,

$$0.018 \leq \frac{d_e}{S} \leq 0.208$$

$$4.5 \times 10^6 \leq \frac{L_j^4}{I_t} \leq 257 \times 10^6$$

$$2 \leq \frac{L_j}{S} \leq 30$$

where,

$d_e =$ Effective slab depth
$S =$ Beam spacing
$L_j =$ Beam span
$I_t =$ Transformed moment of inertia of the T-beam
The total floor deflection, $\Delta_p$, is then computed using the following equation:

$$\Delta_p = \Delta_{jp} + \Delta_{gp} \sqrt{2}$$  \hspace{1cm} (DG11 Eqn. 4.8)

where,

$$\Delta_{gp} = \text{maximum deflection of the more flexible girder due to a 1-kN (0.225-kip) concentrated load, using the same effective moment of inertia as used in the frequency calculation. The deflections usually are estimated using the following expression:}$$

$$= \frac{PL^3}{48EI_i}$$  \hspace{1cm} (DG11 Eqn. 4.9)

which assumes simple span conditions. To account for rotational restraint provided by beam and girder web framing connections, the coefficient 1/48 is reduced to 1/96, which is the geometric mean of 1/48 (for simple span beams) and 1/192 (for beams with built-in ends).

### 2.15.4.2 Vibration Frequency

The program calculates the first natural vibration frequency of a beam using the Dunkerley relationship.

$$f_n = 0.18 \left( \frac{g}{\sqrt{\Delta_j + \Delta_g}} \right)$$  \hspace{1cm} (DG11 Eqn. 3.4)

where,

$$f_n = \text{First natural frequency of the beam in cycles per second}$$

$$\Delta_j \text{ and } \Delta_g = \text{Beam and girder deflections due to the weight supported respectively}$$

$$g = \text{Acceleration of gravity}$$

### 2.15.4.3 Damping

The damping associated with floor systems depends primarily on non-structural components, finishing, furnishings and occupants. DG11 Table 4.1 provides the recommended values for modal damping ratio, $\beta$. Recommended modal damping ratios range between 0.01 to 0.05.
2.15.4.4 Peak Vibration of Floor due to Walking

The maximum displacement due to a footfall impulse, the floor static displacement, $X_{\text{static}}$, due to a point load, $F_m$, is computed as follows:

$$A_m = \frac{X_{\text{max}}}{X_{\text{static}}}$$  \hspace{1cm} (DG11 Eqn. 6.2)

where,

$$X_{\text{static}} = F_m \Delta \rho$$

$$X_{\text{max}} = \frac{F_m \Delta \rho f_o^2}{2 f_n^2}$$  \hspace{1cm} (DG11 Eqn. 6.3)

$F_m$ and $\Delta \rho$ are obtained from DG11 Table 6.2.

Since a floor vibrates at its natural frequency due to a footfall impulse, the maximum velocity is determined from the following equation:

$$V_{\text{max}} = 2\pi f_o X_{\text{max}}$$  \hspace{1cm} (DG11 Eqn. 6.4a)

2.15.4.5 Vibration Velocity Limit for Sensitive Equipment

For sensitive equipment, a criterion is based on the vibration velocities given in Table 6.1 of DG11. The following expression can be used to convert a given velocity, $V$, to the corresponding acceleration, $a$.

$$a/g = 2\pi f V/g$$  \hspace{1cm} (DG11 Eqn. 6.1)

2.16 Distribution of Steel Headed Stud Anchors on a Composite Beam

This section describes how the program calculates and reports the distribution of shear studs on a composite beam. It begins by introducing the term “composite beam segments.” Next it describes how the program calculates the shear stud distribution for a beam.
2.16.1 Composite Beam Segments

For the purposes of reporting the number of shear studs required on each composite beam, the program divides the top flange of each composite beam into segments. The segments extend along the length of the beam. Each composite beam consists of one or more composite beam segments.

A composite beam segment may span between any two of the following three items provided that there is concrete on the beam, and the beam top flange is available over the full length of the segment:

1. The physical end of the beam top flange.
2. Another beam in the program model that frames into the beam being considered.
3. The physical end of the concrete slab on top of the beam considered.

A composite beam segment cannot exist in locations where concrete is not over the beam or where the beam top flange has been cope. Figure 2-12 shows some examples of composite beam segments. The figure uses the following notation:

\[ L \quad = \text{Length of composite beam measured from center-of-support to center-of-support, mm.} \]

\[ LCBS = \text{Length of a composite beam segment, mm.} \]

Note that a composite beam can have more than one composite beam segment, as shown in Figure 2-12c.

2.16.1.1 Physical End of the Beam Top Flange

When one or both ends of a composite beam segment lie at the end of a composite beam, the program must assume the exact location of the end(s) of the beam top flange to calculate a length, \( LCBS \), for the composite beam segment.
Figure 2-12 Examples of Composite Beam Segments, $L_{CBS}$

a) $L_{CBS}$ for Beam Between Two Columns

b) $L_{CBS}$ for Beam Between Two Girders

c) $L_{CBS}$ when Beams Frame into Considered Beam

d) $L_{CBS}$ when Slab Ends in Beam Span
Notes:
1. $S$ is the support distance.
2. $G$ is the gap distance.
3. If a beam is supported by a wall or a point support, ETABS assumes that the dimension $S$ is 0 mm.
4. The dimension $b_f$ in Cases 1 and 2 is the top flange width of the supporting girder.
5. The dimension $b_f$ in Cases 3 and 5 is the flange width of the supporting column (dimension parallel to the local 3-axis). If the two flanges have different widths, the larger flange width is used.
6. The dimension $d$ in Cases 4 and 5 is the depth of the supporting column (dimension parallel to the local 2-axis).

**Figure 2-13 Examples of Support Distance $S$ and Gap Distance $G$**

When determining the location of the ends of the beam top flange, the program begins by assuming that the top flange extends from the center of the left support to the center of the right support. It then subtracts a support distance, $S$, from each end of the beam and a gap distance, $G$, from each end of the beam.
The gap distance, \( G \), is always 12 mm. The support distance varies depending on the type of support and the angle at which the beam frames into the support.

If the end of the beam is supported by a wall or a point support, the support distance, \( S \), is assumed to be zero. If the end of the beam is supported by another beam, support distance \( S \) is determined as illustrated in Cases 1 and 2 in Figure 2-13, which show the beam supported by an I-shaped beam. A similar method is used in the unusual case of other types of support beams.

If the end of the beam is supported by a column, \( S \) is determined as illustrated in Cases 3, 4 and 5 in Figure 2-13, which show the beam supported by an I-shaped column. A similar method is used for box columns and in the very unusual case of some other column shape.

In the unusual case of some other column shape, the program draws a bounding rectangle around the shape. The sides of the rectangle are parallel to the local 2 and 3 axes of the shape. The beam is assumed to connect to the center of the bounding rectangle. The dimensions of the edges of the rectangle are assumed to be \( b_f \) and \( d \), where \( b_f \) is the dimension parallel to the local 3 axis, and \( d \) is the dimension parallel to the local 2 axis.

### 2.16.1.2 Distribution of Shear Studs Within a Composite Beam Segment

The program *always* assumes a uniform intensity of shear studs within a composite beam segment. This is a convenient assumption that in some cases may lead to a slightly conservative number of shear studs.

### 2.16.2 How the Program Distributes Steel Headed Stud Anchors on a Beam

This section describes how the program calculates the shear stud distribution on a beam.

When determining the distribution of shear studs on a composite beam, the program considers the following output stations:

1. The output station with the maximum positive moment.
2. Any output station with a positive moment greater than 0.999 times the maximum positive moment.

3. Any output station that has a point load applied to it for any load case defined in the program. Even if the load case with the point load is not used in the design load combinations for composite beam design, the program will still consider the output station associated with the point load when it determines the shear stud distribution. It will not, however, in any way explicitly consider the loads in that unused load case when determining the shear stud distribution.

At each considered output station, the program begins by determining the distances $L_{1\text{ left}}$ and $L_{1\text{ right}}$. These are illustrated in Figure 2-14 for a typical composite beam with positive moment only and with a concrete slab over metal deck along its entire length. The following notation is used in the figure:

$$L = \text{Length of composite beam measured from center-of-support to center-of-support, mm.}$$

$$L_{1\text{ left}} = \text{Distance from the output station considered to the closest point of zero moment or physical end of the beam top flange, or physical end of the concrete slab on the left side of the output station considered, mm.}$$

$$L_{1\text{ right}} = \text{Distance from the output station considered to the closest point of zero moment or physical end of the beam top flange, or physical end of the concrete slab on the right side of the output station considered, mm.}$$

![Figure 2-14 Illustration of $L_{1\text{ left}}$ and $L_{1\text{ right}}$](image)

How the Program Distributes Steel Headed Stud Anchors on a Beam
Next, the program calculates the number of shear studs, $N$, required within the lengths $L_{\text{left}}$ and $L_{\text{right}}$. This is a code-specific calculation and is described in the next chapter.

The program works along the beam from left to right, making calculations at each considered output station along the way. These calculations are described later in this section. When there is more than one composite beam segment along the beam, the program must also work back along the beam from right to left, again making calculations at each considered output station along the way, after finishing the pass from left to right.

When the program completes the necessary calculations at each considered output station, it has determined the required uniformly spaced shear studs in each composite beam segment along the beam based on strength considerations. If the calculated number of studs is then found to be less than the minimum required number of studs on the beam, the program increases the number of studs on the beam accordingly. This check is described later in the subsection entitled *Minimum and Maximum Number of Shear Studs in a Composite Beam Segment*.

The program also checks if the number of shear studs required based on strength considerations or minimum stud requirements actually fit on the beam. This check is described in the section entitled *Number of Shear Studs that Fit in a Composite Beam Segment* later in this chapter. If the required number of studs does not fit on the beam, the program considers the beam to be inadequate.

In the following description of the calculations, the program performs as it steps along the beam and then back again, the terms $L_{\text{CBS}n}$ and $N_{\text{CBS}n}$ are used. $L_{\text{CBS}}$ is the length of a composite beam segment, and $N_{\text{CBS}}$ is the number of uniformly spaced shear studs required in a composite beam segment. The $n$ is the composite beam segment number. The leftmost composite beam segment is always $L_{\text{CBS}1}$, and the numbering of composite beam segments then proceeds in order toward the right end of the beam.

The values we are ultimately interested in are the $N_{\text{CBS}n}$ values. Note that the final $N_{\text{CBS}n}$ values calculated are the values of interest. All other $N_{\text{CBS}n}$ values are intermediate values.
Also in the equations used note that \( N_{CBS\text{Prev}} \) is the value of \( N_{CBS} \) calculated at the previously considered output station. Finally the term Roundup used in some of the equations means to calculate the indicated quantity and round it up to the next integer.

### 2.16.2.1 Equations Used When the Program Works from Left to Right

When the program is working from left to right along the beam, the equation used to calculate \( N_{CBSn} \) depends on the location of the output station considered.

#### (a) Output Station in Composite Beam Segment 1

When working along the beam from left to right and the output station considered falls in composite beam segment 1, or at the right end of composite beam segment 1, the following equation is used to determine the value of \( N_{CBS1} \). Note that when there is only one composite beam segment along the beam, the following equation is used at each considered output station.

\[
N_{CBS1} = \text{Roundup} \left[ \text{Max} \left( \frac{N}{L_{\text{left}}}, \frac{N}{L_{\text{right}}} \right) \cdot L_{CBS1} \right] \geq N_{CBS1\text{Prev}}
\]

Values of \( N_{CBSn} \) where \( n > 1 \) (i.e., values of \( N_{CBS} \) for composite beam segments 2, 3, etc.) are not applicable and thus not calculated at these stations when working along the beam from left to right. In the term \( N_{CBS1} \), the "1" denotes composite beam segment 1.

#### (b) Output Station in Composite Beam Segment \( n, n > 1 \)

The equations in this subsection are used when the output station considered falls in composite beam segment \( n \), where \( n > 1 \), and the program is working from left to right along the beam. Note that if the output station considered coincides with the right end of composite beam segment \( n \), the output station is assumed to be in composite beam segment \( n \) (when working along the beam from left to right).

The following equation applies for composite beam segments \( i \), where \( i \) is an integer less than \( n \).
The next two equations apply for composite beam segment \( n \).

If \( \frac{N}{L_{\text{left}}} \sum_{i=1}^{n-1} L_{\text{CBS}i} < \sum_{i=1}^{n-1} N_{\text{CBS}i} \), use the following equation to calculate \( N_{\text{CBS}n} \).

\[
N_{\text{CBS}n} = \text{Roundup} \left( \frac{N}{L_{\text{left}}} \sum_{i=1}^{n-1} L_{\text{CBS}i} \right) \geq N_{\text{CBS}n} \text{ Prev}
\]

Otherwise use the next equation to calculate \( N_{\text{CBS}n} \).

\[
N_{\text{CBS}n} = \text{Roundup} \left( \frac{N - \sum_{i=1}^{n-1} N_{\text{CBS}i}}{L_{\text{left}} - \sum_{i=1}^{n-1} L_{\text{CBS}i}} \right) \sum_{i=1}^{n-1} L_{\text{CBS}i} \geq N_{\text{CBS}n} \text{ Prev}
\]

When \( i > n \), values of \( N_{\text{CBS}i} \) are not applicable and thus are not calculated at those stations when working along the beam from left to right.

### 2.16.2.2 Equations Used When the Program Works from Right to Left

Recall that it is only necessary for the program to work back along the beam from right to left if there is more than one composite beam segment along the length of the beam. When the program is working back along the beam from right to left, the equation used to calculate \( N_{\text{CBS}n} \) again depends on the location of the output station considered.

(a) Output Station in Rightmost Composite Beam Segment

The equations in this subsection are used when working back along the beam from right to left and the output station considered falls in the rightmost composite beam segment, or at the left end of the rightmost composite beam segment. For the rightmost composite beam segment:
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\[ N_{CBS_{\text{rightmost}}} = \text{Roundup} \left[ \text{Max} \left( \frac{N}{L_{\text{left}}}, \frac{N}{L_{\text{right}}} \right) * L_{CBS_{\text{rightmost}}} \right], \]

\[ N_{CBS_{\text{rightmost}}} \geq N_{CBS_{\text{rightmost prev}}} \]

For other composite beam segments that are not the rightmost composite beam segment, the following equation applies, where \( i \) represents the composite beam segment number.

\[ N_{CBS_i} = N_{CBS_{\text{prev}}} \]

(b) Output Station Not in Rightmost Composite Beam Segment

The equations in this subsection apply when working back along the beam from right to left. (Note that this implies that there is more than one composite beam segment along the beam.) In this section, assume that the output station considered falls within (or at the left end of) composite beam segment \( n \).

The following equation applies for composite beam segments \( i \), where \( i \) is an integer greater than \( n \). For example, if the output station considered falls in composite beam segment 2, this equation applies to composite beam segments 3, 4, etc.

\[ N_{CBS_i} = \text{Roundup} \left( \frac{N}{L_{\text{right}}} * L_{CBS_i} \right) \geq N_{CBS_{\text{prev}}} \]

The following two equations apply for composite beam segment \( n \). For example, if the output station considered falls in composite beam segment 2, the following two equations apply to composite beam segment 2 only.

If

\[ \frac{N}{L_{\text{right}}} * \sum_{i=n+1}^{\text{rightmost}} L_{CBS_i} < \sum_{i=n+1}^{\text{rightmost}} N_{CBS_i} \]

use the following equation to calculate \( N_{CBS_n} \).

\[ N_{CBS_n} = \text{Roundup} \left( \frac{N - \sum_{i=n+1}^{\text{rightmost}} N_{CBS_i}}{L_{\text{right}} - \sum_{i=n+1}^{\text{rightmost}} L_{CBS_i}} * L_{CBS_n} \right) \geq N_{CBS_{n \text{ prev}}} \]
Otherwise, use this equation to calculate $N_{CBSn}$.

$$N_{CBSn} = \text{Roundup} \left( \frac{N}{L_{\text{right}} \times L_{CBSn}} \right) \geq N_{CBSn \, \text{Prev}}$$

The following equation applies for composite beam segments $i$, where $i$ is an integer less than $n$. For example, if the output station considered falls in composite beam segment 2, this equation applies to composite beam segment 1.

$$N_{CBSi} = N_{CBSi \, \text{Prev}}$$

### 2.16.2.3 Minimum and Maximum Number of Shear Studs in a Composite Beam Segment

After the number of shear studs required in a composite beam segment has been calculated using the procedure described in the previous section, the program checks that the number of studs is not less than the required minimum. This required minimum, $MS_{CBS}$, is calculated based on the maximum longitudinal spacing of shear studs along the length of the beam, $\text{MaxLS}$, which is specified on the Shear Studs tab in the composite beam overwrites. This calculation is shown in the following equation.

$$MS_{CBS} = \text{Roundup} \left( \frac{L_{CBS}}{\text{MaxLS}} \right)$$

The program also checks that the number of studs required in a composite beam segment does not exceed the number that can actually fit in the segment. The section entitled *Number of Shear Studs that Fit in a Composite Beam Segment* describes how the program determines the maximum number of shear studs that can fit into a composite beam segment.

Note that the minimum number of shear studs required in a composite beam segment is calculated based on the maximum longitudinal spacing of shear studs specified on the Shear Studs tab in the overwrites.

### 2.16.3 A Note About Multiple Design Load Combinations

When there are multiple design load combinations on a composite beam, the program determines the stud distribution separately for each design load.
combination and then uses an intelligent algorithm to determine the final stud distribution that satisfies all design load combinations.

As an example, consider a beam with four composite beam segments (CBS1 through CBS4) and two separate design load combinations (1 and 2). Figure 2-15(a) shows the stud distribution obtained for the first design load combination, and Figure 2-15(b) shows the stud distribution obtained for the second design load combination. Note that the term $\text{N}_{CBS}$ in the figure denotes the number of shear studs in the corresponding composite beam segment.

Figure 2-15(c) shows the final stud distribution that reports for this beam. Note that the intelligent algorithm allows the program to shift one of the five shear studs required in composite beam segment 2 for design load combination 1 into composite segment 1.

---

A Note About Multiple Design Load Combinations
2.17  Number of Shear Studs that Fit in a Composite Beam Segment

Composite beam segments are defined in the subsection entitled *Composite Beam Segments* of the section entitled *Distribution of Shear Studs on a Composite Beam*. In short, a composite beam segment spans between any of the following: (1) physical end of the beam top flange; (2) another beam framing into the beam being considered; (3) physical end of the concrete slab on top of the beam. When the program designs a composite beam, it reports the required number of *uniformly spaced* shear studs in each composite beam segment.

For a beam section to be adequate in the program Composite Beam Design postprocessor, the stresses and deflections for the beam must be less than the allowable stresses and deflections, and the number of shear studs required in each composite beam segment must be less than or equal to the maximum number of shear studs that can fit in the composite beam segment. This section describes how the program calculates the maximum number of shear studs that fit in a composite beam segment.

The program uses the same process to determine the number of shear connectors that can fit on a composite beam when there is a solid slab with no metal deck and when the deck ribs span parallel to the beam span. The program uses a different process when the deck ribs span perpendicular to the beam. These conditions are described in the next two sections.

2.17.1  Solid Slab or Deck Ribs Oriented Parallel to Beam Span

When there is a solid slab with no metal deck, or when there is metal deck and the metal deck ribs are assumed to be oriented parallel to the beam span, the program uses the following process to determine the number of shear studs that can be placed within a composite beam segment. See the subsection entitled *Composite Beam Segments* of the section entitled *Distribution of Shear Studs on a Composite Beam* for a definition of a composite beam segment.

The number of shear studs that can fit in a row across the beam top flange may be limited by the width of the beam top flange, by the width of the deck ribs, or...
by the Max Studs per Row item specified on the Shear Studs tab in the composite beam overwrites.

1. The program determines the number of shear studs that can fit in a single row across the width of the top flange of the beam. When there is a solid slab (no metal deck), the number of shear studs is limited by the width or thickness of the beam flange (item 1a below), or by the "Max Studs per Row" item specified on the Shear Studs tab in the composite beam overwrites. When the deck spans parallel to the beam, the number of shear studs may be limited by the width or thickness of the beam flange (item 1a below), the width of the metal deck rib (item 1b below), or by the "Max Studs per Row" item specified on the Shear Studs tab in the composite beam overwrites. Following is a description of each of these limits:

a. When checking the number of shear studs that fit across the width of the beam flange, the program assumes that the studs are centered about the centerline (web) of the beam and that the center of a shear stud can be no closer than $d_s$ or 25 mm, whichever is larger, to the edge of the beam flange. This is illustrated in the following sketch.

In the preceding paragraph and the sketch, $d_s$ is the diameter of the shear stud. The clearance requirement means that the minimum clear distance from the face of a shear stud to the edge of the beam flange is equal to one-half of a shear stud diameter. For shear studs less than 25 mm in diameter (typically they are 19 mm diameter), the program clearance is slightly more than one-half of a shear stud diameter. This clear distance is provided by the program to allow for adequate welding of the shear stud.

b. When checking the number of shear studs that fit within a metal deck rib, the program assumes that the studs and deck rib are centered about the centerline (web) of the beam and that the center of a shear stud can
be no closer than \( d_s + \frac{h_r}{4} \) to the edge of the beam flange. This is illustrated in the following sketch.

\[
\begin{align*}
\geq (d_s + h_r/4) \\
\geq (d_s + h_r/4)
\end{align*}
\]

In the preceding paragraph and the sketch, \( d_s \) is the diameter of the shear stud, and \( h_r \) is the height of the metal deck ribs. The \( w_r \) dimension in the sketch is the average width of the deck ribs. The spacing between the shear studs is the “Min Tran. Spacing” item specified on the Shear Studs tab in the composite beam design overwrites. The default value for this shear stud spacing is \( 4d_s \).

The dimension \( d_s + h_r/4 \) is derived by assuming that the slope of the sides of the metal deck ribs is 2 to 1 and that the clear distance from the face of the shear stud to the point where the edge of the deck rib starts to rise is equal to one-half of a shear stud diameter. This clear distance is provided by the program to allow for adequate welding of the shear stud.

Regardless of the number of studs calculated to fit across the width of the beam flange in items 1a or 1b above, the program does not use a number of studs larger than the “Max Studs per Row” item specified on the Shear Studs tab in the composite beam design overwrites.

2. The program determines the number of rows of shear studs that can fit between the two considered points on the beam top flange. This number of rows is controlled by the “Min Long Spacing” item specified on the Shear Studs tab in the composite beam design overwrites.

3. The program multiplies the maximum number of shear studs in a single row, determined in item 1, by the number of rows of studs that can fit in a composite beam segment, determined in item 2, to calculate the maximum number of studs that can fit in the composite beam segment.

Figure 2-16 is a flowchart that illustrates the details of how the program calculates the maximum number of shear studs that fit in a composite beam segment.
segment when there is a solid slab or when the span of the metal deck is parallel to the beam span.

The term "Int" in the flowchart means to calculate the indicated quantity and round the result down to the nearest integer. The definitions of the variables used in the flowchart are:

\[ t_{f\text{-top}} = \text{Thickness of beam top flange, mm.} \]
\[ d_s = \text{Diameter of a shear stud connector, mm.} \]
\[ SPR_{max} = \text{Maximum number of shear studs that can fit in one row across the top flange of a composite beam, unitless.} \]

**Figure 2-16 Flowchart of the Method Used to Determine Maximum Number of Shear Studs that Can Fit within a Composite Beam Segment When There is a Solid Slab or the Metal Deck Ribs Are Oriented Parallel to the Beam Span** (The term "Int" in the flowchart means to calculate the indicated quantity and round the result down to the nearest integer.)

Temp = Temporary variable equal to the minimum of the 2 or 3 items specified in the parenthesis, mm. The items specified are separated by commas.
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\[ b_{\text{top}} = \text{Width of beam top flange, mm.} \]
\[ w_r = \text{Average width of metal deck rib, mm.} \]
\[ h_r = \text{Height of the metal deck rib, mm.} \]
\[ MTS = \text{Minimum transverse spacing of shear studs across the beam top flange as specified on the Shear Studs tab in the composite beam overwrites, mm.} \]
\[ MSPR = \text{Maximum shear studs per row across the beam top flange as specified on the Shear Studs tab in the composite beam overwrites, unitless.} \]
\[ RS_{\text{max}} = \text{Maximum number of rows of shear studs that can fit in a composite beam segment, unitless.} \]
\[ L_{CBS} = \text{Length of a composite beam segment, mm.} \]
\[ MLS = \text{Minimum longitudinal spacing of shear studs along the length of the beam as specified on the Shear Studs tab in the composite beam overwrites, mm.} \]
\[ NS_{\text{max}} = \text{Maximum number of shear studs that fit in a composite beam segment, unitless.} \]

Note that in the flowchart formulation, the studs located closest to the ends of the composite beam segment are located no closer than MLS/2 to the ends of the composite beam segment. This helps prevent possible double-counting of shear studs in adjacent composite beam segments.

2.17.2 Deck Ribs Oriented Perpendicular to Beam Span

When the deck ribs are oriented perpendicular to the beam span, the program limits the number of rows of shear studs across the width of the beam flange in each metal deck rib to one. For a typical case with 19 mm diameter shear studs and an average width of the deck rib equal to 150 mm, it is difficult to fit more than one row of shear studs in a deck rib and still have adequate edge clearances. To have more than one row of shear studs in a single deck rib, specify a user-defined shear connector pattern for the beam.
Chapter 2 - Design Prerequisites

The process used to determine the number of shear studs that can fit in a composite beam segment when the metal deck is assumed to span perpendicular to the beam span is described as follows.

1. The program determines the number of shear studs that can fit in a single row across the width of the top flange of the beam. This number of shear studs is limited by either the width or thickness of the beam flange, or by the "Max Studs per Row" item specified on the Shear Studs tab in the composite beam overwrites.

When checking the number of shear studs that fit across the width of the beam flange, the program assumes that the studs are centered about the centerline (web) of the beam and that the center of a shear stud can be no closer than either \( d_s \) or 25 mm, whichever is larger, to the edge of the beam flange. This is illustrated in the sketch to the right.

In the preceding paragraph and the sketch, \( d_s \) is the diameter of the shear stud. The clearance requirement means that the minimum clear distance from the face of a shear stud to the edge of the beam flange is equal to one-half of a shear stud diameter. For shear studs less than 25 mm in diameter (typically they are 19 mm in diameter), the program clearance is slightly more than one-half of a shear stud diameter. This clear distance is provided by the program to allow for adequate welding of the shear stud.

Some codes require that if the thickness of the beam flange is less than the diameter of the stud divided by 2.5, the shear studs must be located on top of the beam web. This means that only one stud can fit across the width of the beam flange if \( t_f < d_s / 2.5 \). The program checks the top flange thickness for this requirement when determining the number of studs that fit across the width of the beam flange.

2. The program determines how many deck ribs are available to receive shear studs within the length of the composite beam segment. To determine this, the program makes several assumptions, which are described as follows:

a. The mid-height of a side of the metal deck rib is assumed to align with one end of the composite beam segment, as shown in Figure 2-17. In
other words, one end of the composite beam segment is always assumed to start with an "up" flute.

b. If one-half or more of the width of a metal deck rib down flute is within the length of the composite beam segment, the program assumes that the deck rib is available to receive shear studs. This is illustrated in Figure 2-17.

c. The minimum longitudinal spacing of shear studs along the length of the beam as specified on the Shear Studs tab in the composite beam overwrites is assumed to apply when the deck ribs run perpendicular to the beam span. In some cases, this could cause deck ribs that are within the length of the composite beam segment to be unavailable to receive shear studs.

3. The program multiplies the maximum number of shear studs in a single row across the beam flange, determined as described in item 1, by the number of deck ribs within the length of the composite beam segment that are available to receive shear studs, determined as described in item 2, to calculate the maximum number of studs that can fit in the composite beam segment.

Figure 2-18 is a flowchart that illustrates the details of how the program calculates the maximum number of shear studs that fit in a composite beam segment when the span of the metal deck is perpendicular to the beam span.
The term "Int" in the flowchart means to calculate the indicated quantity and round the result down to the nearest integer. The definitions of the variables used in the flowchart are the same as those used in the Figure 2-18 flowchart, with the following additions:

\[ S_r = \text{Center-to-center spacing of metal deck ribs, mm.} \]

\[ NR = \text{Available number of metal deck ribs within the composite beam segment that are available to receive shear studs, unitless.} \]

### 2.17.2.1 Different Deck Type or Orientation on Beam Sides

When a different type or orientation of the metal deck exists on the two sides of the beam, the program determines the maximum number of shear studs that fit in the composite beam segment for each of the two deck types/orientations. The smaller maximum value obtained is used as the maximum number of shear studs that fit within the composite beam segment.
2.18 User Defined Shear Connector Patterns

This section explains how to specify the shear stud pattern rather than have the program determine the distribution of shear studs. This can be useful when checking an existing building, or if there is a certain shear stud pattern that is required, for example, one shear stud per foot of beam length.

2.18.1 Specifying a User Defined Shear Connector Pattern

User defined shear connector patterns are specified on the Shear Studs tab in the composite beam overwrites. See Appendix B Overwrites for more information.

The composite beam overwrites can be used to specify a uniform spacing of shear studs located on top of the beam web and centered along the length of the beam top flange, or to specify a starting and ending point for a beam section and the number of studs that are uniformly spaced within the beam section. Use one of these options or use the two options together to define the studs on a beam.

The term beam section is purposely used here to differentiate it from a composite beam segment. Do not confuse composite beam sections and composite beam segments. They are two entirely different items. Composite beam segments are described in the subsection entitled Composite Beam Segments of the section entitled Distribution of Shear Studs on a Composite Beam in this chapter. Beam sections are simply an arbitrary length of the beam, defined by a starting and ending location over which a certain number of uniformly spaced shear studs is specified.

The following two sections describe the two methods of specifying user defined shear studs.

2.18.2 Uniformly Spaced Shear Studs Over the Length of the Beam

When uniformly spaced user defined shear studs are specified over the length of the beam, the program treats the shear studs as if they are all in a single line along the beam web and disregards any checks for minimum longitudinal spacing requirements.
Figure 2-19 illustrates uniformly spaced user defined shear studs over the length of the beam. These shear studs are specified by inputting the spacing for the Uniform Spacing item on the Shear Studs tab in the composite beam overwrites.

Note the following about these shear studs:

1. The shear studs are assumed to occur over the length of the top flange of the beam. In most cases, this is shorter than the center-of-support to center-of-support length of the beam.

2. There is assumed to be one shear stud per row. To use this option to specify 2 studs every 300 mm, specify a spacing of 150 mm. The 150 mm spacing gives the closest equivalent to two studs every 300 mm.

3. The program determines the exact distance from the end of the beam top flange (or end of the concrete slab) to the first shear stud, as shown in the following equation. In that equation the term “Int” means to calculate the indicated quantity and round the result down to the nearest integer, and the
term "Specified Spacing" is the spacing input in the composite beam overwrites for the Uniform Spacing item.

\[
ED = \frac{TFL - Int\left(\frac{TFL - MLS}{Specified\ Spacing}\right) \times Specified\ Spacing}{2}
\]

where,

\(ED\) = Distance from the end of the beam top flange (or end of the concrete slab) to the first shear stud, m.

\(TFL\) = The length of the beam top flange available to receive shear studs, mm. This length is typically determined by subtracting the support distance and the gap distance at each end of the beam from the center-of-support to center-of-support length of the beam. In special cases, an additional distance can be subtracted if the slab does not exist over some portion of the beam.

\(MLS\) = Minimum longitudinal spacing of shear studs along the length of the beam, as specified on the Shear Studs tab in the composite beam overwrites, mm.

After the shear studs at the end of the beam top flange (or end of the concrete slab) have been located using the preceding equation, the program knows the exact location of each uniformly spaced shear stud along the length of the beam.

In the preceding equation, the studs at the ends of the beam are assumed to be no closer than \(MLS/2\) from the end of the beam top flange. The studs at the ends of the beam are also assumed to be no farther than \((MLS + Specified\ Spacing)/2\) from the end of the beam top flange. Finally, the distance from the studs at the ends of the beam to the end of the beam top flange is assumed to be the same at each end of the beam.

Similar to the preceding, if the concrete slab stops before the end of the beam, the first shear stud at that end of the beam is assumed to occur at a distance not less than \(MLS/2\) from the end of the slab and not more than \((MLS + the\ specified\ uniform\ spacing)/2\) from the end of the slab.
2.18.3 Additional Shear Studs in Specified Sections of Beam

When the user specifies the starting and ending points of a beam section and the number of uniformly spaced shear studs in the section, the program treats the shear connectors as if they are all in a single line and disregards any checks for minimum longitudinal spacing requirements.

2.18.3.1 Defining Additional Beam Sections

To define additional beam sections for specifying shear studs, simply specify a distance along the beam that locates the starting point of the beam section, specify a second (longer) distance along the beam that locates the ending point of the beam section, and then specify the total number of uniformly spaced shear studs that fall within the specified beam section.

Distances can be specified as absolute (actual) distances or relative distances, both measured from the I-end of the beam. A relative distance to a point is the absolute distance to that point divided by the length of the beam measured from the center-of-support to center-of-support.

Do not confuse beam sections with composite beam segments. See the section entitled Specifying a User Defined Shear Connector Pattern earlier in this section for more information.

Note the following about the shear studs specified for additional beam sections:

- The program assumes that the specified shear studs occur in a single line along the beam web within the specified length of the beam section. It further assumes that the end shear studs in the beam section are located one-half of the equal space from the ends of the specified beam section. These assumptions mean that the spacing of shear studs in a beam section is equal to the length of the beam top flange available to receive shear studs in the beam section divided by the specified number of shear studs. See Figure 2-20 for an example.

The figure shows a beam section that is 2750 mm long. Assume that 11 shear studs have been specified for this beam section. The spacing of shear studs in the beam section is equal to the beam section length divided by the number of studs, that is, 2750 mm/11 studs = 250 mm/stud. The end studs are located
one-half of a space, that is, 250 mm/2 = 125 mm, from each end of the beam section.

The program does not check shear stud spacing requirements for user defined shear stud patterns.

- Assume that a beam section is specified at the end of a beam and the beam top flange does not exist over a portion of that beam section length. This can often happen because, as described in the Physical End of the Beam Top Flange of the section entitled Distribution of Shear Studs on a Composite Beam, the program subtracts a support distance and a gap distance from the end of the beam when computing the length of the beam top flange.

In that case, the program places all of the specified shear studs on the portion of the top flange that does exist. See Figure 2-21 for an illustration.

The figure shows a beam section at the end of the beam that is 3000 mm long. The end of the beam top flange starts 250 mm from the specified left end of the beam section. Thus, the actual length of top flange available for shear studs is 2750 mm. Assume that 11 shear studs have been specified for this beam section.

As previously mentioned, the spacing of shear studs in a beam section is equal to the length of the beam top flange available to receive shear studs in the beam section divided by the specified number of shear studs. In this case,
2750 mm11 studs = 250 mm/stud. The end studs are located one-half of a space, that is \(250 \text{ mm} / 2 = 125 \text{ mm}\), from each end of the beam top flange within the beam section.

![Figure 2-21 Example Showing No Beam Top Flange Over a Portion of the Specified Beam Section Length](image)

- If the beam top flange does not exist over the entire length of the specified beam section, the program ignores the shear studs that are specified for that beam section.

### 2.18.3.2 Example of a User-Defined Shear Stud Pattern

Refer to the example shown in Figure 2-22. To specify the actual shear connector layout shown in Figure 2-22, three beam sections are specified. Table 2-2 shows how each of the three beam sections should be specified.

Figure 2-22b illustrates how the program interprets the stud pattern as specified in Table 2-2. The location and spacing of shear studs is as described in the bulleted items in the previous subsection entitled *Defining Additional Beam Sections*.
Table 2-2 Specification of Beam Sections in the Example Shown in Figure 2-22

<table>
<thead>
<tr>
<th>Beam Section</th>
<th>Starting Point</th>
<th>Ending Point</th>
<th>Number of Studs</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>0 mm</td>
<td>1,000 mm</td>
<td>6</td>
</tr>
<tr>
<td>2</td>
<td>1,000 mm</td>
<td>2,200 mm</td>
<td>4</td>
</tr>
<tr>
<td>3</td>
<td>2,200 mm</td>
<td>3,200 mm</td>
<td>6</td>
</tr>
</tbody>
</table>

2.18.4 How the Program Checks a Beam with User Defined Shear Studs

When the number and location of shear studs on a beam is defined, the program performs flexural design somewhat differently from how it is described elsewhere in this manual. For flexural design with user defined shear studs, the program calculates the percent composite connection (PCC) at each design output station based on the specified shear stud layout. The program then calculates the beam section properties for this PCC and derives a flexural stress ratio (actual stress divided by allowable stress).
2.19 Transformed Section Moment of Inertia

This section describes in general terms how the program calculates the transformed moment of inertia for a composite section, $I_{tr}$. The calculated transformed moment of inertia applies for full (100%) composite connection. See Effective Moment of Inertia for Partial Composite Connection in the next section.

The program determines the transformed section moment of inertia separately for beam deflection check and beam vibration check because the two generally differ.

The deflection transformed section moment of inertia is based on the modulus of elasticity of concrete, $E_c$, defined by the user for the material definition.

The vibration transformed section moment of inertia is based on the enhanced short term modulus of elasticity of concrete due to the small strain range involved in vibration: $E_c$ is taken as the modulus of elasticity as defined by the user multiplied by an enhancement factor, which is 1.35 based on DG11.

Also, for deflection calculations, concrete is assumed to be effective only in compression, whereas for vibration calculations, it is considered effective in both tension and compression.

2.19.1 Background

Figure 2-23 shows a typical rolled steel composite floor beam with the metal deck ribs running parallel to the beam. Figure 2-24 shows a typical composite user-defined steel beam with the metal deck ribs running parallel to the beam. Note that the user-defined beam may have a different top and bottom flange size, and that no fillets are assumed in this beam.
Figure 2-23 Composite Rolled Steel Beam Shown with Metal Deck Ribs Running Parallel to the Beam

Figure 2-24 Composite User-Defined Steel Beam Shown with Metal Deck Ribs Running Parallel to the Beam

2 - 74 Background
For each of these configurations the following items may or may not be included when calculating the transformed section moment of inertia:

**Concrete in the metal deck ribs:** The concrete in the metal deck ribs is included in the calculation when the deck ribs are oriented parallel to the beam (typically the case for girders). It is not included when the deck ribs are oriented perpendicular to the beam (typically the case for infill beams).

**Cover plate:** The cover plate is included only if one is specified by the user in the composite beam overwrites.

Note that the deck type and deck orientation may be different on the two sides of the beam as described in *Multiple Deck Types or Directions Along the Beam Length* in the section entitled *Effective Width of the Concrete Slab*.

Because composite behavior is considered for positive bending only, the transformed section moment of inertia is calculated for positive bending only (top of composite section in compression). Calculation of the transformed section moment of inertia is greatly complicated by the requirement that the concrete resist no tension.

The first task in calculating the transformed section moment of inertia of the composite section is to compute properties for the steel beam alone (plus the cover plate, if it exists). The properties required are the total area, $A_{bare}$, the location of the ENA, $y_{bare}$, and the moment of inertia, $I_s$.

### 2.19.2 Properties of Steel Beam (Plus Cover Plate) Alone

The location of the Elastic Neutral Axis, ENA, for the steel beam alone (plus cover plate if applicable) is defined by the distance $y_{bare}$, where $y_{bare}$ is the distance from the bottom of the bottom flange of the beam to the ENA, as shown in Figure 2-25. If there is a cover plate, $y_{bare}$ is still measured from the bottom of the bottom flange of the beam, not the bottom of the cover plate.

Figure 2-25 also illustrates an example of the dimension $y_1$ that is used in Tables 1 and 2. For a given element of a steel section, the dimension $y_1$ is equal to the distance from the bottom of the beam bottom flange to the centroid of the element. Figure 2-25 illustrates the distance $y_1$ for the beam top flange.
If the beam section is a rolled steel beam or channel chosen from the program section database, $A_{\text{bare}}$, $y_{\text{bare}}$ and $I_{\text{bare}}$ are calculated as shown in Table 2-3 and using the subsequent three equations (after Table 2-4). If the beam section is a user defined (welded) beam, they are calculated using Table 2-4 and the subsequent three equations.

**Table 2-3 Section Properties for Rolled Steel Beam Plus Cover Plate**

<table>
<thead>
<tr>
<th>Item</th>
<th>Area, $A$</th>
<th>$y_1$</th>
<th>$A_{y_1}$</th>
<th>$A_{y_1}^2$</th>
<th>$I_O$</th>
</tr>
</thead>
<tbody>
<tr>
<td>Steel beam</td>
<td>$A_s$</td>
<td>$d/2$</td>
<td>$A_{y_1}$</td>
<td>$A_{y_1}^2$</td>
<td>$I_s$</td>
</tr>
<tr>
<td>Cover plate</td>
<td>$b_{cp}t_{cp}$</td>
<td>$-t_{cp}/2$</td>
<td>$A_{y_1}$</td>
<td>$A_{y_1}^2$</td>
<td>$b_{cp}t_{cp}^3/12$</td>
</tr>
<tr>
<td><strong>Sums</strong></td>
<td>$\sum A$</td>
<td>$\sum (A_{y_1})$</td>
<td>$\sum (A_{y_1}^2)$</td>
<td>$\sum I_O$</td>
<td></td>
</tr>
</tbody>
</table>

**Table 2-4 Section Properties for User-Defined (Welded) Steel Beam Plus Cover Plate**

<table>
<thead>
<tr>
<th>Item</th>
<th>Area, $A$</th>
<th>$y_1$</th>
<th>$A_{y_1}$</th>
<th>$A_{y_1}^2$</th>
<th>$I_O$</th>
</tr>
</thead>
<tbody>
<tr>
<td>Top flange</td>
<td>$b_{f/top}t_{f/top}$</td>
<td>$d - t_{f-top}/2$</td>
<td>$A_{y_1}$</td>
<td>$A_{y_1}^2$</td>
<td>$b_{f-top}t_{f-top}^3/12$</td>
</tr>
<tr>
<td>Web</td>
<td>$h_{tw}$</td>
<td>$d/2$</td>
<td>$A_{y_1}$</td>
<td>$A_{y_1}^2$</td>
<td>$t_{w}h^3/12$</td>
</tr>
<tr>
<td>Bottom flange</td>
<td>$b_{f/bot}t_{f/bot}$</td>
<td>$t_{f-bot}/2$</td>
<td>$A_{y_1}$</td>
<td>$A_{y_1}^2$</td>
<td>$b_{f-bot}t_{f-bot}^3/12$</td>
</tr>
<tr>
<td>Cover plate</td>
<td>$b_{cp}t_{cp}$</td>
<td>$-t_{cp}/2$</td>
<td>$A_{y_1}$</td>
<td>$A_{y_1}^2$</td>
<td>$b_{cp}t_{cp}^3/12$</td>
</tr>
<tr>
<td><strong>Sums</strong></td>
<td>$\sum A$</td>
<td>$\sum (A_{y_1})$</td>
<td>$\sum (A_{y_1}^2)$</td>
<td>$\sum I_O$</td>
<td></td>
</tr>
</tbody>
</table>
Chapter 2 - Design Prerequisites

The area of the steel section (including the cover plate if it exists), \( A_{\text{bare}} \), is given by the following equation

\[
A_{\text{bare}} = \sum A.
\]

The ENA of the steel section is located a distance \( y_{\text{bare}} \) from the bottom of the bottom flange of the steel beam section (not bottom of cover plate) where \( y_{\text{bare}} \) is determined from the following equation

\[
y_{\text{bare}} = \frac{\sum (A_{1} y_{1})}{\sum A}.
\]

The moment of inertia of the steel section (plus cover plate, if one exists) about its ENA, \( I_{\text{bare}} \), is given by the following equation

\[
I_{\text{bare}} = \sum A_{1} y_{1}^{2} + \sum I_{O} - \left( \sum A \right) y_{\text{bare}}^{2}.
\]

The following notations are used in the preceding Tables 2-3 and 2-4 and the preceding equations:

- \( A_{\text{bare}} \) = Area of the steel beam (plus cover plate, if one exists), in\(^2\).
- \( A_{s} \) = Area of the rolled steel section alone (without the cover plate even if one exists), mm\(^2\).
- \( I_{\text{bare}} \) = Moment of inertia of the steel beam (plus cover plate if one exists), mm\(^4\).
- \( I_{O} \) = The moment of inertia of an element of the beam section taken about the ENA of the element, mm\(^4\).
- \( I_{s} \) = Moment of inertia of the steel beam alone (without the cover plate even if one exists), mm\(^4\).
- \( b_{cp} \) = Width of the steel cover plate, mm.
- \( b_{\text{bot}} \) = Width of the bottom flange of a user defined steel beam, mm.
- \( b_{\text{top}} \) = Width of the top flange of a user defined steel beam, mm.
2.19.3 Properties of the Composite Section

The first step, and potentially most calculation-intensive step in the process of determining the composite properties is to calculate the distance from the ENA
of the steel beam (plus cover plate if it exists) to the ENA of the full composite section. This distance is designated \( y_e \) in Figure 2-26.

Recall that for the calculation of transformed section properties to be used for deflection calculations, concrete in tension is ignored while it is assumed effective in both tension and compression for vibration calculations. Because of the possibility that some of the concrete may be in tension, and because the amount of concrete that is in tension is initially unknown (if any), the process for calculating the distance \( y_e \) is iterative. After the distance \( y_e \) has been determined, the other calculations to determine the composite properties are relatively straightforward.

The program uses the following method to calculate the properties of the composite section.

The location of the ENA of the composite section, defined by \( y_e \) (see Figure 2-26), is calculated using the following iterative process:

a. The program assumes (guesses) that the ENA of the composite section is within the height of the steel beam and uses the following equation to calculate the distance \( y_e \) that defines the location of the ENA for the composite section. Note that with this assumption, all of the concrete is
above the ENA of the composite section, and thus it is all in compression and can be considered.

\[ y_e = \frac{\sum (A_{\text{element}}d_{\text{element}})}{\sum A_{\text{element}}} \]

where,

- \( A_{\text{element}} \) = Equivalent area of an element in the composite section, ignoring any area of concrete that is in tension, if appropriate, and ignoring any concrete in the metal deck ribs when the metal deck span is perpendicular to the beam span.

For any element from the steel section (flange, fillet, or web), the equivalent area is taken as its own area unmodified. Any element from the concrete parts is adjusted to match the modulus of elasticity by multiplying the area by \( E_c/E_s \), mm\(^2\).

- \( d_{\text{element}} \) = Distance from the ENA of the element considered to the ENA of the steel beam alone (including cover plate, if it exists), mm. Signs are considered for this distance. Elements located below the ENA of the steel beam alone (including cover plate, if it exists) have a negative distance and those above have a positive distance.

If the ENA as calculated is within the height of the steel beam, as assumed, the assumed location of the ENA is correct and the calculation for \( y_e \) is complete.

b. If the calculated ENA is not within the height of the steel beam, as assumed in Step a, the assumed location of the ENA is incorrect and calculation for \( y_e \) continues.

i. Using the incorrect location of the ENA calculated in Step a, the program calculates the location of \( y_e \) again using the preceding equation for \( y_e \).

ii. If the newly calculated location of the ENA is the same as the previously calculated location (Step i), the assumed location of the ENA has been identified and the calculation for \( y_e \) is complete.
iii If the newly calculated location of the ENA is not the same as the previously calculated zone (Step i), the most recent assumed location of the ENA is incorrect and another iteration is made.

iv The program repeats the iterations until the location of the ENA has been determined.

After the location of the ENA is known, the other calculations to determine the composite section moment of inertia are non-iterative and relatively straightforward. The other calculation steps are as follow.

1. Calculate the transformed section properties for full composite connection as illustrated in Table 2-5.

<table>
<thead>
<tr>
<th>Item</th>
<th>Transformed Area, $A_r$</th>
<th>$y_1$</th>
<th>$A_r y_1$</th>
<th>$A_r y_1^2$</th>
<th>$I_O$</th>
</tr>
</thead>
<tbody>
<tr>
<td>Concrete slab, left side</td>
<td>$b_{eff} t c E_c$</td>
<td>$d + h_r + t_c - \frac{t_r}{2}$</td>
<td>$A_{cr} y_1$</td>
<td>$A_{cr} y_1^2$</td>
<td>$b_{eff} E_c t_r^2$</td>
</tr>
<tr>
<td>Concrete slab, right side</td>
<td>$b_{eff} t c E_c$</td>
<td>$d + h_r + t_c - \frac{t_r}{2}$</td>
<td>$A_{cr} y_1$</td>
<td>$A_{cr} y_1^2$</td>
<td>$b_{eff} E_c t_r^2$</td>
</tr>
<tr>
<td>Concrete in metal deck ribs, left side</td>
<td>$b_{eff} h_r w_r E_c$</td>
<td>$d + h_r - \frac{h_r}{2}$</td>
<td>$A_{cr} y_1$</td>
<td>$A_{cr} y_1^2$</td>
<td>$b_{eff} w_r E_c h_r^3$</td>
</tr>
<tr>
<td>Concrete in metal deck ribs, right side</td>
<td>$b_{eff} h_r w_r E_c$</td>
<td>$d + h_r - \frac{h_r}{2}$</td>
<td>$A_{cr} y_1$</td>
<td>$A_{cr} y_1^2$</td>
<td>$b_{eff} w_r E_c h_r^3$</td>
</tr>
<tr>
<td>Steel beam plus cover plate</td>
<td>$A_{bare}$</td>
<td>$y_{bare}$</td>
<td>$A_{o} y_1$</td>
<td>$A_{o} y_1^2$</td>
<td>$I_{o}$</td>
</tr>
</tbody>
</table>

When reviewing this table, note the following:

a. If the deck spans perpendicular to the beam span, the concrete in the metal deck ribs is ignored. If the deck spans parallel to the beam span, the concrete in the metal deck ribs is considered.

b. The cover plate may or may not be present.

c. The concrete slab and metal deck may not exist on one side of the beam or the other.
d. The top of the concrete slab may be at a different elevation on the two sides of the beam.

e. The appropriate modulus of elasticity of concrete, \( E_c \), should be used. For vibration, \( E_c \) is increased by an enhanced factor.

f. Concrete is considered effective for compression and considered ineffective for tension, while \( I_{tr} \) is calculated for deflection calculations. While \( I_{tr} \) is calculated for vibration, concrete is considered effective for both compression and tension.

Following is a list of the variables introduced in Table 2-5 that have not been mentioned previously in this section.

\[ A_{tr} = \text{Equivalent area of an element of the composite steel beam section, in}^2. \]

\[ h_r^* = \text{Height of the metal deck ribs above the ENA used for calculating the transformed section properties, mm. Note that this could be different on the left and right sides of the beam.} \]

If the deck ribs are oriented perpendicular to the beam span, \( h_r^* = 0 \).

If the deck ribs are oriented parallel to the beam span, one of the following four items applies:

1. If concrete is not needed to be ignored in tension, for example for calculation of \( I_{tr} \) for vibration, \( h_r^* \) is independent of the location of the ENA. In that case, it is taken as the full depth of the rib, \( h_r^* = h_r. \)

2. If the ENA is below the metal deck, \( h_r^* = h_r. \)

3. If the ENA is within the metal deck, \( h_r^* \) equals the height of the metal deck above the ENA.

4. If the ENA is above the metal deck, \( h_r^* = 0. \)

\[ t_c^* = \text{Thickness of the concrete slab above the metal deck (or solid slab) that lies above the ENA that is used for calculating the transformed section properties, mm. Note that this could be different on the left and right sides of the beam. One of the following four items applies:} \]
1. If concrete is not needed to be ignored in tension, for example for calculation of $I_r$ for vibration, $t^*_c$ is independent of the location of the ENA. In that case, it is taken as the full thickness of the slab, $t^*_c = t_c$.

2. If the ENA is below the top of the metal deck (bottom of the concrete slab), $t^*_c = t_c$.

3. If the ENA is within the concrete slab, $t^*_c$ equals the height of the concrete slab above the ENA.

4. If the ENA is above the concrete slab, $t^*_c = 0$

$A_{bare} =$ Area of the steel beam (plus cover plate), mm$^2$. This area does not include the concrete area.

$E_c =$ Modulus of elasticity of concrete slab, MPa. Note that this could be different on the left and right sides of the beam.

$E_s =$ Modulus of elasticity of steel, MPa.

$S_r =$ Center-to-center spacing of metal deck ribs, mm. Note that this may be different on the left and right sides of the beam.

$b_{eff} =$ Effective width of the concrete flange of the composite beam, mm. This width is code dependent. Note that this width may be different on the left and right sides of the beam. See the section entitled Effective Width of the Concrete Slab for additional information.

$d =$ Depth of the steel beam from the outside face of the top flange to the outside face of bottom flange, mm.

$h_r =$ Height of the metal deck rib, mm. Note that this may be different on the left and right sides of the beam.

$t_c =$ Thickness of the concrete slab, mm. If there is metal deck, this is the thickness of the concrete slab above the metal deck. Note that this may be different on the left and right sides of the beam.

$w_r =$ Average width of a metal deck rib, mm. Note that this may be different on the left and right sides of the beam.
$y_{bare} = \text{Distance from the bottom of the bottom flange of the steel beam to the ENA of the steel beam (plus cover plate, if it exists) alone, mm.}$

$y_e = \text{The distance from the ENA of the steel beam (plus cover plate, if it exists) alone to the ENA of the fully composite beam, mm.}$

$z = \text{Distance from the ENA of the steel beam (plus cover plate, if it exists) alone to the top of the concrete slab, mm. Note that this distance may be different on the left and right sides of the beam.}$

$\Sigma A_{tr} = \text{Sum of the areas of all of the elements of the composite steel beam section, mm}^2.$

$\Sigma (A_{tr}y_1) = \text{Sum of the product } A_{tr} \text{ times } y_1 \text{ for all of the elements of the composite steel beam section, mm}^3.$

$\Sigma (A_{tr}y_1^2) = \text{Sum of the product } A_{tr} \text{ times } y_1^2 \text{ for all of the elements of the composite steel beam section, mm}^4.$

The neutral axis of the transformed composite section is located a distance $\overline{y}$ from the bottom of the bottom flange of the steel beam section (not bottom of cover plate). The distance $\overline{y}$ can be determined from either of the following equations. They both give the same result.

$$\overline{y} = \frac{\Sigma (A_{tr}y_1)}{\Sigma A_{tr}}$$

$$\overline{y} = y_{bare} + y_e$$

The distance $\overline{y}$ is illustrated in Figure 2-27.
The transformed section moment of inertia about the ENA of the composite beam, \( I_{tr} \), is calculated using the following equation.

\[
I_{tr} = \sum A_y y_i^2 + \sum I_o - \left( \sum A_y \right) \bar{y}^2
\]

Figure 2-27 illustrates the axis about which \( I_{tr} \) is taken.

2.20 Effective Moment of Inertia for Partial Composite Connection

When there is partial composite connection, the number of shear connectors provided controls the amount of horizontal shear that can be transferred between the steel beam and the concrete slab. The effective moment of inertia of the composite section for positive bending in a partially composite beam is calculated in accordance with Clauses 17.3.1(a) and (b) as follows:

\[
I_{eff} = I_{bare} + 0.85 \cdot PCC^{0.25} \cdot \left( I_{tr} - I_{bare} \right) / Creep Factor
\]

where:

\( PCC = \) Percent composite connection, unitless. The percentage varies between 25% and 100% inclusive.
\( I_{\text{bare}} = \) Moment of inertia of the steel beam alone plus cover plate, if it exists, mm\(^4\).

\( I_{\text{eff}} = \) Effective moment of inertia of a partially composite beam, mm\(^4\).

\( I_{tr} = \) Transformed section moment of inertia about ENA of the composite beam calculated as described in the section entitled Transformed Section Moment of Inertia, mm\(^4\).

Creep Factor = 1.15 per 17.1.3(b) or its user specified value in the preferences.

### 2.21 Composite Plastic Moment Capacity for Positive Bending

This section describes how the positive moment capacity of the composite beam using plastic stress distribution is calculated. It normally covers the plastic moment capacity for full composite connection. The minor modification that is needed for partial composite connection also is discussed.

Figure 2-30 illustrates a generic plastic stress distribution for positive bending.

![Figure 2-28 Generic Plastic Stress Distribution for Positive Bending](image)

Note that the concrete is stressed to \(\alpha f'_c\) and the steel is stressed to \(F_y\) (AISC II.2a). The distance \(y_p\) is measured from the bottom of the beam bottom flange (not cover plate) to the plastic neutral axis (PNA). The distance \(z_p\) is measured from the top of the concrete slab to the PNA; it can be different on the two
sides of the beam as described later. The illustrated plastic stress distribution is the basic distribution of stress used by the program when considering a plastic stress distribution for positive bending. Note that if the metal deck ribs are parallel to the beam, the concrete in the ribs is also considered.

Figure 2-31 illustrates how the program idealizes a steel beam for calculating the plastic stress distribution.
Figure 2-29 Idealization of a Rolled Section and a User-Defined Section Used for Calculating the Plastic Stress Distribution
Two different cases are shown, one for a rolled section and the other for a user defined section. The idealization for the rolled section considers the fillets whereas the idealization for the user defined section assumes there are no fillets because none are specified in the section definition. Although not shown in those figures, the deck type and orientation may be different on the left and right sides of the beam as shown in Figure 2-3 of the section entitled *Effective Width of the Concrete Slab* in this chapter.

For a rolled steel section, the fillets are idealized as a rectangular block of steel. The depth of this rectangular block, \( k_{\text{depth}} \), is:

\[
k_{\text{depth}} = k - tf.
\]

The width of this rectangular block, \( k_{\text{width}} \), is:

\[
k_{\text{width}} = \frac{[A_s - 2btf - (d - 2k)tw]}{2k_{\text{depth}}}.
\]

The basic steps in computing the positive plastic moment capacity are as follows:

- Determine the location of the PNA using the subsection *Location of the Plastic Neutral Axis*.

- Calculate the plastic moment capacity of the composite section using the equation given in subsection *Plastic Moment Capacity for Positive Bending* together with the appropriate equation depending on the location of the PNA. Note that for user defined sections, the terms related to the top and bottom fillets are ignored.

### 2.21.1 Location of the Plastic Neutral Axis

The program determines the location of the PNA by comparing the maximum possible compressive force that can be developed in the concrete, \( MPF_{\text{conc}} \), with the maximum possible tensile force that can be developed in the steel section (including the cover plate, if applicable), \( MPF_{\text{steel}} \).

The maximum concrete force, \( MPF_{\text{conc}} \), is calculated as follows if there is no metal deck, or if the metal deck ribs are oriented perpendicular to the beam span.
If the deck ribs are oriented parallel to the beam span, $MPF_{\text{conc}}$ is calculated as follows:

$$MPF_{\text{conc}} = \phi_{\text{bcc}} \left[ \left( \alpha_i f'_c b_{\text{eff}} t_c \right)_{\text{left}} + \left( \alpha_i f'_c b_{\text{eff}} t_c \right)_{\text{right}} \right].$$

Note that the maximum concrete force has contributions from the left and right sides of the beam that are treated separately and may be different.

The maximum steel force, $MPF_{\text{steel}}$, is calculated as follows if the beam is a rolled section:

$$MPF_{\text{steel}} = \phi_{\text{bcs}} \left( A_{\text{f}} F_y + b_{\text{c}} t_{\text{c}} F_{\text{scp}} \right).$$

$MPF_{\text{steel}}$, is calculated as follows if the beam is a userdefined section

$$MPF_{\text{steel}} = \phi_{\text{bcs}} \left( b_{\text{f-top}} F_{\text{sf-top}} h + b_{\text{f-bot}} F_{\text{sf-bot}} h + b_{\text{c}} t_{\text{c}} F_{\text{scp}} \right).$$

Note that $\phi_{\text{bcc}}$ and $\phi_{\text{bcs}}$ are resistance factors defined by CSI, not in any conventional code. They are provided to give the user more control over section capacity, if desired or needed. They essentially allow different resistance factors for steel and concrete. Note the $\phi_{\text{bcc}}$ factor is applied to the reinforcing steel in the concrete slab (if this steel is considered). By default, both of those resistance factors are set equal to 1.0.

When computing the location of the PNA, it is important to remember that the concrete is assumed to take no tension. Also, the concrete in the metal deck ribs is considered effective in compression only if the metal deck ribs are oriented parallel to the beam span.

The maximum concrete and steel forces are compared to determine whether the PNA is within the concrete slab or the steel section. If $MPF_{\text{conc}}>MPF_{\text{steel}}$, the PNA is within the concrete slab. If $MPF_{\text{steel}}>MPF_{\text{conc}}$, the PNA is within the steel section. If $MPF_{\text{steel}} = MPF_{\text{conc}}$, the PNA is at the top of the steel beam.

If the PNA is within the slab, the fact that the concrete slab can be different on each side of the beam complicates locating the PNA. If the PNA is within the
steel section, there are several general locations for it. After the general locations have been identified, it is a straightforward process to determine the location of the PNA. The general locations are:

- Within the beam top flange.
- Within the beam top fillet (applies to rolled shapes from the program's section database only).
- Within the beam web.
- Within the beam bottom fillet (applies to rolled shapes from the program's section database only).
- Within the beam bottom flange.
- Within the cover plate (if one is specified).

Note it is very unlikely that the PNA would be below the beam web but there is nothing in the program to prevent it. This condition would require a very large beam bottom flange and/or cover plate. Each of the PNA locations in the steel section is described following the description of the PNA in the concrete slab.

2.21.1.1 PNA in the Concrete Slab Above the Steel Beam

The program considers the condition where the slab on the left and right sides of the beam are different. When the program determines that the PNA is above the top of the steel section, that is, when $MPF_{\text{conc}} > MPF_{\text{steel}}$, it puts the following four items in order, from highest elevation to lowest:

- Top of concrete slab on the left side of the beam.
- Top of concrete slab on the right side of the beam.
- Top of metal deck on the left side of the beam.
- Top of metal deck on the right side of the beam.

Next the program adds the compressive forces of those four items, starting with the item at the highest elevation and proceeding downward. As each item is added into the sum, the sum of compressive forces is compared with the maximum tension value, which is the sum of $MPF_{\text{steel}}$. As soon as the sum of forces exceeds $MPF_{\text{steel}}$, the program recognizes that the last location considered is below the PNA, and the second to last location considered is
above the PNA. Using this information, the program can solve directly for the location of the PNA.

Figures 2-32 and 2-33 show the internal forces for a rolled steel section and a user defined steel section, respectively, for the condition where the PNA is in the concrete slab above the metal deck.

Figure 2-30 Rolled Steel Section
With PNA in the Concrete Slab Above the Metal Deck, Positive Bending

Figure 2-31 UserDefined Steel Section
With PNA in the Concrete Slab Above the Metal Deck, Positive Bending

Location of the Plastic Neutral Axis
Figures 2-34 and 2-35 show the internal forces for a rolled steel section and a user defined steel section, respectively, for the condition where the PNA is within the height, $h_r$, of the metal deck ribs.
Note that in Figures 2-32 through 2-35 the concrete compression forces ($C_{c1}$ and $C_{c2}$) may have different magnitudes and locations (elevations) for the left and right sides of the beam.

Also note that the program ignores the rebar area for computing composite moment capacities.

### 2.21.1.2 PNA within the Beam Top Flange

Figures 2-36 and 2-37 show the internal forces for a rolled steel section and a user defined steel section, respectively, for the condition where the PNA is within the beam top flange.

The term $y_2$, which is the distance from the top of the steel beam to the PNA, is shown in these figures and is defined by the following equation:

$$y_2 = \frac{MPF_{steel} - MPF_{conc}}{2\phi_{hes}h_{f, 40p}F_{y, f, top}}$$

Figure 2-34 Rolled Steel Section

*With PNA Within the Beam Top Flange, Positive Bending*
2.21.1.3 PNA within the Beam Top Fillet

The PNA lies within the beam top fillet only if the beam section is a rolled section. Figure 2-38 shows the internal forces for this condition.
The term $y_3$, which is the distance from the bottom side of the beam top flange to the PNA, is shown in Figure 2-38 and is defined by the following equation.

$$
y_3 = \frac{MPF_{\text{steel}} - MPF_{\text{conc}} - 2\phi_{bc}b_{f-top}t_{f-top}F_{yf-top}}{2\phi_{bc}k_{\text{width}}F_{yw}}.
$$

### 2.21.1.4 PNA within the Beam Web

Figures 2-39 and 2-40 show the internal forces for a rolled steel section and a user-defined steel section, respectively, for the condition where the PNA is within the beam web. The term $y_4$, which for a rolled steel beam is the distance from the web toe of the top fillet to the PNA, and for a user-defined beam $y_4$ is the distance from the bottom side of the beam top flange to the PNA, is shown in Figures 2-39 and 2-40, and is defined by the following equation.

$$
y_4 = \frac{MPF_{\text{steel}} - MPF_{\text{conc}} - 2\phi_{bc}b_{f-top}t_{f-top}F_{yf-top}}{2\phi_{bc}k_{\text{t-w}}F_{yw}} - \frac{2\phi_{bc}k_{\text{depth}}F_{yw}}{2\phi_{bc}k_{t-w}F_{yw}}.
$$

The last term applies only to rolled steel beams; it reduces to zero for user-defined beams.

---

*Figure 2-37 Rolled Steel Section With PNA Within the Beam Web, Positive Bending*
2.21.1.5 PNA within the Beam Bottom Fillet

The PNA is within the beam bottom fillet only if the beam section is a rolled section. Figure 2-41 shows the internal forces for this condition. The term $y_5$, which is the distance from the top side of the beam bottom fillet to the PNA, is shown in Figure 2-41 and is defined by the following equation.

$$y_5 = \frac{MPF_{steel} - MPF_{conc} - 2\phi_{bsc}b'_{flap}F_{y'_{flap}}}{2\phi_{bsc}k_{width}F_{yw}} - \frac{2\phi_{bsc}k_{depth}F_{yw}}{2\phi_{bsc}k_{width}F_{yw}} - \frac{2\phi_{bsc}ht_{w}F_{yw}}{2\phi_{bsc}k_{width}F_{yw}}$$

Note that it is unlikely that the PNA will be this low. It requires a very large beam bottom flange and/or cover plate.
2.21.1.6 PNA within the Beam Bottom Flange

Figures 2-42 and 2-43 show the internal forces for a rolled steel section and a user defined steel section, respectively, for the condition where the PNA lies within the beam bottom flange. The term $y_6$, which is the distance from the top of the beam bottom flange to the PNA, is shown in Figures 2-42 and 2-43 and is defined by the following equation.

$$y_6 = \frac{MPF_{steel} - MPF_{conc} - 2\phi_{bcs}}{2\phi_{bcs} b_{f-bot} F_{yf-bot}} - \frac{4\phi_{bcs} k_{depth} F_{yw}}{2\phi_{bcs} b_{f-bot} F_{yf-bot}} - \frac{2\phi_{bcs} h_{web} F_{yw}}{2\phi_{bcs} b_{f-bot} F_{yf-bot}}$$

Note that it is unlikely that the PNA will be this low. It requires a very large beam bottom flange and/or cover plate.
2.21.1.7 PNA within the Cover Plate

Figures 2-44 and 2-45 show the internal forces for a rolled steel section and a user defined steel section, respectively, for the condition where the PNA lies within the cover plate. The term $y_7$, which is the distance from the top of the cover plate to the PNA, is shown in Figures 2-44 and 2-45 and is defined by the following equation.
\[ y_p = \frac{MPF_{steel} - MPF_{concrete} - 2\phi_{lca} h_{f-top} f_{yf} F_{yf-top}}{2\phi_{lca} h_{c-top} F_{ycp}} - \frac{4\phi_{lca} k_{width} k_{depth} F_{yw}}{2\phi_{lca} h_{f-top} F_{ycp}} - \frac{2\phi_{lca} h_{t} F_{yw}}{2\phi_{lca} h_{f-top} F_{ycp}} - \frac{2\phi_{lca} b_{f-top} f_{yf} F_{yf-top}}{2\phi_{lca} b_{c-top} F_{ycp}} \]

\[ \text{Beam Section} \quad \text{Beam Elevation} \quad \text{Beam Internal Forces} \]

\[ \text{Figure 2-42 Rolled Steel Section With PNA Within the Cover Plate, Positive Bending} \]

\[ \text{Beam Section} \quad \text{Beam Elevation} \quad \text{Beam Internal Forces} \]

\[ \text{Figure 2-43 UserDefined Steel Section with PNA Within the Cover Plate, Positive Bending} \]

Note that it is unlikely that the PNA will be this low. It requires an extremely large cover plate. In the event the PNA was in the cover plate, the distance \( y_p \) would become negative.

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2.21.1.8 Calculating the PNA Location

To calculate the location of the PNA for positive bending, the program starts by comparing the value of $MPF_{\text{conc}}$ to that of $MPF_{\text{steel}}$ to determine whether the PNA is in the steel section or in the concrete slab above the steel section. As described in an earlier subsection of this section, if $MPF_{\text{conc}} > MPF_{\text{steel}}$, the PNA is within the concrete slab. If $MPF_{\text{steel}} > MPF_{\text{conc}}$, the PNA is within the steel section. If $MPF_{\text{steel}} = MPF_{\text{conc}}$, the PNA is at the top of the steel beam.

If the PNA is in the concrete slab above the steel section, the procedure described in the previous subsection of this section entitled \textit{PNA in the Concrete Slab Above the Steel Beam} is followed.

If the PNA is within the steel section, the program assumes that the PNA occurs in the top flange of the beam. The distance $y_2$ is calculated as described previously for the PNA within the beam top flange. The calculated distance $y_2$ is then checked to see if it actually is within the beam top flange. If it is, the location of the PNA has been identified.

If the calculated distance $y_2$ is not within the beam top flange, the program continues by assuming that the PNA occurs in the beam top fillet. (Note that if the beam is a user defined beam, there is no top fillet and the program skips directly to assuming that the PNA is in the beam web.) The distance $y_3$ is calculated as described previously for PNA within the beam top fillet. The calculated distance $y_3$ is then checked to see if it actually is within the beam top fillet. If it is, the location of the PNA has been identified.

If the calculated distance $y_3$ is not within the beam top fillet, the program continues by assuming that the PNA occurs in the beam web. The distance $y_4$ is calculated as described previously for the PNA within the beam top fillet. The calculated distance $y_4$ is then checked to see if it actually is within the beam web. If it is, the location of the PNA has been identified.

In any practical case, the PNA is not expected to be below the beam web. However, in the event the PNA has not yet been located, the program continues down the beam section through the bottom fillet, the bottom flange, and finally the cover plate until the location of the PNA has been identified.
2.21.2 Plastic Moment Capacity for Positive Bending

The plastic moment capacity for positive bending in a composite section is calculated from the following equation:

\[
\phi_{bcpp} M_n = \phi_{bcpp} \sum_{\text{Piece}=1}^{10} T_{\text{Piece}} x_{\text{PNA-piece}} + \phi_{bcpp} \sum_{\text{Piece}=1}^{10} C_{\text{Piece}} x_{\text{PNA-piece}}
\]

where:

- \( C_{\text{Piece}} \) = Compression force in a piece of the composite beam, N.
- \( M_n \) = Plastic moment capacity for positive bending, N-mm.
- \( T_{\text{Piece}} \) = Tension force in a piece of the composite beam, N.
- \( x_{\text{PNA-piece}} \) = Distance from centroid of tension or compression force in a piece of a composite beam to the PNA, mm.
- \( \phi_{bcpp} \) = Resistance factor for positive bending when plastic stress distribution is assumed, unitless.

In the preceding equation, the values used for \( T_{\text{Piece}}, C_{\text{Piece}} \) and \( x_{\text{PNA-piece}} \) can assume the tension and compression values of ten constituent pieces of the composite section, and their respective centroidal distances from the PNA. The constituents parts are concrete above the metal deck on the left and right, concrete within the metal deck as ribs at the left and right, the beam top flange, the beam top fillet (of rolled shapes only), the beam web, the beam bottom fillet (of rolled shapes only), the beam bottom flange, and the cover plate. Note that the program ignores reinforcing bars in concrete. The corresponding compression forces are \( C_{C1}, C_{C2}, C_{FT}, C_{KT}, C_{Web}, C_{KB}, C_{FB}, \) and \( C_{cp} \). The corresponding tensile forces are \( T_{C1}, T_{C2}, T_{FT}, T_{KT}, T_{Web}, T_{KB}, T_{FB}, \) and \( T_{cp} \). (Please refer to Figures 2-32 to 2-45 for graphical representations of these forces.) Note that based on the assumption that concrete cannot take tension, \( T_{C1} \) and \( T_{C2} \) are always zero. For any piece from the steel shape, if \( C \) for a piece exists, \( T \) for that piece is zero unless the PNA falls within that piece.

Depending on the location of the PNA, the compression and tension forces and their corresponding \( x_{\text{PNA}} \) for all constituent pieces of the composite section are given as follows:
Concrete above the metal deck on the left side of the beam: The concrete can carry a compression force only; tension is not allowed in the concrete. The following equations are used for the compression force in the concrete above the metal deck.

\[
C_{b1} = \phi_{b1c} \alpha_1 f'_c b_{eff} z_p, \quad \text{if the PNA is above the metal deck,}
\]
\[
C_{c1} = \phi_{b1c} \alpha_1 f'_c b_{eff} t_c, \quad \text{if the PNA is below the solid slab.}
\]

The following equations are used for the distance from the center of the force in the concrete above the metal deck to the PNA.

\[
x_{PNA} = \frac{z_p}{2}, \quad \text{if the PNA is above the metal deck,}
\]
\[
x_{PNA} = z_p - \frac{t_c}{2}, \quad \text{if the PNA is below the solid slab.}
\]

For partial composite connection, the PNA is always in the depth of the steel shape. In that case, the \( C_{c1} \) is determined based on the depth of the effective slab thickness as described in the subsection entitled Location of Plastic Neutral Axis of the section Composite Moment Capacities of a Partially Composite Beam with a Plastic Stress Distribution. If the bottom of the effective concrete in the concrete slab is above the metal deck, \( C_{c1} \) is based on the effective depth \( a_1 \), else it is based on total thickness.

\[
C_{c1} = \phi_{b1c} \alpha_1 f'_c b_{eff} a_1, \quad \text{if the effective line is above the metal deck, } a_1 < t_c
\]
\[
C_{c1} = \phi_{b1c} \alpha_1 f'_c b_{eff} t_c, \quad \text{if the effective line is below the solid slab.}
\]

For partial composite connection, the following equations are used for the distance from the center of the force in the concrete slab above the metal deck to the PNA.

\[
x_{PNA} = z_p - \frac{a_1}{2}, \quad \text{if effective line is above the metal deck, } a_1 < t_c,
\]
\[
x_{PNA} = z_p - \frac{t_c}{2}, \quad \text{if effective line is below the solid slab.}
\]

Note that the terms \( z_p, t_c, \) and \( h_c \) in the preceding equations must be for the left side of the beam.
Concrete above the metal deck on the right side of the beam: The concrete can carry a compression force only; tension is not allowed in the concrete. The following equations are used for the compression force in the concrete above the metal deck. Note that these equations are applied to each side of the beam separately.

\[
C_{c1} = \phi_{bce} \alpha f' c b_{eff} z_p, \quad \text{if the PNA is above the metal deck,}
\]

\[
C_{c1} = \phi_{bce} \alpha f' c b_{eff} t_c, \quad \text{if the PNA is below the solid slab.}
\]

The following equations are used for the distance from the center of the force in the concrete above the metal deck to the PNA.

\[
x_{PNA} = \frac{z_p}{2}, \quad \text{if the PNA is above the metal deck,}
\]

\[
x_{PNA} = z_p - \frac{t_c}{2}, \quad \text{if the PNA is below the solid slab.}
\]

For partial composite connection, the PNA is always in the depth of the steel shape. In that case, \(C_{c1}\) is determined based on the depth of the effective slab thickness as described in the subsection entitled Location of Plastic Neutral Axis of the section Composite Moment Capacities of a Partially Composite Beam with a Plastic Stress Distribution. If the bottom of the effective concrete in the concrete slab is above the metal deck, \(C_{c1}\) is based on the effective depth \(a_i\); else it is based on total thickness.

\[
C_{c1} = \phi_{bce} \alpha f' c b_{eff} a_i, \quad \text{if the effective line is above the metal deck, } a_i < t_c,
\]

\[
C_{c1} = \phi_{bce} \alpha f' c b_{eff} t_c, \quad \text{if the effective line is below the solid slab.}
\]

For partial composite connection, the following equations are used for the distance from the center of the force in the concrete slab above the metal deck to the PNA.

\[
x_{PNA} = z_p - \frac{a_i}{2}, \quad \text{if effective line is above the metal deck, } a_i < t_c,
\]

\[
x_{PNA} = z_p - \frac{t_c}{2}, \quad \text{if effective line is below the solid slab.}
\]
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Note that the terms $z_p$, $t_e$, and $h_r$ in the preceding equations must be for the right side of the beam.

- **Concrete within height of metal deck on the left side of the beam:** The concrete can carry a compression force only; tension is not allowed in the concrete. The following two equations are used for the compression force in the concrete within the metal deck. Also note that these equations apply only if the span of the metal deck ribs is oriented parallel to the beam span. If the metal deck ribs are oriented perpendicular to the beam span, there is no compression force allowed on the concrete within the metal deck ribs.

\[
C_{c2} = \phi_{bce} \alpha_1 f'c b_{eff} \frac{w_t (z_p - t_e)}{S_r}, \quad \text{if the PNA is within the metal deck ribs,}
\]
\[
C_{c2} = \phi_{bce} \alpha_1 f'c b_{eff} \frac{w_t h_r}{S_r}, \quad \text{if the PNA is below the metal deck ribs.}
\]

The following equations are used for the distance from the center of the force in the concrete within the metal deck ribs to the PNA.

\[
x_{PNA} = \frac{z_p - t_e}{2}, \quad \text{if the PNA is within the metal deck ribs,}
\]
\[
x_{PNA} = z_p - t_e - \frac{h_r}{2}, \quad \text{if the PNA is below the metal deck rib.}
\]

For partial composite connection, the PNA is always in the depth of the steel shape. In that case, $C_{c2}$ is determined based on the depth of the effective slab thickness as described in the subsection entitled *Location of Plastic Neutral Axis* of the section *Composite Beam with a Plastic Stress Distribution*. If the bottom of the effective concrete in the concrete slab is within the metal deck, $C_{c2}$ is based on the effective depth $a_2$; else it is based on the total rib depth.

\[
C_{c2} = \phi_{bce} \alpha_1 f'c b_{eff} \frac{w_t a_2}{S_2}, \quad \text{if the effective line is within the metal deck rib,}
\]
\[
C_{c2} = \phi_{bce} \alpha_1 f'c b_{eff} \frac{w_t h_r}{S_2}, \quad \text{if the effective line is below the metal deck rib.}
\]
For partial composite connection, the following equations are used for the distance from the center of the force in the concrete deck rib above the effective line.

\[ x_{PNA} = z_p - \frac{t_c}{2} - \frac{a_2}{2}, \quad \text{if the effective line is within the metal deck ribs,} \]

\[ x_{PNA} = z_p - \frac{t_c}{2} - \frac{h_r}{2}, \quad \text{if the effective line is below the metal deck rib.} \]

Note that the terms \( z_p, t_c, \) and \( h_r \) in the preceding equations must be for the left side of the beam.

- **Concrete within height of metal deck on the right side of the beam:** The concrete can carry a compression force only; tension is not allowed in the concrete. The following two equations are used for the compression force in the concrete within the metal deck. Also note that these equations apply only if the span of the metal deck ribs is oriented parallel to the beam span. If the metal deck ribs are oriented perpendicular to the beam span, there is no compression force allowed on the concrete within the metal deck ribs.

\[ C_{C2} = \phi_{bec} \alpha f'_c b_{eff} \frac{w_e (z_p - t_c)}{S_r}, \quad \text{if the PNA is within the metal deck ribs,} \]

\[ C_{C2} = \phi_{bec} \alpha f'_c b_{eff} w_e h_r, \quad \text{if the PNA is below the metal deck ribs.} \]

The following equations are used for the distance from the center of the force in the concrete within the metal deck ribs to the PNA.

\[ x_{PNA} = z_p - \frac{t_c}{2}, \quad \text{if PNA is within the metal deck ribs,} \]

\[ x_{PNA} = z_p - t_c - \frac{h_r}{2}, \quad \text{if PNA is below the metal deck rib.} \]

For partial composite connection, the PNA is always in the depth of the steel shape. In that case, \( C_{C2} \) is determined based on the depth of the effective slab thickness as described in the subsection entitled *Location of Plastic Neutral Axis* of the section *Composite Beam with a Plastic Stress Distribution*. If the bottom of the effective concrete in the concrete slab is within the metal deck, \( C_{C2} \) is based on the effective depth \( a_2 \); else it is based on the total rib depth.
$C_{c2} = \phi_{nc} \alpha_{f_c} f'_{c,eff} \frac{w_i a_i}{S_2}$, if the effective line is within the metal deck rib,

$C_{c2} = \phi_{nc} \alpha_{f_c} f'_{c,eff} \frac{h_i}{S_2}$, if the effective line is below the metal deck rib.

For partial composite connection, the following equations are used for the distance from the center of the force in the concrete deck rib above the effective line.

$x_{PNA} = z_p - \frac{t}{2} - \frac{a_i}{2}$, if the effective line is within the metal deck rib,

$x_{PNA} = z_p - \frac{t}{2} - \frac{h_i}{2}$, if the effective line is below the metal deck rib.

Note that the terms $z_p$, $t$, and $h_i$ in the preceding equations must be for the right side of the beam.

- **Beam top flange**: The force in the beam top flange can be tension, compression, or compression in the upper portion of the flange and tension in the lower portion. The following equations are used for the tension and compression forces in the beam top flange.

$T_{FT} = \phi_{bc} b_{f,ap} t_{f,ap} y_{f,ap}$, if the PNA is above the top of the top flange,

$T_{FT} = \phi_{bc} b_{f,ap} \left( t_{f,ap} - y_{2} \right) F_{f,ap}$, if the PNA is within the top flange,

$T_{FT} = 0$, if the PNA is below the bottom of the top flange,

$C_{FT} = 0$, if the PNA is above the top of the top flange,

$C_{FT} = \phi_{bc} b_{f,ap} y_{2} F_{f,ap}$, if the PNA is within the top flange,

$C_{FT} = \phi_{bc} b_{f,ap} t_{f,ap} F_{f,ap}$, if the PNA is below the bottom of the top flange.

The distance of tension force, $T_{FT}$, in the top flange to the PNA is given by the following equations.

$x_{PNA} = y_{p} - d + \frac{t_{f,ap}}{2}$, if the PNA is above the top of the top flange,

$x_{PNA} = \frac{t_{f,ap} - y_{2}}{2}$, if the PNA is within the top flange,

$x_{PNA} = 0$, if the PNA is below the bottom of the top flange.
The distance of compression force, \( C_{FT} \), in the top flange to the PNA is given by the following equations.

\[
x_{PNA} = \begin{cases} 
0, & \text{if the PNA is above the top of the top flange}, \\
\frac{V_2}{2}, & \text{if the PNA is within the top flange}, \\
Z_p - t_f - h_r - \frac{t_{f, top}}{2}, & \text{if the PNA is below the bottom of the top flange}.
\end{cases}
\]

Note the terms \( Z_p, t_f, \) and \( h_r \) in the preceding equations must all be for the left side of the beam or all for the right side of the beam. It does not matter which side of the beam is used, but all of the terms must be consistent.

- **Beam top fillet**: The force in the beam top fillet can be tension, compression, or compression in the upper portion of the fillet and tension in the lower portion. The following equations are used for the tension and compression forces in the beam top fillet. Note that these equations do not apply to user-defined sections.

\[
T_{KT} = \phi_{kr} k_{width} k_{depth} F_{yw},
\]

\[
T_{KT} = \phi_{kr} k_{width} (k_{depth} - y_3) F_{yw},
\]

\[
T_{KT} = 0,
\]

\[
C_{KT} = 0,
\]

\[
C_{KT} = \phi_{kr} k_{width} y_3 F_{yw},
\]

\[
C_{KT} = \phi_{kr} k_{width} k_{depth} F_{yw},
\]

The distance of the tension force in the top fillet, \( T_{KT} \), to the PNA is given by the following equations.

\[
x_{PNA} = y_p - d + t_{f, top} + \frac{k_{depth}}{2}, \quad \text{if the PNA is above the top of the top flange},
\]

\[
x_{PNA} = \frac{k_{depth} - y_3}{2}, \quad \text{if the PNA is within the top flillet},
\]

\[
x_{PNA} = 0, \quad \text{if the PNA is below the bottom of the top fillet}.
\]

The distance of the compression force in the top fillet, \( C_{KT} \), to the PNA is given by the following equations.
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\[ x_{PNA} = 0, \quad \text{if the PNA is above the top of the top fillet}, \]

\[ x_{PNA} = \frac{y_f}{2}, \quad \text{if the PNA is with the top fillet}, \]

\[ x_{PNA} = z_p - t_s - h_s - r_{f, top} - \frac{k_{depth}}{2}, \quad \text{if the PNA is below the bottom of the top fillet}. \]

Note the terms \( z_p, t_s, \) and \( h_s \) in the preceding equation must all be for the left side of the beam or all for the right side of the beam. It does not matter which side of the beam is used, but all of the terms must be consistent.

**Beam web:** The force in the beam web can be tension, compression, or compression in the upper portion of the web and tension in the lower portion. The following equations are used for the tension and compression forces in the beam web.

\[ T_{Web} = \phi_{kc} t_w h F_{yw}, \quad \text{if the PNA is above the top of the web}, \]

\[ T_{Web} = \phi_{kc} t_w (h - y_f) F_{yw}, \quad \text{if the PNA is within the web}, \]

\[ T_{Web} = 0, \quad \text{if the PNA is below the bottom of the web}, \]

\[ C_{Web} = 0, \quad \text{if the PNA is above the top of the web}, \]

\[ C_{Web} = \phi_{kc} t_w y_f F_{yw}, \quad \text{if the PNA is within the web}, \]

\[ C_{Web} = \phi_{kc} t_w h F_{yw}, \quad \text{if the PNA is below the bottom of the web}. \]

The distance of the tension force in the web, \( T_{Web} \), to the PNA is given by the following equations.

\[ x_{PNA} = y_p - d + t_{f, top} + k_{depth} + \frac{h}{2}, \quad \text{if the PNA is above the top of the web}, \]

\[ x_{PNA} = \frac{h - y_f}{2}, \quad \text{if the PNA is within the web}, \]

\[ x_{PNA} = 0, \quad \text{if the PNA is below the bottom of the web}. \]

The distance of the compression force in the web, \( C_{Web} \), to the PNA is given by the following equations.
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\[ x_{\text{PNA}} = 0, \quad \text{if the PNA is above the top of the web,} \]
\[ x_{\text{PNA}} = \frac{y_A}{2}, \quad \text{if the PNA is within the web,} \]
\[ x_{\text{PNA}} = z_p - t_c - h_y - t_f, - k_{\text{depth}} - \frac{h}{2}, \quad \text{if the PNA is below the bottom of the web.} \]

Note the terms \( z_p, t_c, \) and \( h_r \) in the preceding equation must all be for the left side of the beam or all for the right side of the beam. It does not matter which side of the beam is used, but all of the terms must be consistent.

- **Beam bottom fillet:** The force in the beam bottom fillet can be tension, compression, or compression in the upper portion of the fillet and tension in the lower portion. The following equations are used for the tension and compression forces in the beam bottom fillet. Note that these equations do not apply to user defined sections.

\[ T_{KB} = \phi_{HC} k_{\text{width}} k_{\text{depth}} F_{yw}, \quad \text{if the PNA is above the top of the bottom fillet,} \]
\[ T_{KB} = \phi_{HC} k_{\text{width}} (k_{\text{depth}} - y_A) F_{yw}, \quad \text{if the PNA is within the bottom fillet,} \]
\[ T_{KB} = 0, \quad \text{if the PNA is below the bottom fillet,} \]
\[ C_{KB} = 0, \quad \text{if the PNA is above the top of the bottom fillet,} \]
\[ C_{KB} = \phi_{HC} k_{\text{width}} y_A F_{yw}, \quad \text{if the PNA is within the bottom fillet,} \]
\[ C_{KB} = 0, \quad \text{if the PNA is below the bottom fillet.} \]

The distance of the tension force, \( T_{KB} \), to the PNA is given by the following equations.

\[ x_{\text{PNA}} = y_p - d + t_f - \frac{3k_{\text{depth}}}{2} + h, \quad \text{if the PNA is above the top of the bottom fillet,} \]
\[ x_{\text{PNA}} = \frac{k_{\text{depth}} - y_A}{2}, \quad \text{if the PNA is within the bottom fillet,} \]
\[ x_{\text{PNA}} = 0, \quad \text{if the PNA is below the bottom fillet.} \]

The distance of the compression force, \( C_{KB} \), to the PNA is given by the following equations.

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\[ x_{PNA} = 0, \quad \text{if the PNA is above the top of the bottom fillet,} \]
\[ x_{PNA} = \frac{y_z}{2}, \quad \text{if the PNA is within the bottom fillet,} \]
\[ x_{PNA} = z_p - t_c - h_r - r_d - t_{f-up} - \frac{3k_{depth}}{2} - h, \quad \text{if the PNA is below the bottom fillet.} \]

Note the terms \( z_p, t_c, \) and \( h_r \) in the preceding equation must all be for the left side of the beam or all for the right side of the beam. It does not matter which side of the beam is used, but all of the terms must be consistent.

**Beam bottom flange:** The force in the beam bottom flange can be tension, compression, or compression in the upper portion of the flange and tension in the lower portion. The following equations are used for the tension and compression forces in the beam bottom flange.

\[
T_{FB} = \phi_{bc} b_{f-bot} f_{f-bot} F_{yf-bot}, \quad \text{if the PNA is above the top of the bottom flange,} \\
T_{FB} = \phi_{bc} b_{f-bot} \left( f_{f-bot} - y_y \right) F_{yf-bot}, \quad \text{if the PNA is within the bottom flange,} \\
T_{FB} = 0, \quad \text{if the PNA is below the bottom flange,} \\
C_{FB} = 0, \quad \text{if the PNA is above the top of the bottom flange,} \\
C_{FB} = \phi_{bc} b_{f-bot} y_y F_{yf-bot}, \quad \text{if the PNA is within the bottom flange,} \\
C_{FB} = \phi_{bc} b_{f-bot} f_{f-bot} F_{yf-bot}, \quad \text{if the PNA is below the bottom flange.} 
\]

The distance of the tension force in the bottom fillet, \( T_{FB} \), to the PNA is given by the following equations.

\[
x_{PNA} = y_p - d + t_{f-up} + 2k_{depth} + h + \frac{t_{f-bot}}{2}, \quad \text{if the PNA is above the top of the bottom flange,} \\
x_{PNA} = \frac{f_{f-bot} - y_y}{2}, \quad \text{if the PNA is within the bottom flange,} \\
x_{PNA} = 0, \quad \text{if the PNA is below the bottom of the bottom flange.} 
\]

The distance of the compression force in the bottom fillet, \( C_{FB} \), to the PNA is given by the following equations.

\[
x_{PNA} = 0, \quad \text{if the PNA is above the top of the bottom flange,} \\
x_{PNA} = \frac{y_y}{2}, \quad \text{if the PNA is within the bottom flange,} \\
x_{PNA} = z_p - t_c - h_r - r_d - t_{f-up} 2k_{depth} - h - \frac{t_{f-bot}}{2}, \quad \text{if the PNA is below the bottom flange.} 
\]
Note the terms \( z_p, t_c, \) and \( h_r \) in the preceding equation must all be for the left side of the beam or all for the right side of the beam. It does not matter which side of the beam is used, but all of the terms must be consistent.

- **Cover plate:** The force in the cover plate can be tension, or compression in the upper portion of the cover plate and tension in the lower portion. The following equations are used for the tension and compression forces in the cover plate.

\[
\begin{align*}
T_{CP} &= \phi b_c b_p t_c F_{yp}, & \text{if the PNA is above the top of the cover plate}, \\
T_{CP} &= \phi b_c b_p \left( t_c - y_y \right) F_{yp}, & \text{if the PNA is within the cover plate}, \\
C_{CP} &= 0, & \text{if the PNA is above the top of the cover plate}, \\
C_{CP} &= \phi b_c b_p y_y F_{yp}, & \text{if the PNA is within the cover plate}.
\end{align*}
\]

The distance of the tension force in the cover plate, \( T_{CP} \), to the PNA is given by the following equations

\[
\begin{align*}
x_{PNA} &= y_p - d + t_{j-top} + 2k_{depth} + h + t_{j-bot} + \frac{t_p}{2} \quad \text{if the PNA is above the top of the cover plate}, \\
x_{PNA} &= \frac{t_c - y_y}{2} \quad \text{if the PNA is within the cover plate}.
\end{align*}
\]

The distance of the compression force in the cover plate, \( C_{CP} \), to the PNA is given by the following equations

\[
\begin{align*}
x_{PNA} &= 0 \quad \text{if the PNA is above the top of the cover plate}, \\
x_{PNA} &= \frac{y_y}{2} \quad \text{if the PNA is within the cover plate}.
\end{align*}
\]

### 2.22 Composite Moment Capacity of a Partially Composite Beam with a Plastic Stress Distribution

This section describes how the positive moment capacity of the composite beam using a plastic stress distribution is calculated for partial composite connection.
2.22.1 Location of the Plastic Neutral Axis

The location of the PNA for partial composite connection with a plastic stress distribution is calculated using the method described in the subsection Location of the Plastic Neutral Axis of the section entitled Composite Plastic Moment Capacity for Positive Bending in this chapter, with the modifications described here.

The program determines the location of the PNA by comparing the maximum possible compressive force that can be developed in the concrete, \( MPF_{\text{conc}} \), with the maximum possible tensile force that can be developed in the steel section (including the cover plate, if applicable), \( MPF_{\text{steel}} \).

The maximum concrete force, \( MPF_{\text{conc}} \), is calculated as follows if there is no metal deck, or if the metal deck ribs are oriented perpendicular to the beam span.

\[
MPF_{\text{conc}} = \phi_{\text{hcc}} \left[ 0.85 f'_c b'_{\text{eff}} t_c \right]_{\text{left}} + \left( 0.85 f'_c b'_{\text{eff}} t_c \right)_{\text{right}} \leq p MPF_{\text{steel}}
\]

If the deck ribs are oriented parallel to the beam span, \( MPF_{\text{conc}} \) is calculated as follows.

\[
MPF_{\text{conc}} = \phi_{\text{hcc}} \left[ 0.85 f'_c b'_{\text{eff}} \left( t_c + \frac{w_i h_i}{S_i} \right) \right]_{\text{left}} + \left( 0.85 f'_c b'_{\text{eff}} \left( t_c + \frac{w_i h_i}{S_i} \right) \right)_{\text{right}} \leq p MPF_{\text{steel}}
\]

Note that the maximum concrete force has contributions from the left and right sides of the beam that are treated separately and may be different.

The maximum steel force, \( MPF_{\text{steel}} \), is calculated as follows if the beam is a rolled section:

\[
MPF_{\text{steel}} = \phi_{\text{hcc}} \left( A_{F_s} + b_{cp} t_{cp} F_{\text{ycp}} \right)
\]

\( MPF_{\text{steel}} \) is calculated as follows if the beam is a userdefined section.

\[
MPF_{\text{steel}} = \phi_{\text{hcc}} \left( b_{f-top} f_{f-top} F_{sf-top} + t_{w} h + b_{f-bot} t_{f-bot} F_{sf-bot} + b_{cp} t_{cp} F_{\text{ycp}} \right)
\]

Note that for a partial composite case, the expressions for \( MPF_{\text{steel}} \) remain the same. The expressions of \( MPF_{\text{conc}} \) have an upper limit based on steel’s axial
capacity. Here $p$ is the partial composite connection (PCC), which theoretically ranges from 0 to 1.

When computing the location of the PNA, it important to remember that the concrete is assumed to take no tension. Also, the concrete in the metal deck ribs is considered effective in compression only if the metal deck ribs are oriented parallel to the beam span.

The maximum concrete and steel forces are compared to determine whether the PNA is within the concrete slab or the steel section. Since $MPF_{steel} \geq MPF_{conc}$, the PNA is within the steel section.

Since the PNA is within the steel section, there are several general locations for it. After the general locations have been identified, it is a straightforward process to determine the location of the PNA. The general locations are as follows:

- Within the beam top flange.
- Within the beam top fillet (applies to rolled shapes from the program's section database only).
- Within the beam web.
- Within the beam bottom fillet (applies to rolled shapes from the program's section database only).
- Within the beam bottom flange.
- Within the cover plate (if one is specified).

Note it is very unlikely that the PNA would be below the beam web but there is nothing in the program to prevent it. This condition would require a very large beam bottom flange and/or cover plate. Each of the PNA locations in the steel section is described following the description of the PNA in the concrete slab.

With the known values of $MPF_{steel}$ and $MPF_{conc}$, where $MPF_{conc} \leq p(MPF_{steel})$, the program uses the subsections of the section Location of the Plastic Neutral Axis to determine the exact location of the PNA by calculating $y_2, y_3, y_4, y_5, y_6,$ and $y_7$. 

2 - 114 Location of the Plastic Neutral Axis
Then, the program assumes that the PNA occurs in the top flange of the beam. The distance $y_2$ is calculated as described previously for PNA within the beam top flange. The calculated distance $y_2$ is then checked to see if it actually is within the beam top flange. If it is, the location of the PNA has been identified.

If the calculated distance $y_2$ is not within the beam top flange, the program continues by assuming that the PNA occurs in the beam top fillet. (Note that if the beam is a user-defined beam, there is no top fillet and the program skips directly to assuming that the PNA is in the beam web.) The distance $y_3$ is calculated as described previously for PNA within the beam top fillet. The calculated distance $y_3$ is then checked to see if it actually is within the beam top fillet. If it is, the location of the PNA has been identified.

If the calculated distance $y_3$ is not within the beam top fillet, the program continues by assuming that the PNA occurs in the beam web. The distance $y_4$ is calculated as described previously for the PNA within the beam top fillet. The calculated distance $y_4$ is then checked to see if it actually is within the beam web. If it is, the location of the PNA has been identified.

In any practical case, the PNA is not expected to be below the beam web. However, in the event the PNA has not yet been located, the program continues down the beam section through the bottom fillet, the bottom flange and finally the cover plate until the location of the PNA has been identified.

### 2.22.2 Determining the Effective Portion of the Concrete Slab

For partial composite connection, when different composite decks and or spans are specified on each side of the beam, the effective portion of the slab is determined as follows: The program first puts the following six items in order, from highest elevation to lowest, to determine how much of the concrete slab is effective for partial composite connection:

- Top of concrete slab on the left side of the beam.
- Top of concrete slab on the right side of the beam.
- Top of metal on the left side of the beam.
- Top of metal on the right side of the beam.
- Bottom of metal on the left side of the beam.
- Bottom of the metal on the right side of the beam.

Next the program sums the compressive forces of these eight items, starting with the item at the highest elevation and proceeding downward. As each item is added into the sum, the sum of the compressive forces is compared with the $p(MPF_{steel})$ as determined in the previous subsection.

As soon as the sum of forces exceeds $p(MPF_{steel})$, the program recognizes that the last location considered is below the bottom of the effective concrete, and the second to last location considered is above the bottom of the effective concrete. Using this information, the program can solve directly for the location of the bottom of the effective concrete.

Figure 2-46 shows the internal concrete forces for a rolled steel section (a user-defined steel section is similar) for the condition where the bottom of the effective concrete is in the concrete slab above the metal deck. In this case, $a_1$ represents the distance from the top of the concrete slab to the bottom of the effective concrete. Note that the distance $a_1$ can be different on the left and right sides of the beam.

![Figure 2-44: Rolled Steel Section With Bottom of Effective Concrete in Concrete Slab Above Metal Deck, Positive Bending With Partial Composite Connection](image)

Figure 2-47 shows the internal concrete forces for a rolled steel section (a user-defined steel section is similar) for the condition where the bottom of the effective concrete is within the height, $h_r$, of the metal deck ribs. In this case,
\( a_2 \) represents the distance from the top of the metal deck ribs to the bottom of the effective concrete. Note that the distance \( a_2 \) can be different on the left and right sides of the beam.

The program obtains the distances \( a_1 \) and/or \( a_2 \) using an iterative solution technique.

If the bottom of effective concrete is in the concrete above the metal deck, \( a_2 \) is set equal to 0. If the bottom of effective concrete is within the height of the metal deck, \( a_1 \) is set equal to \( t_c \).

\[
\phi_{bcp} M_n = \phi_{bcpp} \sum_{\text{Piece}=1}^{12} T_{\text{piece}} x_{\text{PNA-piece}} + \phi_{bcpp} \sum_{\text{Piece}=1}^{12} C_{\text{piece}} x_{\text{PNA-piece}}
\]

All of the preceding terms have been described in the subsection Plastic Moment Capacity for Positive Bending in the previous section entitled Composite Plastic Moment Capacity for Positive Bending. The exception is...
that the forces in the concrete slabs and concrete ribs in the metal decks, both at
the left and right sides of the beam, are expressed in terms of $a_1$ and $a_2$ instead
of $z_p$ and $h_r$ only. Also the corresponding $x_{PNA}$ have been expressed in terms of
$a_1$ and $a_2$. All of these exceptions have been described previously there.

When calculating the moment capacity, concrete or reinforcing steel below the
bottom of the effective concrete is not considered in the calculation.

Note that the PNA for a partially composite beam always lies within the steel
beam section, not the concrete slab. Thus it is not necessary to check for the
PNA location within the concrete slab.
This chapter provides a detailed description of the algorithms used by the programs in the design/check of structures in accordance with “CSA S16-09 — Specifications for Structural Steel Building” (CSA 2009). Subsequent references to this code are identified with the prefix “CSA.”

3.1 Notation

- $A_{\text{bare}}$ Area of the steel beam (plus cover plate) alone, mm$^2$.

- $A_c$ Area of concrete within the slab effective width that is above the elastic neutral axis (ENA) for full composite action, mm$^2$. For beams with metal deck ribs running perpendicular to the beam span, only the concrete above the metal deck and above the ENA is included. For beams with metal deck ribs running parallel to the beam span, the concrete above the metal deck and the concrete in the deck ribs are included if it is above the ENA. This value may be different on the left and right sides of the beam.

- $A_f$ Area of compression flange, mm$^2$.

- $A_g$ Gross area of steel member, mm$^2$. 
\( A_s \) Area of rolled steel section, or the total area (excluding cover plate) of a user defined steel section, \( \text{mm}^2 \). Note that the total area of a user defined steel section is found by summing the area of the top flange, web, and bottom flange.

\( A_{sa} \) Cross-sectional area of a steel-headed stud anchor, \( \text{mm}^2 \).

\( A_{sb} \) Initial displacement amplitude of a single beam resulting from a heel drop impact, mm.

\( A_r \) Area of an element of the composite steel beam section, \( \text{mm}^2 \).

\( A_w \) Area of the web equal to the overall depth \( d \) times the web thickness \( t_w \), \( \text{mm}^2 \).

\( B_1 \) Moment magnifier, unitless.

\( C_{bot} \) Cope depth at bottom of beam, mm.

\( C_{C1} \) Compressive force in concrete slab above metal deck, N. If no metal deck exists, this is the compressive force in the slab.

\( C_{C2} \) Compressive force in concrete that is in the metal deck ribs, N. This force occurs only when the metal deck ribs are oriented parallel to the steel beam, and the plastic neutral axis is below the top of the metal deck.

\( C_{FT} \) Compressive force in the top flange of the steel beam, N. This force occurs only when the plastic neutral axis is below the top of the beam.

\( C_{KT} \) Compressive force in the top fillets of a rolled steel beam, N. This force occurs only when the plastic neutral axis is below the bottom of the top flange of the beam.

\( C_R \) Compressive force in the slab rebar, N. This force occurs only when the plastic neutral axis is below the rebar, and the user has specified the rebar to be considered.

\( C_{top} \) Cope depth at top of beam, mm.
$C_w$ Warping constant for a section, mm$^6$.

$C_{Web}$ Compressive force in the steel beam web, N. This force occurs only when the plastic neutral axis is within the beam web.

$D$ Damping ratio, percent critical damping inherent in the floor system, unitless.

$E_c$ Modulus of elasticity of concrete slab, MPa. Note that this could be different on the left and right sides of the beam. Also note that this is different for stress calculations and deflection calculations.

$E_s$ Modulus of elasticity of steel, MPa.

$F_{cr}$ Critical stress for columns in compression, MPa.

$F_L$ Smaller of $(F_{yf} - F_r)$ or $F_{yw}$, MPa.

$F_r$ Compressive residual stress in flange, MPa.

$F_u$ Minimum specified tensile strength of structural steel or shear stud, MPa.

$F_y$ Minimum specified yield stress of structural steel, MPa.

$F_{ycp}$ Minimum specified yield stress of cover plate, MPa.

$F_{yf-bot}$ Minimum specified yield stress of steel in the beam bottom flange, MPa.

$F_{yf-top}$ Minimum specified yield stress of steel in the beam top flange, MPa.

$F_{yw}$ Minimum specified yield stress of steel in the beam web, MPa.

$G$ Shear modulus of elasticity of steel, MPa.

$H_s$ Length of shear stud connector after welding, mm.
$I_{eff}$  Effective moment of inertia of a partially composite beam, mm$^4$.

$I_o$  Moment of inertia of an element of the composite steel beam section taken about its own center of gravity, mm$^4$.

$I_s$  Moment of inertia of the steel beam alone plus cover plate if applicable, mm$^4$.

$I_{tr}$  Transformed section moment of inertia about the elastic neutral axis of the composite beam, mm$^4$.

$I_x, I_y$  Moment of inertia about the $x$ and $y$ axes of the beam respectively, mm$^4$.

$I_{yc}$  Moment of inertia of compression flange about the $y$ axis, or if there is both positive and negative bending in the beam, the smaller moment of the two flanges, mm$^4$.

$J$  Torsional constant for a section, mm$^4$.

$K$  Effective length factor for prismatic member, unitless.

$L$  Center-of-support to center-of-support length of the beam, mm.

$L_b$  Laterally unbraced length of beam; length between points that are braced against lateral displacement of the compression flange or braced against twist of the cross-section, mm.

$L_c$  Limiting unbraced length for determining allowable bending stress, mm.

$L_{CBS}$  Length of a composite beam segment, mm. A composite beam segment spans between any of the following: (1) physical end of the beam top flange; (2) another beam framing into the beam being considered; (3) physical end of concrete slab. Figure 2-12 in the section entitled Distribution of Steel Headed Stud Anchors on a Composite Beam in Chapter 2 illustrates some typical cases for $L_{CBS}$. 

1 - 4  Notation
Chapter 3 - Design Process

$L_{csc}$ Length of channel shear connector, mm.

$L_p$ Limiting laterally unbraced length of beam for full plastic bending resistance, uniform moment case ($C_b = 1.0$), mm.

$L_r$ Limiting laterally unbraced length of beam for inelastic lateral-torsional buckling, mm.

$L_s$ Distance between two points used when the program is calculating the maximum number of shear studs that can fit between those points, mm. If the deck span is oriented parallel to the beam span and at least one of the points is at the end of the beam, then $L_s$ is taken as the distance between the two points minus 3 inches.

$L_1$ Distance from point of maximum moment to the closest point of zero moment or physical end of beam top flange, or physical end of concrete slab, mm.

$L_2$ Distance from point of maximum moment to the nearest point of zero moment or physical end of beam top flange, or physical end of concrete slab measured on the other side of the point of maximum moment from the distance $L_1$, mm.

$L_3$ Distance from point load to the point of zero moment, physical end of beam top flange, or physical end of concrete slab measured on the appropriate side of the point load, mm. If the point load is located on the left side of the point of maximum moment, the distance is measured from the point load toward the left end of the beam. If the point load is located on the right side of the point of maximum moment, the distance is measured toward the right end of the beam.

$M$ Moment, N-mm.

$M_A$ Absolute value of moment at the quarter point of the unbraced beam segment, N-mm.

$M_B$ Absolute value of moment at the centerline of the unbraced beam segment, N-mm.

Notation 3 - 5
$M_C$: Absolute value of moment at the three-quarter point of the unbraced beam segment, N-mm.

$M_{cr}$: Elastic buckling moment, N-mm.

$M_{max}$: Maximum positive moment for a beam, N-mm.

$M_n$: Nominal flexural strength, N-mm.

$M_p$: Plastic bending moment, N-mm.

$M_{pt \text{ load}}$: Moment at the location of a point load, N-mm.

$M_r$: Limiting buckling moment, $M_{cr}$, when $\lambda = \lambda_r$ and $C_b = 1.0$, N-mm.

$M_u$: Required flexural strength, N-mm.

$MPF_{\text{conc}}$: Maximum possible force that can be developed in the concrete slab, and rebar in slab, if applicable, N.

$MPF_{\text{steel}}$: Maximum possible force that can be developed in the steel section, and cover plate, if applicable, N.

$N_{CBS}$: The number of uniformly distributed shear connectors the program specifies for a composite beam segment, unitless.

$N_{\text{eff}}$: The effective number of beams resisting the heel drop impact, unitless.

$N_r$: Number of shear stud connectors in one rib at a beam intersection; not to exceed three in computations, although more than three studs may be installed, unitless.

$N_1$: Required number of shear connectors between the point of maximum moment and an adjacent point of zero moment (or end of slab), unitless.

$N_2$: Required number of shear connectors between a point load and a point of zero moment (or end of slab), unitless.
NR  Available number of metal deck ribs between two points, unitless.

$NS_{\text{max}}$  Maximum number of shear stud connectors between two points a distance of $L_s$ apart, unitless.

$P$  Axial load, N.

$P_e$  Euler buckling load, N.

$P_n$  Nominal axial strength (tension or compression), N.

$P_{nc}$  Nominal compressive axial strength, N.

$P_{nt}$  Nominal tensile axial strength, N.

$P_o$  Heel drop force, N. This force is taken as 0.29 kN.

$P_u$  Required axial strength (tension or compression), N.

$P_y$  Axial compressive yield strength, N.

$PCC$  Percent composite connection, unitless. The exact formula for this term is code dependent.

$Q_n$  Nominal strength of one shear connector (shear stud or channel), N.

$RF$  Reduction factor for horizontal shear resistance of shear connectors, unitless.

$RS_{\text{max}}$  Maximum number of rows of shear stud connectors that can fit between two points a distance of $L_s$ apart, unitless.

$S_{\text{sed}}$  Minimum edge distance from mid-height of a metal deck rib to the center of a shear stud, mm. For an example see paragraph 1b of the subsection Solid Slab or Deck Ribs Oriented Parallel to Beam Span in the subsection entitled Number of Shear Studs that Fit in a Composite Beam Segment in Chapter 2. The default value is 25 mm. This can be changed in the preferences and the overwrites.
<table>
<thead>
<tr>
<th>Symbol</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>$S_{eff}$</td>
<td>Effective section modulus of a partially composite beam referred to the extreme tension fiber of the steel beam section (including cover plate), mm$^3$.</td>
</tr>
<tr>
<td>$S_r$</td>
<td>Center-to-center spacing of metal deck ribs, mm.</td>
</tr>
<tr>
<td>$S_s$</td>
<td>Section modulus of the steel beam alone, plus cover plate if applicable, referred to the tension flange, mm$^3$.</td>
</tr>
<tr>
<td>$S_{reff}$</td>
<td>The section modulus for the partial composite section referred to the top of the equivalent transformed section, mm$^3$.</td>
</tr>
<tr>
<td>$S_{top}$</td>
<td>Section modulus for the fully composite uncracked transformed section referred to the extreme compression fiber, mm$^3$.</td>
</tr>
<tr>
<td>$S_{tr}$</td>
<td>Section modulus for the fully composite uncracked transformed section referred to the extreme tension fiber of the steel beam section (including cover plate), mm$^3$.</td>
</tr>
<tr>
<td>$S_x$, $S_y$</td>
<td>Section modulus about the $x$ and $y$ axes of the beam respectively, mm$^3$.</td>
</tr>
<tr>
<td>$S_{xc}$</td>
<td>Section modulus about the $x$ axis of the outside fiber of the compression flange, mm$^3$.</td>
</tr>
<tr>
<td>$S_{xt}$</td>
<td>Section modulus about the $x$ axis of the outside fiber of the tension flange, mm$^3$.</td>
</tr>
<tr>
<td>$T_B$</td>
<td>Tensile force in a composite rolled steel beam when the plastic neutral axis is above the top of the beam, N.</td>
</tr>
<tr>
<td>$T_{CP}$</td>
<td>Tensile force in the cover plate, N.</td>
</tr>
<tr>
<td>$T_{FB}$</td>
<td>Tensile force in the bottom flange of a steel beam, N.</td>
</tr>
<tr>
<td>$T_{FT}$</td>
<td>Tensile force in the top flange of a steel beam, N.</td>
</tr>
<tr>
<td>$T_{KB}$</td>
<td>Tensile force in the bottom fillets of a rolled steel beam, N.</td>
</tr>
<tr>
<td>$T_{KT}$</td>
<td>Tensile force in the top fillets of a rolled steel beam, N.</td>
</tr>
<tr>
<td>Symbol</td>
<td>Description</td>
</tr>
<tr>
<td>--------</td>
<td>-------------</td>
</tr>
<tr>
<td>$T_{\text{Web}}$</td>
<td>Tensile force in the web of a steel beam, N.</td>
</tr>
<tr>
<td>$V$</td>
<td>Shear force, N.</td>
</tr>
<tr>
<td>$V_n$</td>
<td>Nominal shear strength, N.</td>
</tr>
<tr>
<td>$V_u$</td>
<td>Required shear strength, N.</td>
</tr>
<tr>
<td>$W$</td>
<td>Total load supported by the beam, N. The user specifies a load combination that the program uses to determine this weight.</td>
</tr>
<tr>
<td>$Z$</td>
<td>Plastic section modulus of the steel beam alone plus cover plate if applicable, mm$^3$.</td>
</tr>
<tr>
<td>$Z_x, Z_y$</td>
<td>Plastic section modulus about the $x$ and $y$ axes of the beam respectively, mm$^3$.</td>
</tr>
<tr>
<td>$a$</td>
<td>Clear distance between transverse stiffeners, mm.</td>
</tr>
<tr>
<td>$a_r$</td>
<td>For a user defined section, the ratio of the web area to the flange area, but not more than 10, unitless.</td>
</tr>
<tr>
<td>$a_1$</td>
<td>Distance from the top of the concrete to the bottom of the effective concrete for partial composite connection when the bottom of the effective concrete is within the slab above the metal deck (or there is a solid slab with no metal deck), mm.</td>
</tr>
<tr>
<td>$a_2$</td>
<td>Distance from the top of the metal deck to the bottom of the effective concrete for partial composite connection when the bottom of the effective concrete is within the height of the metal deck, mm.</td>
</tr>
<tr>
<td>$a_3$</td>
<td>Distance from the top of the metal deck to the elastic neutral axis when the elastic neutral axis is located in the slab above the metal deck, mm.</td>
</tr>
<tr>
<td>$b$</td>
<td>Width, mm.</td>
</tr>
<tr>
<td>$b_{cp}$</td>
<td>Width of the steel cover plate, mm.</td>
</tr>
</tbody>
</table>
$b_{eff}$: Effective width of the concrete flange of the composite beam, mm.

$b_f$: Width of the flange of a rolled steel beam, mm.

$b_{f/bot}$: Width of the bottom flange of a user defined steel beam, mm.

$b_{f/top}$: Width of top flange of a user defined steel beam, mm.

d: Depth of a steel beam from the outside face of the top flange to the outside face of the bottom flange, mm.

d$_{avg}$: Average depth of the concrete slab, including the concrete in the metal deck ribs, mm.

d$_{sc}$: Diameter of a shear stud connector, mm.

f: First natural frequency of the beam in cycles per second.

$f'_c$: Specified compressive strength of concrete, MPa.

g: Acceleration of gravity, mm/seconds$^2$.

$h$: Clear distance between flanges less the fillet or corner radius at each flange for rolled shapes and clear distance between flanges for other shapes, mm.

$h_r$: Height of metal deck rib, mm.

$k$: Distance from the outer face of a rolled beam flange to the web toe of a fillet, mm.

$k_{depth}$: Distance from the inner face of a rolled beam flange to the web toe of a fillet, mm.

$k_{width}$: Width of the idealized fillet of a rolled beam section, mm.

$l$: Controlling laterally unbraced length of a member, mm.

$l_{22}$, $l_{33}$: Laterally unbraced length of a member for buckling about the local 2 and 3 axes of the beam respectively, mm.
$r_d$  Distance from the top of the beam flange to the bottom of the metal deck, mm.

$r_{22}, r_{33}$  Radius of gyration about the local 2 and 3 axes of the beam respectively, mm.

$r_x, r_y$  Radius of gyration about the $x$ and $y$ axes of the beam respectively, mm.

$r_{yc}$  Radius of gyration of the compression flange about the $y$ axis, mm.

$s_b$  Beam spacing, mm.

$t$  Thickness, mm.

$t_c$  Thickness of concrete slab, mm. If there is metal deck, this is the thickness of the concrete slab above the metal deck.

$t_{cp}$  Thickness of the cover plate, mm.

$t_f$  Thickness of the steel beam flange, mm.

$t_{f\text{-bot}}$  Thickness of the bottom flange of a user defined steel beam, mm.

$t_{f\text{-top}}$  Thickness of the top flange of a user defined steel beam, mm.

$t_o$  Time to the maximum initial displacement of a single beam resulting from a heel drop impact, seconds.

$t_w$  Thickness of the web of a user defined steel beam, mm.

$w_a$  Additional metal deck rib width, mm. This term is used to specify metal deck ribs that are split over the beam. The width $w_a$ is added to the width $w_r$ when determining the width of deck rib available for shear studs.

$w_c$  Unit weight per volume of concrete, N/mm$^3$.

$w_d$  Unit weight per area of metal deck, MPa.
$w_r$ Average width of the metal deck rib, mm.

$x_1$ The assumed gap distance from the supporting beam or column flange to the end of the beam flange, mm. The default value for this length is 12 mm.

$\bar{y}$ Distance from the bottom of the bottom flange of the steel beam section to the elastic neutral axis of the fully composite beam, mm.

$y_{bare}$ The distance from the bottom of the bottom flange of the steel beam to the neutral axis of the non-composite steel beam plus the cover plate if applicable, mm.

$y_e$ The distance from the elastic neutral axis of the bare steel beam alone (plus cover plate, if applicable) to the elastic neutral axis of the fully composite beam, mm.

$y_{eff}$ The distance from the bottom of the bottom flange of the steel beam to the neutral axis of the partially composite beam, mm.

$y_1$ Distance from the bottom of the bottom flange of the steel beam section to the centroid of an element of the composite beam section, mm.

$y_2$ Distance from the top of the top flange of the steel beam section to the plastic neutral axis when the plastic neutral axis is within the beam top flange, mm.

$y_3$ Distance from the bottom of the top flange of a rolled steel beam section to the plastic neutral axis when the plastic neutral axis is within the fillets, mm.

$y_p$ Distance from the plastic neutral axis of composite section to the bottom of the beam bottom flange (not cover plate), mm.

$\Sigma A$ Sum of the areas of all of the elements of the steel beam section, mm$^2$.

$\Sigma A_{tr}$ Sum of the areas of all of the elements of the composite steel beam section, mm$^2$. 

3 - 12 Notation
<table>
<thead>
<tr>
<th>Notation</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>( \sum(A_{ty}y_1) )</td>
<td>Sum of the product ( A_{ty} ) times ( y_1 ) for all of the elements of the composite steel beam section, mm(^3).</td>
</tr>
<tr>
<td>( \sum(Ay_1) )</td>
<td>Sum of the product ( A ) times ( y_1 ) for all of the elements of the steel beam section, mm(^3).</td>
</tr>
<tr>
<td>( \sum(Ay_1^2) )</td>
<td>Sum of the product ( A ) times ( y_1^2 ) for all of the elements of the steel beam section, mm(^4).</td>
</tr>
<tr>
<td>( \sum(A_{ty}y_1^2) )</td>
<td>Sum of the product ( A_{ty} ) times ( y_1^2 ) for all of the elements of the composite steel beam section, mm(^4).</td>
</tr>
<tr>
<td>( \sum I_0 )</td>
<td>Sum of the moments of inertia of each element of the composite steel beam section taken about the center of gravity of the element, mm(^4).</td>
</tr>
<tr>
<td>( \sum Q_n )</td>
<td>Sum of the nominal strength of the shear connectors (shear stud or channel) between the considered point and the point of zero moment, N.</td>
</tr>
<tr>
<td>( \sum Q_{n-PCC} )</td>
<td>Required nominal strength of the shear connectors (shear stud or channel) between the considered point and the point of zero moment for partial composite connection percentage, PCC, N.</td>
</tr>
<tr>
<td>( \sum Q_{n-100} )</td>
<td>Required nominal strength of the shear connectors (shear stud or channel) between the considered point and the point of zero moment for full (100%) composite action, N.</td>
</tr>
<tr>
<td>( \beta )</td>
<td>Unitless factor used in calculating the number of shear studs between a point load and a point of zero moment, equal to ( S_{tr}/S_t ) for full composite connection and ( S_{eff}/S_t ) for partial composite connection.</td>
</tr>
<tr>
<td>( \phi )</td>
<td>Resistance factor, unitless.</td>
</tr>
<tr>
<td>( \phi_{\text{concrete}} )</td>
<td>Resistance factor applied to concrete for bending in a composite section, unitless. The default value is 0.65.</td>
</tr>
<tr>
<td>( \phi_{\text{steel}} )</td>
<td>Resistance factor applied to steel for bending in a composite section, unitless. The default value is 0.9.</td>
</tr>
</tbody>
</table>
3.2 Design Methodology

The flowchart in Figure 3-1 shows the general methodology for composite beam design of a single beam element using the CSA S16-09 specification. The numbered boxes in the flowchart correspond to the "Box" identifiers used in the text of this chapter. The flowchart is intended to convey the important features of the CSA S16-09 design methodology. It should not be literally construed as a flowchart for the actual computer code included in the program.

Box 1 - Start Here
To begin, note that the flowchart is set up for a single beam. Thus the flow process shown must be applied to each beam designed. Do not confuse the beam that is being designed with a trial section for that beam. The beam that is being designed is an actual element in the model. A trial section is simply a beam section size that is checked for the beam that is being designed.

Box 2 - Design Load Combinations
The program creates default design load combinations for composite beam design using the CSA S16-09 specification. Also any user specified design load combinations can be interpreted and implemented. Refer to Design Load Combinations for a description of the CSA S16-09 default design load combinations.
Box 3 - Design Check Locations
The program determines all of the design check locations for a given beam. Also refer to Beam Unbraced Length and Design Check Locations in Chapter 2.

Box 4 - Checking Order for Beams
If the beam is assigned an auto selection property, the checking order for the beam must be determined. The program considers the beams in the auto select list in the order described in the section entitled How the Program Optimizes Design Groups in Chapter 2.
Figure 3-1 Flowchart for CSA S16-09 Design of a Single Beam
Box 5 - Trial Beam Section
The program allows the user to select the next trial beam section to be checked for conformance with the CSA S16-09 specification and any additional user defined criteria. Refer to the section entitled How the Program Optimizes Design Groups in Chapter 2 for a description of this selection process.

Box 6 - Compact and Noncompact Requirements
For CSA S16-09 design of composite beams, the program requires that the beam section be either compact or noncompact. Slender sections are not designed. The program checks to make sure the beam is not slender. Refer to Compact and Noncompact Requirements later in this chapter for a description of how the program checks compact and noncompact requirements.

Box 7 - Stress Distribution Used to Calculate Moment Capacity
The program determines whether to use a plastic or an elastic stress distribution when calculating the moment resistance for CSA S16-09 design. See Compact and Noncompact Requirements later in this chapter for more information.

Box 8 - Transformed Section Properties
The program computes the transformed section properties of the trial beam section. If there is only positive bending in the beam, only the transformed section properties for positive bending are calculated. Similarly, if there is only negative bending in the beam, only the transformed section properties for negative bending are calculated. If there is both positive and negative bending in the beam, transformed section properties for both positive and negative bending are calculated.

Refer to Effective Width of the Concrete Slab in Chapter 2 for a description of how the program calculates the effective width of the concrete slab for the composite beam. Refer to Transformed Section Moment of Inertia in Chapter 2 for a description of how the program calculates the transformed section properties.

In CSA S16-09 design, the transformed section properties are used for calculating deflection, and they are used when the moment resistance is determined based on an elastic stress distribution; that is, when the web is noncompact.
Box 9 - Initial Moment Resistance and Deflection Check
The program checks that the moment resistance of the beam using full composite connection is greater than or equal to the applied factored moment. It also checks if the deflection using full composite connection is acceptable. The main purpose of this check is to quickly eliminate inadequate beam sections. Refer to Bending and Deflection Checks later in this chapter for more information.

Box 10 - Vibration Criteria Check
The program calculates the vibration parameters. If vibration is specified to be used as one of the tools for selecting the optimum beam size, the program checks if the vibration parameters satisfy the specified limits. If the vibration check is satisfied, the design using the current trial section continues; otherwise, the design for this section is terminated. For more detailed information on the vibration checks, refer to Floor Vibration in Chapter 2.

Box 11 - Axial Load
The program checks if axial load exists on the beam for any design load combination. If so, the axial load resistance is determined and the interaction is subsequently checked, as indicated in Box 14. If there is no axial load on the beam, the axial resistance is not determined and the interaction check (Box 14) is skipped. Refer to Compact and Noncompact Requirements later in this chapter for a description of how the program calculates axial load resistance.

Box 12 - P-M Interaction Check
If there is axial load on the beam, the program checks the P-M interaction equations. If the interaction check is satisfied, the design using the current trial section continues; otherwise, the design for this section is terminated. Refer to Moment Capacity for Steel Section Alone later in this chapter for more information.

Box 13 - Partial Composite Action
A significant amount of design is performed at this point in the process. The program determines the smallest amount of composite connection for which the beam is adequate. Both flexural checks and deflection checks are made at this point. In addition, the program considers axial load on the beam if it exists and is specified to be considered. Flexural checks are also made for the construction loads.
For more information refer to *Composite Moment Capacity of a Partially Composite Beam with a Plastic Stress Distribution* in Chapter 2 and *Bending Checks and Deflection Checks* later in this chapter. Also refer to the section entitled *Positive Moment Capacity with an Elastic Stress Distribution* in Chapter 2.

**Box 14 - Required Number of Shear Connectors**
The program calculates the required number of shear connectors on the beam and the distribution of those shear connectors. For more information refer to *Steel Anchors* later in this chapter. Also refer to *Distribution of Shear Studs on a Composite Beam* and *Number of Shear Studs that Fit in a Composite Beam Segment* in Chapter 2. Finally refer to *Effective Width of the Concrete Slab* in Chapter 2 for limitations associated with composite beams and formed metal deck.

**Box 15 - Checking if Shear Connectors Fit on the Beam**
The program checks if the number of shear connectors calculated (Box 14) actually fits on the beam. For more information refer to *Number of Shear Studs that Fit in a Composite Beam Segment* in Chapter 2. If the connectors fit on the beam, the design using the current trial section continues; otherwise, the design for this section is terminated.

**Box 16 - Beam Shear**
The program checks the beam shear for the reactions at each end of the beam. See *Beam Shear Capacity* later in this chapter for more information. If the beam shear check is satisfied, the design using the current trial section continues; otherwise, the design for this section is terminated.

**Box 17 - Camber**
The program determines the camber for the beam, if it is specified to have camber. Refer to *Beam Deflection and Camber* in Chapter 2 for more information.

**Box 18 - Section Price**
Determination of the price of a section applies only when price has been specified by the user as the method of selecting the optimum section. In such cases, the program determines the price of the current beam. Refer to the section entitled *How the Program Optimizes Design Groups* in Chapter 2 for more information.
Box 19 - Check if a Section is the Current Optimum Section
This check applies only if price has been specified as the method of selecting the optimum section. The program checks if the price of the current trial beam is less than that of any other beam that satisfies the design criteria. If so, the current beam section becomes the current optimum beam section. Refer to the section entitled How the Program Optimizes Design Groups in Chapter 2 for more information.

If the optimum beam size is to be selected by weight, this check becomes irrelevant because the beams are checked in order from the lightest to the heaviest beams and thus the first beam found to work is the optimum beam.

Box 20 - Checking for Possible Additional Optimum Sections
This check applies only if the beam has been assigned an auto selection property. The program checks if another section in the auto selection list might qualify as the optimum beam section. Refer to the section entitled How the Program Optimizes Design Groups in Chapter 2 for more information.

Box 21 - Design Complete
At this point, the design for this particular beam element is complete. If the beam has been assigned an auto select property, the current optimum section, assuming one has been found, is the optimum section for the beam. The program will indicate if no beam with an optimum section is included in the auto select list.

If the beam is assigned a regular, non-auto select property, the design for that beam property will be provided or the beam will be indicated to be inadequate.

There are some additional aspects included in the composite beam design module that are not directly addressed in the flowchart shown in Figure 3-1. Those include designing beams in groups and designing beams with partial length cover plates.

For more information on the design by group feature, refer to the section entitled How the Program Optimizes Design Groups in Chapter 2. The extension of the methodology described for designing by groups is relatively simple and is assumed to be apparent to the reader.
When a beam has a partial length cover plate, the program checks not only the design at the point of the maximum moment (Box 8 of Figure 3-1), but also the design at the point of the largest moment where the cover plate does not exist.

### 3.3 Compact and Noncompact Requirements

This section describes how the program checks the CSA S16-09 specification requirements for compact and noncompact beams. The basic compact and noncompact requirements checked are in CSA S16-09 Chapter B, Table 4.1b. The program checks the width-to-thickness ratios of the beam compression flange, beam web, and, if it exists and is in compression, the cover plate. When a singly symmetric beam is designed for non-composite behavior, it is also checked for lateral torsional buckling requirements.

The program classifies beam sections as either plastic, compact, noncompact or slender. It checks the plastic, compact and noncompact section requirements at each design location along the beam for each design load combination separately. A beam section may be classified differently for different design load combinations. For example, a beam may be classified as compact for design load combination A and as noncompact for design load combination B. Two reasons that a beam may be classified differently for different design load cases are as follows.

The compact section requirements for beam webs depend on the axial load in the beam. Different design load combinations may produce different axial loads in the beam. This is an issue only when beam axial loads are specified to be considered in the composite beam analysis and design.

The compression flange may be different for different design load combinations. If the sizes of the top and bottom flanges are not the same, classification of the section may depend on which flange is determined to be the compression flange.

At each design location, for each design load combination, the program first checks a beam section for the compact section requirements for the compression flange, web, cover plate (if applicable) and lateral torsional buckling (if applicable) described herein. If the beam section meets all of those requirements, it is classified as compact for that design load combination. If the beam section does not meet all of the compact section requirements, it is
checked for the noncompact requirements for the flanges, web, cover plate (if applicable) and lateral torsional buckling (if applicable) described herein. If the beam section meets all of those requirements, it is classified as noncompact for that design load combination. If the beam section does not meet all of the noncompact section requirements, it is classified as slender for that design load combination, and the program does not consider it for composite beam design.

3.3.1 Limiting Width-to-Thickness Ratios for Flanges

This section describes the limiting width-to-thickness ratios considered by the program for beam compression flanges. The width-to-thickness ratio for flanges is denoted $b_t$, and is equal to $b_f/2t_f$ for I-shaped sections and $b_f/t_f$ for channel sections.

3.3.1.1 Plastic Section Limits for Flanges

For plastic sections, the width-to-thickness ratio for the compression flange is limited to that indicated by the following equation,

$$\frac{b}{t} \leq \frac{145}{\sqrt{F_{sy}}}, \text{ for plastic sections,}$$

(CSA 11.1, 11.2, 13.5.c, Table 2)

where $F_{sy}$ is the specified yield stress of the flange considered. The preceding equation applies to both rolled sections selected from the program's database and to user defined sections.

3.3.1.2 Compact Section Limits for Flanges

For compact sections, the width-to-thickness ratio for the compression flange is limited to that indicated by the following equation,

$$\frac{b}{t} \leq \frac{170}{\sqrt{F_{sy}}}, \text{ for compact sections,}$$

(CSA 11.1, 11.2, 13.5.c, Table 2)

where $F_{sy}$ is the specified yield stress of the flange considered. The preceding equation applies to both rolled sections selected from the program's database and to user defined sections.
3.3.1.3 Noncompact Section Limits for Flanges

3.3.1.3.1 I-Shaped Rolled Beams and Channels
For noncompact I-shaped rolled beams and channels, the width-to-thickness ratio for the compression flange is limited to that indicated by the following equation,

\[
\frac{b}{t} \leq \frac{200}{\sqrt{F_{yf}}}, \text{ for noncompact sections, (CSA 11.1, 11.2, 13.5.c, Table 2)}
\]

where \(F_{yf}\) is the specified yield stress of the beam or channel.

3.3.1.3.2 User Defined and Hybrid Beams
For noncompact user defined and hybrid beams, the width-to-thickness ratio for the compression flange is limited to that indicated by the following equation,

\[
\frac{b}{t} \leq \frac{200}{\sqrt{F_{yf}}}, \text{ for noncompact sections, (CSA 11.1, 11.2, 13.5.c, Table 2)}
\]

where \(F_{yf}\) is the specified yield stress of the beam or channel.

3.3.2 Limiting Width-to-Thickness Ratios for Webs
This section describes the limiting width-to-thickness ratios considered by the program for beam webs.

3.3.2.1 Compact Section Limits for Webs
When checking a beam web for compact section requirements, the width-to-thickness ratio used is \(h/t_{w}\). The equation used for checking the compact section limits in the web depends on the ratio of elastic neutral axis to plastic neutral axis and the ratio of \(C_f/C_y\) :

- The program uses \(\phi_b = 0.9\) for both elastic and plastic stress distribution. It is used for moment resistance.
- The following equation defines the plastic section limit for webs. For flexure in webs of doubly symmetric I-shaped sections and channels:
The following equation defines the compact section limit for webs. For flexure in webs of doubly symmetric I-shaped sections and channels:

\[
\frac{h}{t_w} \leq \frac{1100}{F_y} \left( 1 - 0.39 \frac{C_f}{C_y} \right). \quad \text{(CSA 11.1, 11.2, 13.5.c, Table 2)}
\]

In the preceding equations, the value of \( F_y \) used is the largest of the \( F_y \) values for the beam flanges and the web.

### 3.3.2.2 Noncompact Section Limits for Webs

When checking a beam web for noncompact section requirements, the width-thickness ratio that is used for web compactness is \( h/t_w \), and its limit for noncompact section is taken as follows:

\[
\frac{h}{t_w} \leq \frac{1700}{F_y} \left( 1 - 0.61 \frac{C_f}{C_y} \right). \quad \text{(CSA 11.1, 11.2, 13.5.c, Table 2)}
\]

### 3.3.3 Limiting Width-to-Thickness Ratios for Cover Plates

The width-to-thickness checks made for the cover plate depend on the width of the cover plate compared to the width of the beam bottom flange. Figure 3-2 illustrates the conditions considered.
In Case A of the figure, the width of the cover plate is less than or equal to the width of the beam bottom flange. In that case, the width-to-thickness ratio is taken as $b_1/t_{cp}$, and it is checked as a flange cover plate.

In Case B of Figure 3-2, the width of the cover plate is greater than the width of the beam bottom flange. Two conditions are checked in that case. The first condition is the same as that shown in Case A, where the width-to-thickness ratio is taken as $b_1/t_{cp}$ and is checked as a flange cover plate. The second condition checked in Case B takes $b_2/t_{cp}$ as the width-to-thickness ratio and checks it as a plate projecting from a beam.

### 3.3.3.1 Plastic Section Limits for Cover Plates

For both cases A and B shown in Figure 3-2, the cover plate is checked for compact section requirements as follows:

\[
\frac{b_1}{t_{cp}} \leq \frac{145}{\sqrt{F_{yf}}} \tag{CSA 11.1, 11.2, 13.5.c, Table 2}
\]

\[
\frac{b_2}{t_{cp}} \leq \frac{145}{\sqrt{F_{yf}}} \tag{CSA 11.1, 11.2, 13.5.c, Table 2}
\]
where \( b_1, b_2, \) and \( t_{cp} \) are defined in Figure 3-2.

### 3.3.3.2 Compact Section Limits for Cover Plates

For both cases A and B shown in Figure 3-2, the cover plate is checked for compact section requirements as follows:

\[
\frac{b_1}{t_{cp}} \leq \frac{170}{\sqrt{F_{sf}}} \quad \text{(CSA 11.1, 11.2, 13.5.c, Table 2)}
\]

\[
\frac{b_2}{t_{cp}} \leq \frac{170}{\sqrt{F_{sf}}} \quad \text{(CSA 11.1, 11.2, 13.5.c, Table 2)}
\]

where \( b_1, b_2, \) and \( t_{cp} \) are defined in Figure 3-2.

### 3.3.3.3 Noncompact Section Limits for Cover Plates

For both cases A and B shown in Figure 3-2, the cover plate is checked for noncompact section requirements as follows:

\[
\frac{b_1}{t_{cp}} \leq \frac{200}{\sqrt{F_{sf}}} \quad \text{(CSA 11.1, 11.2, 13.5.c, Table 2)}
\]

\[
\frac{b_2}{t_{cp}} \leq \frac{200}{\sqrt{F_{sf}}} \quad \text{(CSA 11.1, 11.2, 13.5.c, Table 2)}
\]

where \( b_1, b_2, \) and \( t_{cp} \) are defined in Figure 3-2.

### 3.3.4 Slenderness Ratios for Lateral Torsional Buckling

When a singly symmetric beam is designed for non-composite behavior, it is checked for lateral torsional buckling requirements. If the singly symmetric beam is unshored, this check occurs for any construction design load case. It also occurs for beams that have negative bending that are not specified to consider the composite action provided by the slab rebar. Finally, the check occurs for any singly symmetric beam specified to be non-composite.

When reviewing for lateral torsional buckling requirements, the value of \( L_b / r_{xc} \) is checked. \( L_b \) is the laterally unbraced length of beam; that is, the length between points that are braced against lateral displacement of the compression
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flange. The term \( r_{yc} \) is the radius of gyration of the compression flange about the \( y \) axis.

### 3.4 Composite Plastic Moment Capacity for Positive Bending

The plastic moment resistance for full composite connection, \( M_p \), is calculated based on the section entitled "Composite Plastic Moment Capacity for Positive Bending" in Chapter 2.

The plastic moment resistance for partial composite beam, \( M_p \), is calculated based on the section entitled "Composite Moment Capacity of a Partially Composite Beam with a Plastic Stress Distribution" in Chapter 2.

Figure 2-30 in Chapter 2 illustrates a generic plastic stress distribution for positive bending for both full and partial composite cases. Note that the concrete is stressed to \( \alpha_i = 0.85 - 0.0015 f'_c \), where \( \alpha_i \geq 0.67 \) and the steel is stressed to \( F_y \) (CSA 17.9.3). The illustrated plastic stress distribution is the basic distribution of stress used by the program when considering a plastic stress distribution for positive bending. Note that if the metal deck ribs are parallel to the beam, the concrete in the ribs is also considered.

It should be noted that for both full and partial composite cases, the concrete stress block is stressed to \( \alpha_i f'_c \), where \( \alpha_i = 0.85 - 0.0015 f'_c \) (CSA 17.9.3).

### 3.5 Moment Capacity for Steel Section Alone

This section describes how the program calculates the moment resistance of a non-composite steel beam, including a cover plate, if applicable.

The program calculates the moment resistance, \( M_p \), only if the beam is compact or noncompact. It does not calculate \( M_r \) if the section is slender. The plastic moment, \( M_p \), for a non-composite rolled steel beam section without a cover plate is calculated as \( M_p = ZF_y \).

The exact methodology used to compute the plastic moment resistance in the other cases depends on whether the beam, including the cover plate if it exists,
is doubly or singly symmetric, and whether the beam web is classified as compact or noncompact.

Figure 3-3 shows a flowchart that identifies the appropriate section in this chapter for calculating the moment resistance of the steel section alone.

The figure has boxes labeled a through g; start in the box labeled a. Note that the criteria used by the program to determine if a section is compact or noncompact for the CSA S16-09 specification is described in this chapter in the section entitled Compact and Noncompact Requirements.

**Figure 3-3 Flowchart to Determine which Section of this Chapter Applies When Calculating Plastic Moment for Steel Sections Alone**

### 3.5.1 Steel Beam Properties

If properties for the steel section alone are available directly from the program's section database, then those properties are used to compute the moment resistance. For other cases such as a user defined section or a section with a cover plate, the section properties are calculated in a manner similar to that described in *Transformed Section Moment of Inertia* in Chapter 2, except that there is no concrete or reinforcing steel to consider.

After the moment of inertia has been calculated, the section moduli and radius of gyration are calculated using standard formulas. This process is repeated to get properties about both axes. The torsional constant is determined by summing the torsional constants for the various components of the section. For
example, it may be determined by summing the \( J \)'s of a rolled section and the cover plate, if applicable, or in a user defined section, by summing the \( J \)'s for the top flange, web, bottom flange and cover plate, if applicable.

### 3.5.2 Moment Capacity for a Doubly Symmetric I-Beam

The nominal flexural strength for major axis bending depends on compactness of the web and flanges.

The factored moment resistance in the major and minor directions is based on the geometric shape of the section, the section classification for compactness, and the unbraced length of the member. The bending strengths are evaluated according to CSA S16-09 as follows (CSA 13.5 and 13.6):

The program uses the minimum of the flexure strength, \( M_r \), computed from the Cross-Sectional Strength, Overall Member Strength and Torsional and Torsional-Lateral Buckling Strength.

Cross-Sectional Strength and Overall Member Strength: The \( M_{r33} \) and \( M_{r22} \) are calculated assuming that the member is laterally fully supported (\( l_{22} = 0 \) and \( l_{33} = 0 \)) irrespective of its actual lateral bracing length (CSA 13.5).

Lateral-Torsional Buckling Strength: \( M_{r33} \) and \( M_{r22} \) are calculated based on actual unbraced length (CSA 13.6).

If the capacities (\( M_{r22} \) and \( M_{r33} \)) are overwritten by the user, they are assumed not to apply to this case and are ignored.

For Cross-Sectional Strength and Overall Member Strength cases, the moment capacities are considered to be as follows:

For Plastic and Compact Section, \[ M_r = \phi Z F_y, \quad \text{and} \quad (\text{CSA 13.5}) \]

For noncompact, \[ M_r = \phi S F_y. \quad (\text{CSA 13.5}) \]

For Lateral-Torsional Buckling Strength, the moment capacities are considered to be as follows (CSA 13.6a).

For plastic and compact sections of I-shapes and boxes bent about the major axis,
when \( M_f > 0.67 M_{p33} \),

\[
M_{r33} = 1.15 \phi M_{p33} \left[ 1 - 0.28 \frac{M_{p33}}{M_u} \right] \leq \phi M_{p33} ,
\]

(CSA 13.6 a)

when \( M_f \leq 0.67 M_{p33} \),

\[
M_{r33} = \phi M_f
\]

where,

- \( M_{r33} = \) Factored major bending resistance,
- \( M_{p33} = \) Major plastic moment,
- \( M_f = \) Critical elastic moment,

\[
M_f = \frac{\omega_2 \pi}{L} \sqrt{E I_{22} G J + \left( \frac{\pi E}{L} \right)^2 I_{22} C_w}
\]

(CISC 13.6 a)

\( L = \) Laterally unbraced length, \( I_{22} \),

\( C_w = \) Warping constant assumed as 0.0 for boxes, pipes, rectangular and circular bars, and

\[
\omega_2 = 1.75 + 1.05 \left[ \frac{M_a}{M_b} \right] + 0.30 \left[ \frac{M_a}{M_b} \right]^2 \leq 2.5 .
\]

(CSA 13.6 a)

\( M_a \) and \( M_b \) are end moments of the unbraced segment and \( M_a \) is less than \( M_b \), \( \left[ \frac{M_a}{M_b} \right] \) being positive for double curvature bending and negative for single curvature bending. If any moment within the segment is greater than \( M_b \), \( \omega_2 \) is taken as 1.0. The program defaults \( \omega_2 \) to 1.0 if the unbraced length, \( I \) of the member is overwritten by the user (i.e., it is not equal to the length of the member). \( \omega_2 \) should be taken as 1.0 for cantilevers. However, the program is unable to detect whether the member is a cantilever. The user can overwrite the value of \( \omega_2 \) for any member by specifying it.

For noncompact sections of I-shapes and channels bent about the major axis,

when, \( M_u > 0.67 M_{y33} \)  

(CISC 13.6 b)
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\[ M_{r33} = 1.15 \phi M_{y33} \left[ 1 - 0.28 \frac{M_{y33}}{M_u} \right] \leq \phi M_{y33} \]  
(CSA 13.6 b)

when, \( M_u \leq 0.67 M_{y33} \),  
(CSA 13.6 b)

\[ M_{r33} = \phi M_u. \]  
(CSA 13.6 b)

\( M_{r33} \) and \( M_u \) are as defined earlier for plastic and compact sections, and \( M_{y33} \) is the major yield moment.

3.5.3 Moment Capacity for a Channel Section Beam

For noncompact channel sections bent about their major axis,

when, \( M_u > 0.67 M_{y33} \)  
(CSA 13.6 b)

\[ M_{r33} = 1.15 \phi M_{y33} \left[ 1 - 0.28 \frac{M_{y33}}{M_u} \right] \leq \phi M_{y33}; \]  
(CSA 13.6 b)

when, \( M_u \leq 0.67 M_{y33} \),  
(CSA 13.6 b)

\[ M_{r33} = \phi M_u. \]  
(CSA 13.6 b)

3.6 Bending Checks

This section describes how the program checks bending for CSA S16-09 design.

3.6.1 Bending Check Locations

For each design load combination the program checks bending at the following locations:

- Point of maximum moment for the design load combination considered.
- Point load locations for the design load combination considered.
3.6.2 Bending Check at Point of Maximum Moment

For beams with no axial load, or when axial loads are not considered, the program uses the following equation to perform bending checks for both composite and non-composite beams. If there is axial load to be considered, the interaction formulas described in the section entitled Steel Section Alone in this chapter are used rather than this equation.

\[ \frac{M_f}{M_r} \leq 1.0 \]  \hspace{1cm} (AISC B3-1)

where,

- \( M_f \) = The maximum required flexural strength, that is, the maximum applied factored moment, N-mm.
- \( M_r \) = Moment resistance for full composite connection or partial composite connection, as applicable, N-mm.

The program check does not include minor axis bending moment and axial force for composite section. However, if the beam is found to be non-composite, a more rigorous approach is used to check the section.

3.6.3 Bending Check at Point Loads

The bending check at point load locations is ensured by checking the number of shear connectors between the point of zero moment and the point load.

3.7 Steel Anchors

This section begins by defining the program's default allowable shear connector loads for CSA S16-09 composite beam design. Shear connector capacities are defined for both shear studs and channel shear connectors. Next the equations used for determining the number of shear connectors on the beam are provided.
3.7.1 Steel Headed Stud Anchor

The capacity for a single steel headed stud anchor is calculated using the following equation:

\[ q_{rs} = 0.5A_{sc} \sqrt{f'_{c} E_c} \leq A_{sc} F_u \]  
(CSA 17.7.2)

For ribbed slabs with the ribs parallel to the beam,

(a) when \( 3.0 > \frac{w_d}{h_d} \geq 1.50 \)

\[ q_{rr} = q_{rs} \left[ 0.75 + 0.167 \left( \frac{w_d}{h_d} - 1.5 \right) \right] \leq q_{rs} \]

(b) when \( \frac{w_d}{h_d} < 1.50 \)

\[ q_{rr} = \left[ 0.92 \frac{w_d}{h_d} dh \left( f'_{c} \right)^{0.2} \right] \leq 0.75q_{rs} \]  
(CSA 17.7.2)

where

\( s \) = Longitudinal stud spacing

For ribbed slabs with the ribs perpendicular to the beam,

(a) when \( h_d = 75 \text{ mm} \)

\[ q_{rr} = 0.35 \rho A_p \sqrt{f'_{c}} \leq q_{rs} \]

(b) when \( h_d = 38 \text{ mm} \)

\[ q_{rr} = 0.61 \rho A_p \sqrt{f'_{c}} \leq q_{rs} \]

where

\( A_p \) = concrete pullout area, taking the deck profile and stud burnoff into account. For a single stud, the apex of the pyramidal pullout area, with four sides sloping at 45°, shall be taken as the center of the top surface of the head of the stud. For a pair of studs, the pullout area has a ridge extending from stud to stud.
\[ \rho = 1.0 \text{ for normal-density concrete (2,150 to 2,500 kg/m}^3) \]
\[ = 0.85 \text{ for semi-low density concrete (1,850 to 2,150 kg/m}^3) \]

The terms \( f'_c \) and \( E_c \) can be different on the two sides of the beam. The program calculates \( q_{rs} \) for each side of the beam separately using the preceding equation and uses the smaller value in the calculations.

### 3.7.2 Steel Channel Anchors

The capacity for channel shear connectors is calculated using the following equation,

\[ q_{rs} = 36.5 \left( t + 0.5w \right) L_c \sqrt{f'_c} \]

The equation is based on CSA S16-09 specifications 17.7.2.4.

Because the program does not allow channel shear connectors to be used with formed metal deck, there is no reduction factor that needs to be applied to the value of \( q_{rs} \) calculated using the preceding equation.

The terms \( f'_c \) can be different on the two sides of the beam. The program calculates \( q_{rs} \) for each side of the beam separately using the preceding equation and uses the smaller value in the calculations.

### 3.7.3 Horizontal Shear for Full Composite Connection

The total horizontal shear to be resisted between the point of maximum positive moment (where the concrete is in compression) and the points of zero moment for full composite connection, \( \sum Q_{n-100}^c \), is given by the smaller of \( \sum Q_{n-100}^c \) and \( \sum Q_{n-100}^s \) as applicable.

The total maximum horizontal shear that can develop due to crushing of concrete, \( \sum Q_{n-100}^c \), is given by

\[ \sum Q_{n-100}^c = \alpha_1 f'_c \text{left} A_c \text{left} + \alpha_1 f'_c \text{right} A_c \text{right} \]

The total maximum horizontal shear that can be developed due to tensile yielding of the steel section, \( \sum Q_{n-100}^s \), is given by
\[
\sum Q_{n-100}^s = A_c F_y + b_{sp} t_{sp} F_{yp} \quad \text{(Rolled Shape)}
\]
\[
\sum Q_{n-100}^w = b_{f-top} t_{f-top} F_{yf-top} + h t_w F_{yw} + b_{f-bot} t_{f-bot} F_{yf-bot} + b_{sp} t_{sp} F_{yp} \quad \text{(Welded)}
\]

In the preceding equations,

\( A_c \) = Area of concrete slab within the effective width. It may include the rib area if the rib is parallel to the beam, in².

\( A_s \) = Area of steel cross-section, in².

### 3.7.4 Number of Shear Connectors

#### 3.7.4.1 Between Maximum Moment and Point of Zero Moment

For full composite action, the number of shear connectors between a point of maximum positive or negative moment and adjacent points of zero moment, \( N_1 \), is given as follows:

\[
N_1 = \frac{\sum Q_{n-100}}{Q_n}.
\]

In the preceding equation, \( \sum Q_{n-100} \) is as determined in the previous section entitled Horizontal Shear for Full Composite Connection, and \( Q_a \) is determined as described in the previous subsections.

For partial composite connection, the number of shear connectors between a point of maximum positive (not negative) moment and adjacent points of zero moment, \( N_1 \), is given as follows:

\[
N_1 = \frac{\sum Q_{n-PCC}}{Q_n}
\]

In the preceding equation, \( \sum Q_{n-PCC} \) is equal to the percent composite connection times \( \sum Q_{n-100} \). For example, if there is 70% composite connection, \( \sum Q_{n-PCC} = 0.7 \sum Q_{n-100} \). Thus, the percent composite connection, \( p \), for CSA S16-09 design is given as follows:
3.7.4.2 Between the Point Load and the Point of Zero Moment

The program uses the following equation to check that the number of shear connectors provided between a point load and a point of zero moment is sufficient. This equation is not specified by CSA but is used by CSI as the LRFD equivalent of Equation I4-5 in the AISC-ASD89 specification.

\[ N_2 = N_1 \left( \frac{M_f - M_{\text{steel alone}}}{M_{\text{comp}} - M_{f \text{ steel alone}}} \right) \]

In the preceding equation,

- \( M_{\text{comp}} \) = Maximum moment resistance of the composite beam, considering partial composite connection if applicable, N-mm.
- \( M_{\text{steel alone}} \) = Moment resistance of the steel beam alone, N-mm.
- \( M_f \) = Moment at the point load location, N-mm.
- \( N_1 \) = Number of shear connectors required between the point of maximum moment and the point of zero moment, or the end of the slab, unitless.
- \( N_2 \) = Number of shear connectors required between the point load considered and the point of zero moment, or the end of the slab, unitless.

This equation is checked at each point load location.

3.8 Beam Shear Capacity

This section describes how the program calculates the allowable shear stress for CSA S16-09 composite beam design.
3.8.1 Shear Capacity

The factored shear strength, $V_{r2}$, for major direction shears in I-shapes and channels is evaluated as follows (CSA 13.4.1.1):

- For $\frac{h}{t_w} \leq 439 \sqrt[3]{\frac{k_w}{F_y}}$,
  \[ V_{r2} = \varphi A_w \left\{ 0.66 F_y \right\} \quad \text{(CSA 13.4.1.1)} \]

- For $439 \sqrt[3]{\frac{k_w}{F_y}} < \frac{h}{t_w} \leq 502 \sqrt[3]{\frac{k_w}{F_y}}$,
  \[ V_{r2} = \varphi A_w \left\{ 290 \frac{\sqrt{\frac{k_w}{F_y}}}{h/t_w} \right\} \quad \text{(CSA 13.4.1.1)} \]

- For $502 \sqrt[3]{\frac{k_w}{F_y}} < \frac{h}{t_w} \leq 621 \sqrt[3]{\frac{k_w}{F_y}}$,
  \[ V_{r2} = \varphi A_w \left\{ F_{cri} + F_t \right\}, \quad \text{where} \quad \text{(CSA 13.4.1.1)} \]
  \[ F_{cri} = \left\{ 290 \frac{\sqrt{\frac{k_w}{F_y}}}{h/t_w} \right\}, \quad \text{and} \]
  \[ F_t = \left( 0.6F_y - 0.866 F_{cri} \right) \left\{ \frac{1}{\sqrt{1 + \left( \frac{a/h}{h} \right)^2}} \right\}. \]

  Assuming no stiffener is used, the value of $F_t$ is taken as zero.

- For $\frac{h}{t_w} > 621 \sqrt[3]{\frac{k_w}{F_y}}$,
  \[ V_{r2} = \varphi A_w \left\{ F_{cre} + F_t \right\} \quad \text{(CSA 13.4.1.1)} \]
The required shear strength, that is, the applied factored shear, $N$. 

$F_{c,e} = \frac{180000k_v}{(h/t_w)^2}$

In the preceding equations, $k_v$ is the shear buckling coefficient, and it is defined as:

$$k_v = 4 + \frac{5.34}{(a/h)^2} \quad \text{for} \quad a/h < 1$$  \hspace{1cm} (CSA 13.4.1.1)

$$k_v = 5.34 + \frac{4}{(a/h)^2} \quad \text{for} \quad a/h \geq 1$$  \hspace{1cm} (CSA 13.4.1.1)

and the aspect ratio is the ratio of the distance between the stiffeners to web depth. Assuming no stiffener is used, the value of $k_v$ is taken as 5.34.

Note that in preceding equations, $A_w$, the area of the web, is calculated as shown in the following equation, where $C_{\text{top}}$ and $C_{\text{bot}}$ are the depths of copes, if any, at the top and bottom of the beam section.

$$A_w = (d - C_{\text{top}} - C_{\text{bot}}) t_w.$$  

### 3.8.2 Checking the Beam Shear

The program checks the beam shear at the ends of the beam using the following equation.

$$\frac{V_f}{V_r} \leq 1.0$$  \hspace{1cm} (CSA 13.4.1.1)

where,

$V_f$ = The required shear strength, that is, the applied factored shear, $N$. 

$V_r$ = Shear resistance, $N$. 

3 - 38 Beam Shear Capacity
3.8.3 Limitations of Beam Shear Check

Following are some limitations of the program's beam shear check for composite beams.

- No check is made for shear on the net section considering the bolt holes.
- No check is made for shear rupture on a beam with the top flange coped as described in CSA S16-09 specification.
- Beam shear is checked at the ends of the beam only. In unusual cases, where some of the load cases act downward and some act upward, the maximum shear may occur elsewhere. For example, consider a beam that has a uniform load acting downward over its entire length and a single concentrated load acting upward at the center. Assume that the magnitude of the upward concentrated load is equal to the magnitude of the uniform load times its length. In that case, the end reactions are zero, and the maximum shear occurs at the center of the beam. The program will check the shear at the ends of the beam in this case but not at the center.

3.9 Deflection Check

Deflection is calculated as described in the section entitled Beam Deflection and Camber in Chapter 2. For full composite connection $I_r$ is used in the deflection calculations. For partial composite connection $I_{eff}$ is used in the deflection calculations.

3.10 Beam Tension Flange Stress Check

When the beam is not shored and is designed as composite, the program checks that the tension stress in the beam bottom flange remains in the elastic range per CSA Clause 17.11. This tension stress is computed as the sum of:

- the stresses caused by dead loads acting on the steel section alone before the concrete has hardened

$$f_1 = \frac{M_{\text{dead construction}}}{S_x}$$
The stresses caused by the remaining load acting on the composite section. These stresses are computed based on the elastic section moment modulus $S_{tr}$ computed assuming full composite action.

$$f_2 = \frac{M_{\text{superimposed dead}} + M_{\text{live}}}{S_{tr}}$$

While the above equation underestimates stresses when the composite action is partial only, it is the one used in the composite beam design example provided in the CISC Handbook of Steel Construction 10th Edition.

The total stress is the sum of $f_1 + f_2$ and it must be less than $F_y$.

### 3.11 Floor Vibration

For CSA S16-09, by default the program performs the floor vibration check in accordance with AISC Steel Design Guide 11 (DG11). The program calculates the first natural vibration frequency, estimated peak acceleration (in units of g), $a_p/g$, and acceleration limit, $a_o/g$, for each beam and reports this information to determine the adequacy of a composite beam section.

The acceleration limit of any floor system can be achieved by limiting the vibration characteristics of beams or girders. The program optimize the floor vibration by limiting the estimated peak acceleration of each individual beam only. Please refer to *Floor Vibration* in Chapter 2 for more information.
Appendix A
Preferences

The composite beam design preferences are basic assignments that apply to all composite beams. Default values are provided for all composite beam design preference items. Thus, it is not necessary to specify or change any of the preferences. However, at least review the default values for the preference items to make sure they are acceptable.

A1 Beam Tab

Table A1 lists the composite beam preference items available on the Beam tab in the Preferences form.

<table>
<thead>
<tr>
<th>Item</th>
<th>Possible Values</th>
<th>Default Value</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>Shored?</td>
<td>Yes/No</td>
<td>No</td>
<td>Toggle for shored or unshored construction.</td>
</tr>
<tr>
<td>Middle Range (%)</td>
<td>≥ 0%</td>
<td>70%</td>
<td>Length in the middle of the beam over which the program checks the effective width on each side of the beam, expressed as a percentage of the total beam length.</td>
</tr>
<tr>
<td>Pattern Live Load Factor</td>
<td>≥ 0</td>
<td>0.75</td>
<td>Factor applied to live load for special pattern live load check for cantilever back spans and continuous spans.</td>
</tr>
<tr>
<td>Stress Ratio Limit</td>
<td>&gt;0</td>
<td>1.0</td>
<td>The acceptable stress ratio limit. This item applies to design optimization only.</td>
</tr>
</tbody>
</table>
### A2 Shear Studs Tab

Table A2 lists the composite beam preference items available on the Shear Studs tab in the Preferences form.

<table>
<thead>
<tr>
<th>Item</th>
<th>Possible Values</th>
<th>Default Value</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>Minimum PCC (%)</td>
<td>&gt; 0</td>
<td>40</td>
<td>Minimum percent composite connection applied to the beams which require com-</td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td>posite action to meet strength or deflection criteria. This percentage also</td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td>applies to beams for which Force Composite is specified in the Overwrites.</td>
</tr>
<tr>
<td>Maximum PCC(%)</td>
<td>&gt; 0</td>
<td>100</td>
<td>Maximum percent composite connection for the beams.</td>
</tr>
<tr>
<td>Single Segment?</td>
<td>Yes/No</td>
<td>No</td>
<td>Toggle for placement of steel headed stud anchors in a single segment. To</td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td>place studs in a single segment with uniform spacing throughout the beam,</td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td>select Yes. This factor has no effect on checking beams with user defined</td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td>studs.</td>
</tr>
<tr>
<td>Min. Long. Spacing</td>
<td>&gt; 0</td>
<td>6(d_s)</td>
<td>Minimum longitudinal spacing of shear studs along the length of the beam.</td>
</tr>
<tr>
<td></td>
<td></td>
<td>(i.e., six stud diameters)</td>
<td></td>
</tr>
<tr>
<td>Max. Long. Spacing</td>
<td>&gt; 0</td>
<td>1000 mm</td>
<td>Maximum longitudinal spacing of shear studs along the length of the beam.</td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td>This setting applies to all beams composite or non-composite unless &quot;NonComposition w/o Studs&quot; is specified in the overwrites.</td>
</tr>
<tr>
<td>Min. Trans. Spacing</td>
<td>&gt; 0</td>
<td>4(d_s)</td>
<td>Minimum transverse spacing of shear studs across the beam flange.</td>
</tr>
<tr>
<td></td>
<td></td>
<td>(i.e., four stud diameters)</td>
<td></td>
</tr>
<tr>
<td>Max. Studs per Row</td>
<td>&gt;0</td>
<td>3</td>
<td>Maximum number of shear studs in a single row across the beam flange.</td>
</tr>
</tbody>
</table>
## A3 Camber Tab

Table A3 lists the composite beam preference items available on the Camber tab in the Preferences form.

<table>
<thead>
<tr>
<th>Item</th>
<th>Possible Values</th>
<th>Default Value</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>Calculate Camber?</td>
<td>Yes/No</td>
<td>Yes</td>
<td>Toggle for whether or not beams have a camber.</td>
</tr>
<tr>
<td>Camber DL, %</td>
<td>≥0</td>
<td>80</td>
<td>Percent of dead load (not including superimposed dead load) on which camber calculations are based.</td>
</tr>
<tr>
<td>Minimum Beam Depth for Camber</td>
<td>≥0</td>
<td>340 mm</td>
<td>Actual (not nominal) beam depth below which beams are never cambered.</td>
</tr>
<tr>
<td>Minimum Web Thick. for Camber</td>
<td>≥0</td>
<td>6 mm</td>
<td>Web thickness below which beams are never cambered.</td>
</tr>
<tr>
<td>Minimum Beam Span for Camber</td>
<td>≥0</td>
<td>7 m</td>
<td>Minim beam span below which beams are never cambered.</td>
</tr>
<tr>
<td>Minimum Camber, abs.</td>
<td>≥0</td>
<td>15 mm</td>
<td>The limiting number in the current unit. If the calculated camber falls below this limit, the required camber will be reported as zero.</td>
</tr>
<tr>
<td>Minimum Camber, L/</td>
<td>&gt; 0</td>
<td>900</td>
<td>The minimum camber limitation denominator. Inputting a value of 360 means that the maximum camber limit is L/360. If the calculated camber falls below this limit, the required camber will be reported as zero.</td>
</tr>
<tr>
<td>Camber Abs Max Limit</td>
<td>&gt;0</td>
<td>150 mm</td>
<td>The absolute maximum camber in the current unit. If the calculated camber is larger than this limit, the required camber will be reported as this limiting value.</td>
</tr>
<tr>
<td>Camber Max Limit, L/</td>
<td>&gt;0</td>
<td>180</td>
<td>The maximum camber limitation denominator. Inputting a value of 360 means that the maximum camber limit is L/360. If the calculated camber is larger than this limit, the required camber will be reported as this limiting value.</td>
</tr>
<tr>
<td>Camber Increment</td>
<td>&gt;0</td>
<td>5</td>
<td>The camber interval in the current unit. The camber is reported as an integer multiple of the interval. This is used for rounding purposes only.</td>
</tr>
</tbody>
</table>
Table A3: Composite Beam Preferences on the Camber Tab

<table>
<thead>
<tr>
<th>Item</th>
<th>Possible Values</th>
<th>Default Value</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>Camber Rounding Down</td>
<td>Yes/No</td>
<td>Yes</td>
<td>Camber rounding procedure. If Yes is selected, camber is rounded down consistently to the next level; else camber is rounded to the nearest level.</td>
</tr>
</tbody>
</table>

See the section entitled *Beam Deflection and Camber* in Chapter 2 for a description of beam deflection and camber.

A4 Deflection Tab

Table A4 lists the composite beam preference items available on the Deflection tab in the Preferences form.

Table A4: Composite Beam Preferences on the Deflection Tab

<table>
<thead>
<tr>
<th>Item</th>
<th>Possible Values</th>
<th>Default Value</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>PreComp DL Limit, L/</td>
<td>≥0</td>
<td>0</td>
<td>Pre-composite dead load deflection limitation denominator. Inputting a value of 120 means that the deflection limit is L/120. Inputting zero is special, since it means no check has to be made for this item.</td>
</tr>
<tr>
<td>Super DL+LL Limit, L/</td>
<td>≥0</td>
<td>240</td>
<td>Post-composite superimposed dead plus live load deflection limitation denominator. Inputting a value of 120 means that the deflection limit is L/120. Inputting zero is special, since it means no check has to be made for this item.</td>
</tr>
<tr>
<td>Live Load Limit, L/</td>
<td>≥0</td>
<td>360</td>
<td>Live load deflection limitation denominator. Inputting a value of 360 means that the deflection limit is L/360. Inputting zero is special, since it means no check has to be made for this item.</td>
</tr>
<tr>
<td>Total Camber Limit, L/</td>
<td>≥0</td>
<td>240</td>
<td>Net load deflection (total deflection minus camber) limitation denominator. Inputting a value of 240 means that the deflection limit is L/240. Inputting zero is special, since it means no check has to be made for this item. Camber is subtracted from the total load deflection before checking.</td>
</tr>
</tbody>
</table>
## Appendix A - Preferences

### Table A4: Composite Beam Preferences on the Deflection Tab

<table>
<thead>
<tr>
<th>Item</th>
<th>Possible Values</th>
<th>Default Value</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>Creep Factor</td>
<td>≥1</td>
<td>1.15</td>
<td>The factor that accounts for the increase in deflection due to creep of concrete. It affects deflection calculation only (see CSA Section 17.3.1).</td>
</tr>
<tr>
<td>Free Shrinkage Strain</td>
<td>≥0</td>
<td>0.000583</td>
<td>Free shrinkage strain of the concrete used in the decks. This affects deflection due to shrinkage.</td>
</tr>
<tr>
<td>Strain Ec Chi Factor</td>
<td>&gt;0</td>
<td>0.73</td>
<td>Aging coefficient of concrete. This affects deflection due to shrinkage.</td>
</tr>
<tr>
<td>Strain Ec Phi Factor</td>
<td>&gt;0</td>
<td>2.7</td>
<td>Creep coefficient of concrete. This affects deflection due to shrinkage.</td>
</tr>
</tbody>
</table>

See the section entitled *Beam Deflection and Camber* in Chapter 2 for a description of beam deflection and camber.

### A5 Vibration Tab

Table A5 lists the composite beam preference items available on the Vibration tab in the Preferences form.

### Table A5: Composite Beam Preferences on the Vibration Tab

<table>
<thead>
<tr>
<th>Item</th>
<th>Possible Values</th>
<th>Default Value</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>Vibration Criterion</td>
<td>Walking, Rhythmic,</td>
<td>Walking</td>
<td>Vibration criterion to be considered in design.</td>
</tr>
<tr>
<td></td>
<td>Sensitive Equipment, None</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Occupancy Category</td>
<td>Paper Office,</td>
<td>Paper Office</td>
<td>Occupancy category to be considered in the design. Selecting this item changes the default parameters for the damping ratio (DG11 Table 4.1) and vibrational acceleration due to gravity $a_0/g$ (DG11 Table 4.1). However, the default parameters can be changed here.</td>
</tr>
<tr>
<td></td>
<td>Electronics Office,</td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td>Residential</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Damping Ratio</td>
<td>&gt; 0</td>
<td>0.0250</td>
<td>Damping ratio of the system (DG11 Table 4.1, DG11 Section 5.2).</td>
</tr>
</tbody>
</table>
Table A5: Composite Beam Preferences on the Vibration Tab

<table>
<thead>
<tr>
<th>Item</th>
<th>Possible Values</th>
<th>Default Value</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>Acceleration Limit, (a_0/g) &gt; 0%</td>
<td>&gt; 0%</td>
<td>0.005</td>
<td>Vibrational acceleration limit as a fraction of acceleration due to gravity, (a_0/g) for walking excitation (DG11 Table 4.1).</td>
</tr>
</tbody>
</table>

See *Floor Vibration* in Chapter 2 for a description of beam vibration.

A6  **Price Tab**

Table A6 lists the composite beam preference items available on the Price tab in the Preferences form.

Table A6: Composite Beam Preferences on the Price Tab

<table>
<thead>
<tr>
<th>Item</th>
<th>Possible Values</th>
<th>Default Value</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>Optimize for Price?</td>
<td>Yes/No</td>
<td>No</td>
<td>Toggle to consider price rather than steel weight when selecting the optimum beam section from an auto select section list.</td>
</tr>
<tr>
<td>Steel Price ($)</td>
<td>≥ 0</td>
<td>$1 per pound</td>
<td>Price of steel per unit weight of steel beam (including cover plate if it exists).</td>
</tr>
<tr>
<td>Stud Price ($)</td>
<td>≥ 0</td>
<td>$0</td>
<td>Installed price for a single shear stud connector.</td>
</tr>
<tr>
<td>Camber Price ($)</td>
<td>≥ 0</td>
<td>$0</td>
<td>Camber price per unit weight of steel beam (including cover plate, if it exists).</td>
</tr>
</tbody>
</table>

See "*How the Program Optimizes Design Groups*" in Chapter 2 for additional information on the "Optimize for Price?" item.

A7  **Factors Tab**

Table A7 lists the preference items available for phi factors in AISC 306-10 design. Some of these phi factors are specified by the AISC specification. Others have been created by CSI to give more control over the capacities for the composite section. Note that the default value for all of the phi factors specifically created by CSI (and not specified by AISC) is 0.9, the same as the \(\phi\) factors for flexure (AISC I3.2a, G1) and thus by default they have no effect on the design.
<table>
<thead>
<tr>
<th>Item</th>
<th>Possible Values</th>
<th>Default Value</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>Phi-concrete</td>
<td>&gt;0</td>
<td>0.65</td>
<td>Resistance factor applied to concrete strength for computing beam flexural and axial capacities.</td>
</tr>
<tr>
<td>Phi-steel</td>
<td>&gt; 0</td>
<td>0.9</td>
<td>Resistance factor applied to steel strength for computing beam flexural, shear and axial capacities.</td>
</tr>
<tr>
<td>Phi-rebar</td>
<td>&gt; 0</td>
<td>0.85</td>
<td>Resistance factor applied to rebar yield strength for computing beam flexural and axial capacities.</td>
</tr>
<tr>
<td>Phi-connector</td>
<td>&gt; 0</td>
<td>0.8</td>
<td>Resistance factor applied to steel shear connector for computing beam flexural capacity.</td>
</tr>
<tr>
<td>Reaction Factor</td>
<td>&gt; 0</td>
<td>1.0</td>
<td>The reported reaction forces are multiplied by this factor. Specifying 1 in the overwrites means that the program calculated load-factored end reaction forces is to be reported.</td>
</tr>
</tbody>
</table>

Refer to the sections mentioned in the Description column of the table for more information.
Appendix B
Overwrites

The composite beam design overwrites are basic assignments that apply only to those composite beams to which they are assigned. Default values are provided for all composite beam overwrite items. Thus, it is not required that any of the overwrites be changed. However, at least review the default values for the overwrite items to make sure they are acceptable. When changes are made to overwrite items, the program applies the changes only to the elements to which they are specifically assigned; that is, to the elements that are selected when the overwrites are changed.

B1 Beam

Table B-1 lists the composite beam overwrite items available.

<table>
<thead>
<tr>
<th>Item</th>
<th>Possible Values</th>
<th>Default Value</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>Restrict Beam Depth?</td>
<td>Yes/No</td>
<td>No</td>
<td>Toggle to select if the beam depth is to be considered in an auto select section list. If yes, maximum and minimum depths must be input.</td>
</tr>
</tbody>
</table>
### Table B-1: Composite Beam Overwrites

<table>
<thead>
<tr>
<th>Item</th>
<th>Possible Values</th>
<th>Default Value</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>Maximum Depth</td>
<td>&gt; 0</td>
<td>1100 mm</td>
<td>Maximum actual (not nominal) beam depth to be considered in an auto select section list.</td>
</tr>
<tr>
<td>Minimum Depth</td>
<td>≥ 0</td>
<td>0</td>
<td>Minimum actual (not nominal) beam depth to be considered in auto select section list.</td>
</tr>
<tr>
<td>Restrict Beam Width?</td>
<td>Yes/No</td>
<td>No</td>
<td>Toggle to select if the beam width is to be considered in an auto select section list. If yes, maximum and minimum width must be input.</td>
</tr>
<tr>
<td>Maximum Depth</td>
<td>&gt; 0</td>
<td>460 mm</td>
<td>Maximum actual beam width to be considered in an auto select section list.</td>
</tr>
<tr>
<td>Minimum Width</td>
<td>≥ 0</td>
<td>0</td>
<td>Minimum actual beam width to be considered in auto select section list.</td>
</tr>
<tr>
<td>Shored Construction?</td>
<td>Yes/No</td>
<td>No (unshored)</td>
<td>Toggle for shored or unshored construction.</td>
</tr>
<tr>
<td>Beam Fy</td>
<td>≥ 0</td>
<td>Specified in Material Properties</td>
<td>Yield stress of the beam, $F_y$. Specifying 0 in the overwrites means that $F_y$ is as specified in the material properties</td>
</tr>
<tr>
<td>Beam Fu</td>
<td>≥ 0</td>
<td>Specified in Material Properties</td>
<td>Minimum tensile strength of the beam, $F_u$. Specifying 0 means that $F_u$ is as specified in the material properties</td>
</tr>
<tr>
<td>Cover Plate Present?</td>
<td>Yes/No</td>
<td>No</td>
<td>Toggle switch indicating if a full length cover plate exists on the bottom of the beam bottom flange.</td>
</tr>
<tr>
<td>Plate width</td>
<td>≥ 0</td>
<td>0</td>
<td>Width of cover plate, $b_{cp}$.</td>
</tr>
<tr>
<td>Plate thickness</td>
<td>≥ 0</td>
<td>0</td>
<td>Thickness of cover plate, $t_{cp}$.</td>
</tr>
<tr>
<td>Plate Fy</td>
<td>&gt; 0</td>
<td>0</td>
<td>Cover plate yield stress, $F_{ycp}$. Specifying 0 means that $F_{ycp}$ is set to that specified in the beam material properties</td>
</tr>
</tbody>
</table>

The Shored item affects both the deflection calculations and the flexural stress calculations for the beam. See the section entitled *Beam Deflection and Camber* in Chapter 2 for a description of beam deflection. If the beam is shored, no checks are performed for the construction loading design load combination.
Typically, when a beam is designed using the Composite Beam Design postprocessor that beam is designed as a composite beam if it has a deck section (not slab section) assigned along the full length of the specified Middle Range on at least one side of the beam.

When a beam is designed as non-composite with minimum shear studs, the beam is designed as a non-composite beam. Then steel stud anchors are specified for the beam with as large a spacing as possible, without exceeding the specified maximum longitudinal spacing. The maximum longitudinal spacing can be overwritten on the Steel Stud Anchor tab.

See *Effective Width of the Concrete Slab* in Chapter 2 for a description of the beam effective width.

The beam yield stress and the cover plate yield stress both default to the yield stress specified for the material property associated with the beam section.

In this program, the cover plate can have a yield stress that is different from that of the beam, if desired. See "Cover Plates" in the section entitled *Composite Beam Properties* in Chapter 2 for a description of cover plates.

### B2 Bracing (C) and Bracing

Tables B-2a, B-2b, and B-2c list the composite beam overwrite items available for bracing.

<table>
<thead>
<tr>
<th>Table B-2a: First Two Composite Beam Overwrite Items</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>Item</strong></td>
</tr>
<tr>
<td>Omega2 factor</td>
</tr>
<tr>
<td>Bracing Condition</td>
</tr>
</tbody>
</table>
When the $\omega_2$ factor is program calculated, the program uses the following equation to calculate it unless the user has specified the Bracing Condition as Length Specified.

$$\omega_2 = \frac{4M_{\text{max}}}{\sqrt{M_{\text{max}}^2 + 4M_a^2 + 7M_b^2 + 4M_c^2}} \leq 2.5.$$  (CSA 13.6 (a))

where,

- $M_{\text{max}} = $ maximum factored bending moment in unbraced segment
- $M_a = $ factored bending moment at one-quarter point of unbraced segment
- $M_b = $ factored bending moment at midpoint of unbraced segment
- $M_c = $ factored bending moment at three-quarter point of unbraced segment

The numeric value of $\omega_2$ is 1.0 for cantilever overhangs.

When the $\omega_2$ factor is program calculated and the Bracing Condition is set in the overwrites to Length Specified, the program uses 1.0 for $\omega_2$.

When the Bracing Condition is specified as Program Calculated, the program assumes the beam is braced as described in Determination of the Braced Points of a Beam in the section entitled Beam Unbraced Length and Design Check Locations in Chapter 2. Note that the program automatically considers the bracing for construction loading and for the final condition separately. For the construction loading condition, the program assumes that the concrete fill does assist in bracing the beam.

When the Bracing Condition is specified as Bracing Specified, two additional items may be specified in addition to those shown in Table B-2a. The two additional items are shown in Table B-2b.

<table>
<thead>
<tr>
<th>Item</th>
<th>Possible Values</th>
<th>Default Value</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>No. Point Braces</td>
<td>$\geq 0$</td>
<td>0</td>
<td>The number of user specified point brace locations. Clicking in this box opens the Point Braces form, which can be used to specify point braces.</td>
</tr>
</tbody>
</table>
Table B-2b: Additional Composite Beam Overwrite Items When the Bracing Condition Is Specified as Bracing Specified

<table>
<thead>
<tr>
<th>Item</th>
<th>Possible Values</th>
<th>Default Value</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>No. Uniform Braces</td>
<td>≥ 0</td>
<td>0</td>
<td>The number of user specified uniform braces. Clicking in this box opens the Uniform Braces form, which can be used to specify the uniform braces.</td>
</tr>
</tbody>
</table>

The No. Point Braces and No. Uniform Braces items allows specification of the actual bracing for the beam. These items are described in User-Specified Uniform and Point Bracing in Beam Unbraced Length and Design Check locations in Chapter 2.

When the Bracing Condition is specified as Length Specified, two items may be specified in addition to those shown in Table B2a. The two additional items are shown in Table B2c.

Table B2c: Additional Composite Beam Overwrite Items When the Bracing Condition Is Specified as Length Specified

<table>
<thead>
<tr>
<th>Item</th>
<th>Possible Values</th>
<th>Default Value</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>Absolute Length?</td>
<td>Yes/No</td>
<td>No</td>
<td>Toggle switch for whether the maximum unbraced length is given as an absolute length or a relative length.</td>
</tr>
<tr>
<td>Unbraced L22</td>
<td>≥ 0 and ≤ beam length</td>
<td>Length of beam</td>
<td>Maximum unbraced length for buckling about the beam local 2 axis.</td>
</tr>
</tbody>
</table>

When the maximum unbraced length is specified as an absolute length, the actual maximum unbraced length is specified. When the maximum unbraced length is specified as a relative length, the value specified is equal to the maximum unbraced length divided by the length of the beam. The relative length specified is always between 0 and 1, inclusive.

See Beam Unbraced Length and Design Check Locations for additional information about the unbraced length of the beam.

B3 Deck

Table B-3 lists the composite beam overwrite items available for the Deck.
Table B-3: Composite Beam Overwrites for the Deck

<table>
<thead>
<tr>
<th>Item</th>
<th>Possible Values</th>
<th>Default Value</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>Deck ID Left</td>
<td>Program calculated, any defined deck property, or None</td>
<td>Program calculated</td>
<td>Deck ID assigned to left side of beam.</td>
</tr>
<tr>
<td>Deck direction</td>
<td>Program calculated, parallel, or perpendicular</td>
<td>Program calculated</td>
<td>Span direction of the metal deck ribs on the left side of the beam relative to the span direction of the beam.</td>
</tr>
<tr>
<td>b-eff left</td>
<td>Program calculated or user-defined</td>
<td>Program calculated</td>
<td>Toggle specifying how the effective width of the concrete slab on the left side of the beam is determined</td>
</tr>
<tr>
<td>b-eff left</td>
<td>$\geq 0$</td>
<td>Program calculated</td>
<td>User defined effective width of concrete slab on the left side of beam, $\text{b}_{\text{eff left}}$.</td>
</tr>
<tr>
<td>Deck ID Right</td>
<td>Program calculated, any defined deck property, or None</td>
<td>Program calculated</td>
<td>Deck ID assigned to right side of beam.</td>
</tr>
<tr>
<td>Deck direction</td>
<td>Program calculated, parallel, or perpendicular</td>
<td>Perpendicular</td>
<td>Span direction of the metal deck ribs on the right side of beam relative to the span direction of beam</td>
</tr>
<tr>
<td>b-eff right</td>
<td>Program calculated or user-defined</td>
<td>Program calculated</td>
<td>Toggle specifying how the effective width of the concrete slab on the right side of the beam is determined</td>
</tr>
<tr>
<td>b-eff right</td>
<td>$\geq 0$</td>
<td>0</td>
<td>User defined effective width of concrete slab on the right side of the beam, $\text{b}_{\text{eff right}}$.</td>
</tr>
</tbody>
</table>

When the Deck ID is program calculated, the user must refer to the output data to determine what the program assumed for this item. It is not shown in the overwrites.

If the deck direction is program calculated, do not overlook the important note about deck orientation in *Multiple Deck Types or Directions Along the Beam Length* in the section *Effective Width of the Concrete Slab* in Chapter 2.
B4 Shear Studs

Table B-4 lists the composite beam overwrite items available for the Shear Studs.

**Table B-4: Composite Beam Overwrites for the Shear Studs**

<table>
<thead>
<tr>
<th>Item</th>
<th>Possible Values</th>
<th>Default Value</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>Beam Type</td>
<td>Composite, NC w studs, NC w/o studs, or Force Composite</td>
<td>Composite</td>
<td>Type of beam design. NC w studs is short for Noncomposite with minimum shear studs. NC w/o studs is short for Noncomposite without shear studs. Force Composite is short for always design with composite action.</td>
</tr>
<tr>
<td>Minimum PCC (%)</td>
<td>&gt; 0</td>
<td>40</td>
<td>Minimum value of percent composite connection applied to beams which require composite action to meet strength or deflection design criteria. This percentage also applies to beams for which &quot;Force Composite&quot; is specified.</td>
</tr>
<tr>
<td>Maximum PCC(%)</td>
<td>&gt; 0</td>
<td>100</td>
<td>Maximum percent composite connection considered for the beam.</td>
</tr>
<tr>
<td>User Pattern?</td>
<td>Yes/No</td>
<td>No</td>
<td>Toggle to indicate if a user defined steel headed stud anchor pattern is defined.</td>
</tr>
<tr>
<td>Uniform Spacing</td>
<td>≥ 0</td>
<td>0, indicating there are no uniformly spaced connectors</td>
<td>Uniform spacing of steel headed stud anchors along the beam. There is one shear stud per row along the beam.</td>
</tr>
<tr>
<td>No. Additional Sections</td>
<td>≥ 0</td>
<td>0, indicating there are no additional connectors specified</td>
<td>Number of sections in which additional uniformly spaced steel headed stud anchors are specified. Clicking in this box opens the Additional Sections form, which can be used to specify the section length and the number of uniformly spaced steel headed anchors in the section.</td>
</tr>
</tbody>
</table>
Table B-4: Composite Beam Overwrites for the Shear Studs

<table>
<thead>
<tr>
<th>Item</th>
<th>Possible Values</th>
<th>Default Value</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>Single Segment?</td>
<td>Yes/No</td>
<td>No</td>
<td>Toggle for placement of steel headed stud anchors in a single segment. To place studs in a single segment with uniform spacing throughout the beam, select Yes. This factor has no effect on checking beams with user defined studs.</td>
</tr>
<tr>
<td>Max. Studs per Row</td>
<td>&gt;0</td>
<td>3</td>
<td>Maximum number of shear studs in a single row across the beam flange.</td>
</tr>
<tr>
<td>Q&lt;sub&gt;r&lt;/sub&gt;</td>
<td>Program calculated or &gt; 0</td>
<td>Program calculated</td>
<td>Capacity of a single shear stud. Specifying 0 in the overwrites means that this value is program calculated.</td>
</tr>
</tbody>
</table>

The program default value for the minimum longitudinal spacing of steel headed stud anchors along the length of the beam is six shear stud diameters. Note that this item is input as an absolute length, not as a multiplier on the stud diameter.

The program default value for the maximum longitudinal spacing of steel headed stud anchors along the length of the beam is 1000 mm. This item is taken as an absolute length by the program, not as a multiplier on the total slab thickness as required by the code. The code specifies that the maximum longitudinal spacing of steel headed stud anchors along the length of the beam shall not exceed eight times the total slab thickness (rib height, \( h_r \), plus the concrete slab above the metal deck, \( t_c \)) or 1000 mm. If the total slab thickness is less than 1000 mm/6 = 167mm, the program default value may be unconservative and should be revised.

The program default value for the minimum transverse spacing of steel headed stud anchors across the beam flange is four shear stud diameters. Note that this item is input as an absolute length, not as a multiplier on the stud diameter. See the section entitled Distribution of Steel Headed Stud Anchors on a Composite Beam in Chapter 2 for an additional description of how steel headed stud anchors are distributed on composite beams.

The “Max Studs per Row” item indicates the maximum number of steel headed stud anchors that is allowed in a row across the beam flange. For wider beams, the Min Tran Spacing item might indicate that more steel anchors could be ac-
commodated across the beam flange but the Max Studs per Row item will limit the number of studs in any row. See the section entitled Distribution of Steel Headed Stud Anchors on a Composite Beam in Chapter 2 for an additional description of how steel anchors are distributed on beams.

See Steel Headed Stud Connector in the section entitled Steel Anchors in Chapter 2 for a description of how the program calculates the allowable shear load for a single steel anchor. Note that when a $Q_r$ value is specified in the overwrites, the program assumes that the specified value of $Q_r$ has already been modified by any applicable reduction factors for the metal deck. Finally, note that specifying 0 (zero) in the overwrites for this item means that the allowable shear stud load is calculated by the program, not that it is zero.

Steel anchors are described in more detail in the sections entitled Distribution of Steel Headed Stud Anchors on a Composite Beam, Number of Shear Studs that Fit in a Composite Beam Segment, and User Defined Shear Connector Patterns in Chapter 2.

### B5 Deflection

Table B-5 lists the composite beam overwrite items available for Deflection.

**Table B5: Composite Beam Overwrites for Deflection**

<table>
<thead>
<tr>
<th>Item</th>
<th>Possible Values</th>
<th>Default Value</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>Deflection Check Type</td>
<td>Ratio, Absolute, Both</td>
<td>Ratio</td>
<td>Toggle to consider live load and total load deflection limitations as absolute or as divisor of beam length (relative).</td>
</tr>
<tr>
<td>PreComp DL Limit, L/</td>
<td>≥0</td>
<td>0</td>
<td>Pre-composite dead load deflection limitation denominator. Inputting a value of 120 means that the deflection limit is L/120. Inputting zero is special, since it means no check has to be made for this item.</td>
</tr>
<tr>
<td>Super DL+LL Limit, L/</td>
<td>≥0</td>
<td>240</td>
<td>Post-composite superimposed dead plus live load deflection limitation denominator. Inputting a value of 120 means that the deflection limit is L/120. Inputting zero is special, since it means no check has to be made for this item.</td>
</tr>
<tr>
<td>Item</td>
<td>Possible Values</td>
<td>Default Value</td>
<td>Description</td>
</tr>
<tr>
<td>------------------------------</td>
<td>-----------------</td>
<td>---------------</td>
<td>-----------------------------------------------------------------------------</td>
</tr>
<tr>
<td>Live Load Limit, (L/)</td>
<td>(\geq 0)</td>
<td>360</td>
<td>Live load deflection limitation denominator. Inputting a value of 360 means that the deflection limit is (L/360). Inputting zero is special, since it means no check has to be made for this item.</td>
</tr>
<tr>
<td>Total Camber Limit, (L/)</td>
<td>(\geq 0)</td>
<td>240</td>
<td>Net load deflection (total deflection minus camber) limitation denominator. Inputting a value of 240 means that the deflection limit is (L/240). Inputting zero is special, since it means no check has to be made for this item. Camber is subtracted from the total load deflection before checking.</td>
</tr>
<tr>
<td>PreComp DL Limit, abs</td>
<td>(\geq 0)</td>
<td>0</td>
<td>Deflection limitation for post-composite superimposed dead plus live load. For absolute deflection the input value is taken as it is. Inputting zero is special, since it means no check has to be made for this item.</td>
</tr>
<tr>
<td>Super DL+LL Limit, abs</td>
<td>(\geq 0)</td>
<td>Beam Span / 240</td>
<td>Deflection limitation for post-composite superimposed dead plus live load. For absolute deflection the input value is taken as it is. Inputting zero is special, since it means no check has to be made for this item.</td>
</tr>
<tr>
<td>Live Load Limit, abs</td>
<td>(\geq 0)</td>
<td>Beam Span / 360</td>
<td>Deflection limitation for live load. For absolute deflection the input value is taken as it is. Inputting zero is special, since it means no check has to be made for this item.</td>
</tr>
<tr>
<td>Total Camber Limit, abs</td>
<td>(\geq 0)</td>
<td>Beam Span / 240</td>
<td>Limitation for net deflection. Camber is subtracted from the total load deflection to get net deflection. For absolute deflection the input value is taken as it is. Inputting zero is special, since it means no check has to be made for this item.</td>
</tr>
<tr>
<td>Calculate Camber?</td>
<td>Yes/No</td>
<td>Yes</td>
<td>Toggle for the program to calculate beam camber.</td>
</tr>
<tr>
<td>Fixed Camber</td>
<td>(\geq 0)</td>
<td>0</td>
<td>User specified camber when the program does not calculate beam camber.</td>
</tr>
</tbody>
</table>
Table B5: Composite Beam Overwrites for Deflection

<table>
<thead>
<tr>
<th>Item</th>
<th>Possible Values</th>
<th>Default Value</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>Free Shrinkage Strain</td>
<td>≥0</td>
<td>0.000583</td>
<td>The factor that accounts for the increase in deflection due to creep of concrete. It affects deflection calculation only (see CSA Section 17.3.1).</td>
</tr>
<tr>
<td>Strain Ec Chi Factor</td>
<td>&gt;0</td>
<td>0.73</td>
<td>Free shrinkage strain of the concrete used in the decks. This affects deflection due to shrinkage.</td>
</tr>
<tr>
<td>Strain Ec Phi Factor</td>
<td>&gt;0</td>
<td>2.7</td>
<td>Aging coefficient of concrete. This affects deflection due to shrinkage.</td>
</tr>
</tbody>
</table>

See the section entitled *Beam Deflection and Camber* in Chapter 2 for a description of beam deflection and camber.

### B6 Vibration

Table B6 lists the composite beam overwrite items available for Vibration.

Table B-6: Composite Beam Overwrites for Vibration

<table>
<thead>
<tr>
<th>Item</th>
<th>Possible Values</th>
<th>Default Value</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>Vibration Criterion</td>
<td>Walking, Rhythmic, Sensitive Equipment, None</td>
<td>Walking</td>
<td>Vibration criterion to be considered in the design.</td>
</tr>
<tr>
<td>Occupancy Category</td>
<td>Paper Office, Electronics Office, Residential</td>
<td>Paper Office</td>
<td>Occupancy category to be considered in the design. Selecting this item changes the default parameters for the damping ratio (DG11 Table 4.1) and vibrational acceleration limit as a fraction of acceleration due to gravity (a_0/g) (DG11 Table 4.1). However, the default parameters can be changed here.</td>
</tr>
</tbody>
</table>
### Table B-6: Composite Beam Overwrites for Vibration

<table>
<thead>
<tr>
<th>Item</th>
<th>Possible Values</th>
<th>Default Value</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>Damping Ratio</td>
<td>&gt; 0</td>
<td>0.0250</td>
<td>Damping ratio of the system (DG11 Table 4.1, DG11 Section 5.2). The default value comes from the Preferences if the vibration criterion and occupancy category match; otherwise the value comes from the predefined table.</td>
</tr>
<tr>
<td>Bay Frequency</td>
<td></td>
<td>0.000</td>
<td>Panel frequency. This is normally calculated by the program. This controls the vibration analysis significantly.</td>
</tr>
<tr>
<td>Acceleration Limit, (a_0/g)</td>
<td></td>
<td>0.005</td>
<td>Vibrational acceleration limit as a fraction of acceleration due to gravity (a_0/g) for walking excitation (DG11 Table 4.1). Default value comes from the Preferences if the vibration criterion and occupancy category match; otherwise the value comes from the predefined table.</td>
</tr>
<tr>
<td>Additional Dead Load</td>
<td></td>
<td>4</td>
<td>Additional dead load (DL) to be considered as mass source. This increases mass and reduces the natural frequency of the system.</td>
</tr>
<tr>
<td>Additional Live Load</td>
<td></td>
<td>11</td>
<td>Live load (LL) in addition to dead load to be considered as mass source. This increases mass and reduces the natural frequency of the system.</td>
</tr>
<tr>
<td>Additional Colateral Load</td>
<td></td>
<td>0</td>
<td>Additional collateral load (CL), in addition to dead load and live load, to be considered as mass source. This increases mass and reduces the natural frequency of the system.</td>
</tr>
</tbody>
</table>

See the section entitled *Floor Vibration* in Chapter 2 for a description of beam vibration.


